

Nuclear PDFs and D-meson production in the GM-VFNS

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experiment”

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Part I: Nuclear PDFs

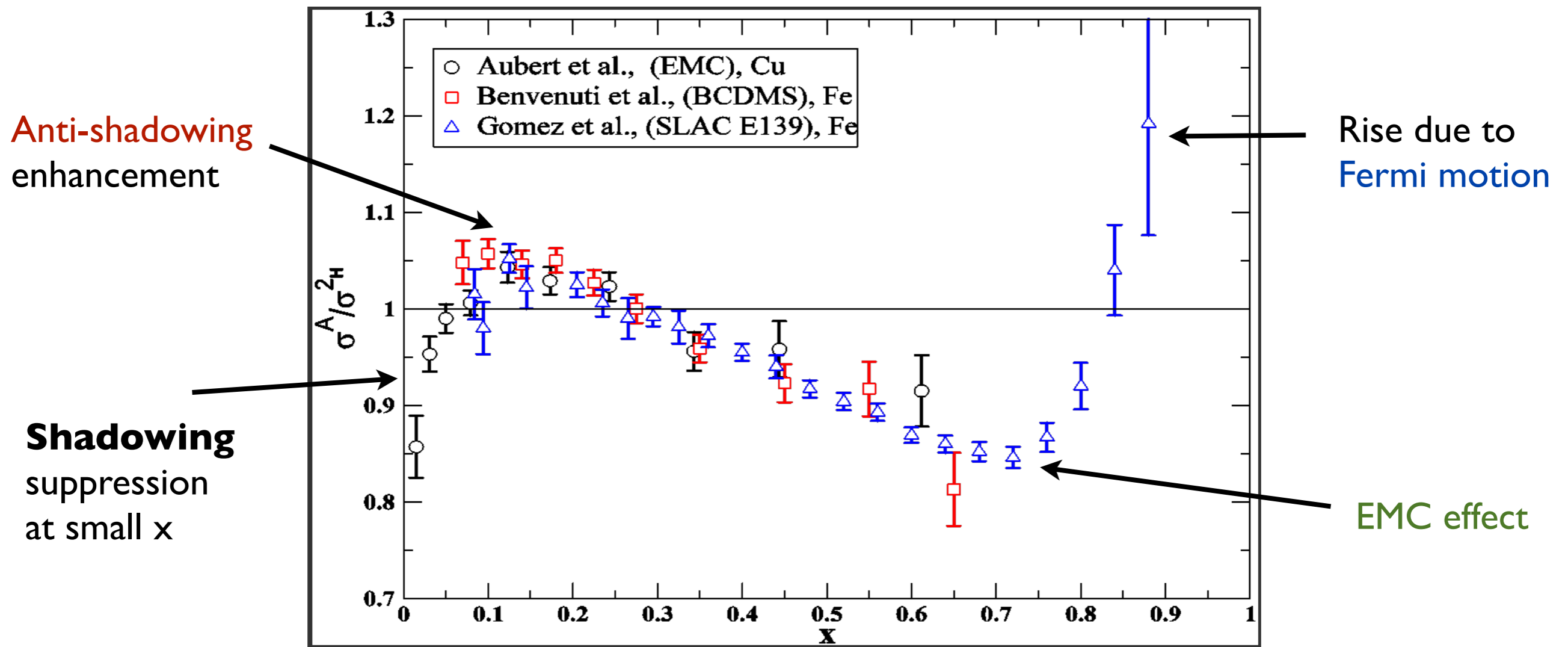
Outline

- Introduction
- Brief review of available nuclear PDFs
- LHC pPb data useful for constraining nPDF

Introduction

Nuclear modifications of DIS structure functions

$$F_2^A(x) \neq ZF_2^p(x) + NF_2^n(x)$$



Can we translate these modifications into **universal nuclear PDFs**?

Nuclear PDFs

- There are at least two motivations for NPDFs:
 1. They encode **information on the partonic structure** of nuclei
 2. They are **crucial tools** for the description of pA and AA collisions at RHIC/LHC and lepton-A DIS
- Predictions for observables have to include **reliable estimates of the uncertainties** due to the NPDFs
- So far NPDFs are determined by performing **global analyses of data** similar to global analyses of proton PDFs

Theoretical Framework

- Factorization theorems
 - provide (field theoretical) **definitions of universal PDFs**
 - make the formalism **predictive**
 - make a statement about the **error**
- **PDFs** and predictions for **observables+uncertainties** **refer to this standard pQCD framework**
- There might be breaking of QCD factorization, deviations from **DGLAP** evolution — in particular in a nuclear environment

Still need solid understanding of standard framework to establish deviations!

In the nuclear case, consider factorization as a **working assumption** to be tested phenomenologically

Theoretical Framework

- Factorization theorems

- provide (field theoretical) definitions of universal PDFs

- make the formalism predictive

-

Factorization:

pp : Yes

pA : probably Yes

AA : ???

- PDFs
start

this

- The
evolution

Need careful analysis of data in pp , pA , and AA !

DGLAP

- Still
to be

Questions:

In pA : How big are higher twist terms?

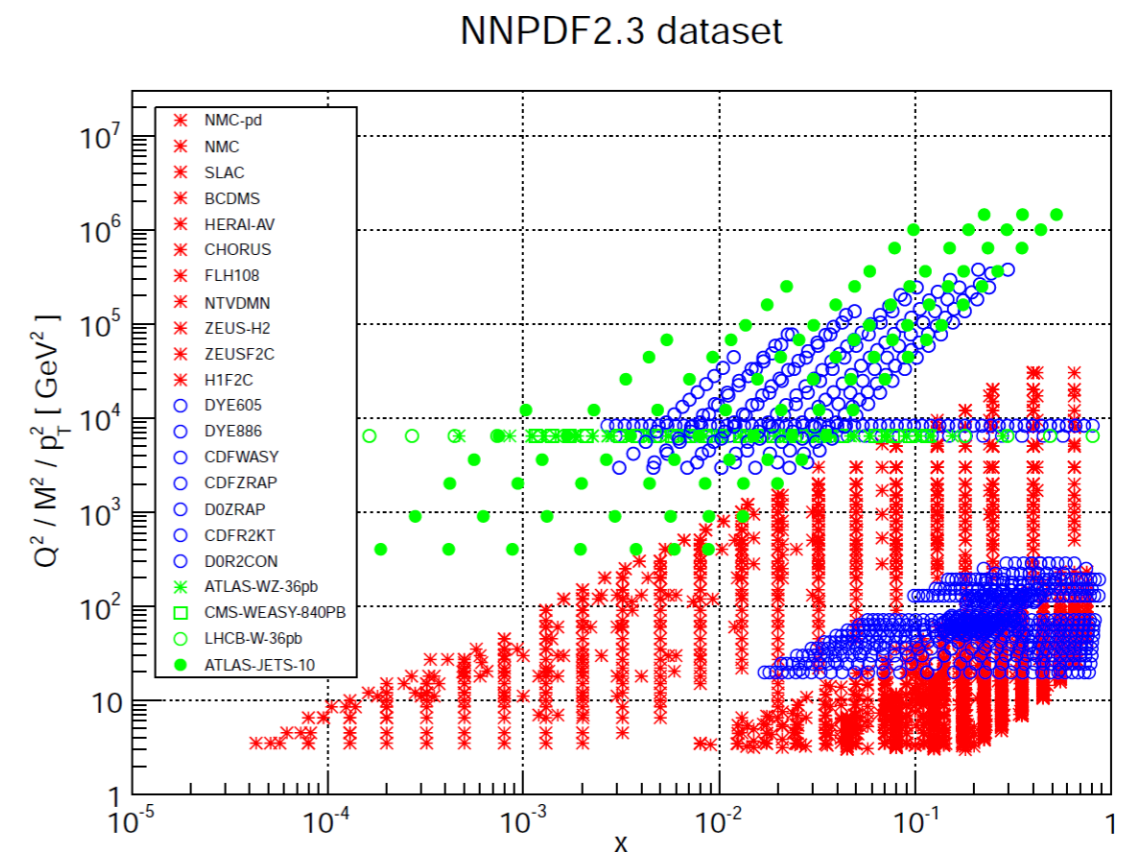
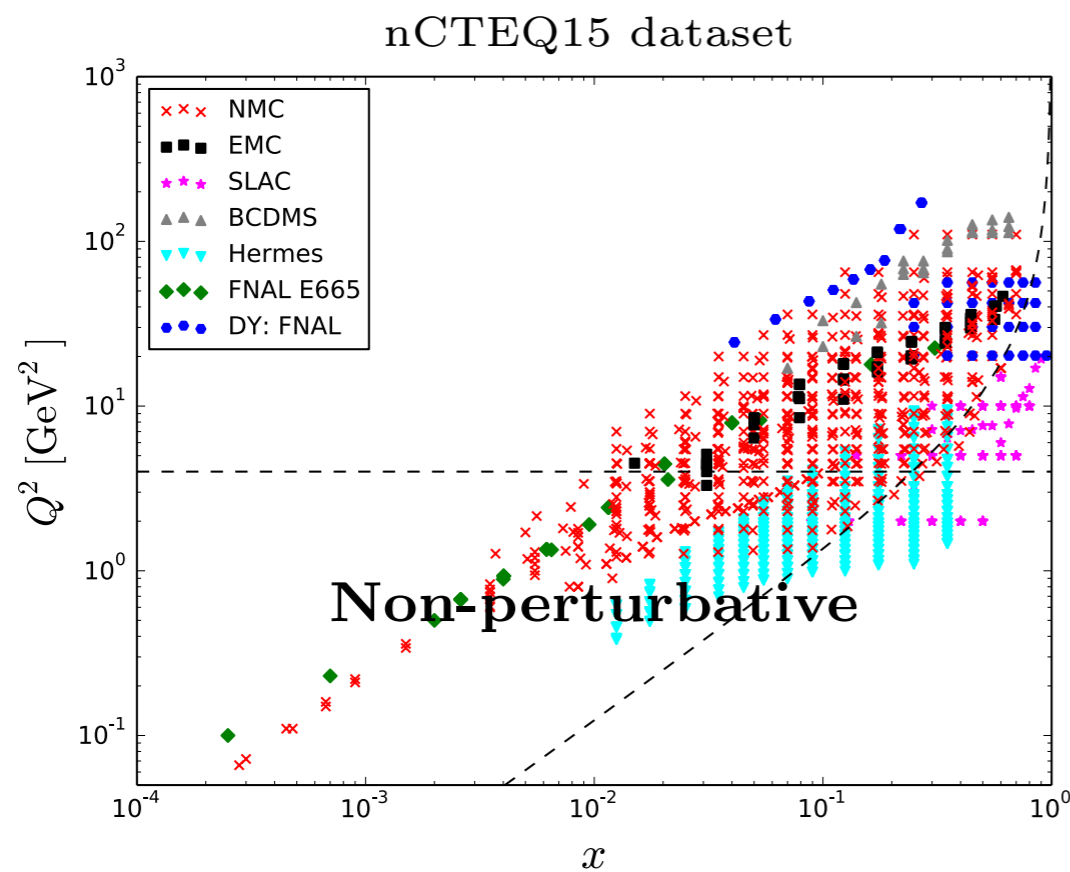
In AA : If factorization breaking, how big?

Is there an alternative to the factorization approach?

In the nuclear case, consider factorization as a **working assumption** to be tested phenomenologically

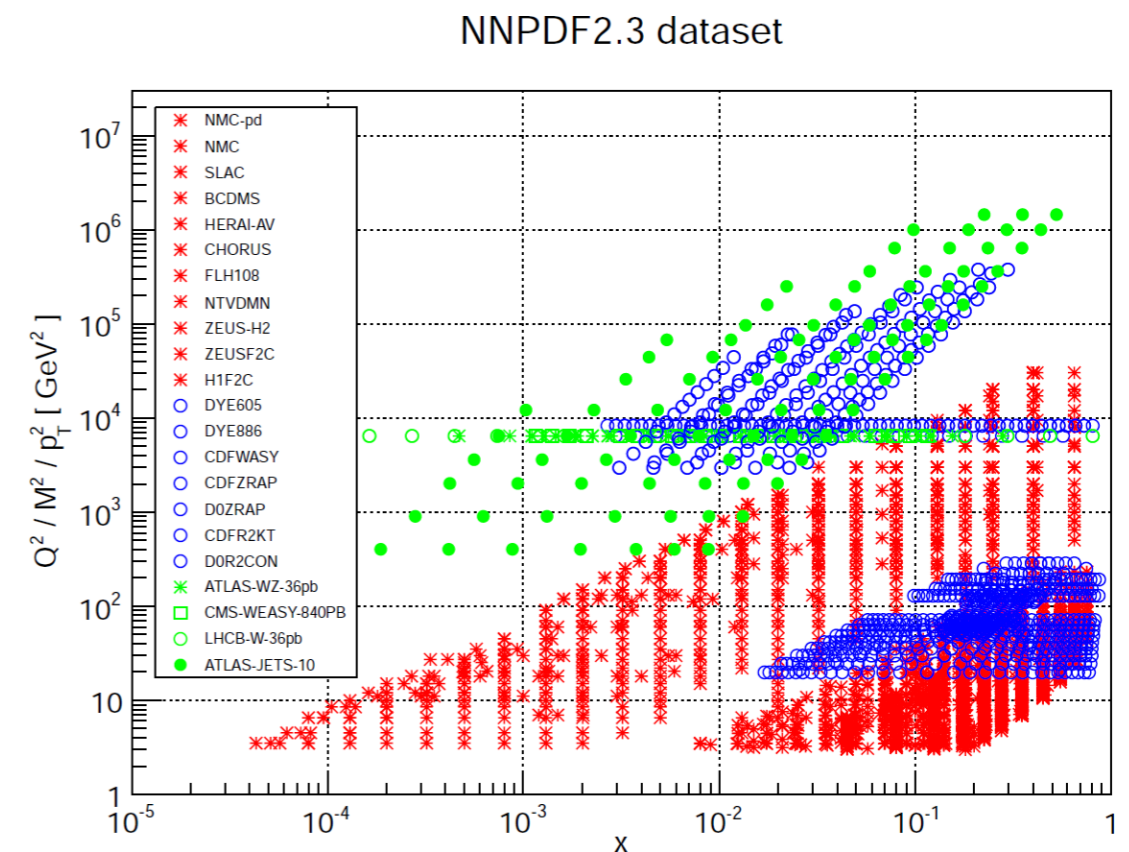
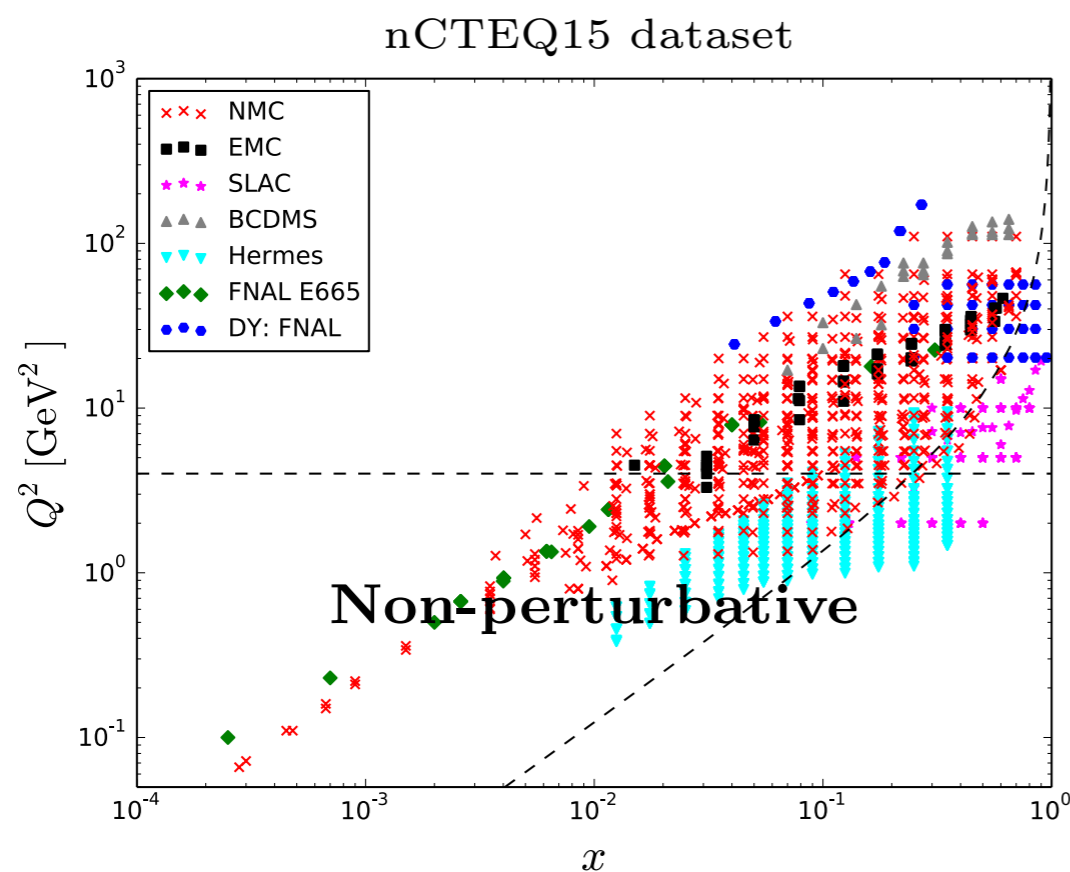
Main differences with free-proton PDFs

- Theoretical status of factorization
- Parametrization: more parameters to model A -dependence
- Less data constraints, much(!) smaller kinematic coverage



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- Less data constraints → more **assumptions** about input PDFs
- Assumptions “hide” uncertainties!

Brief review of available nuclear PDFs

Available nuclear PDFs (NLO)

- **EPPS'16 (supersedes EPS'09)**

Eskola, Paakkinen, Paukkunen, Salgado, arXiv:1612.0574

NEW

- **nCTEQ'15**

nCTEQ collaboration, PRD93(2016)085037, arXiv:1509.00792

- **DSSZ'11**

de Florian, Sassot, Stratmann, Zurita, PRD85(2012)074028, arXiv:1509.00792

- **HKN'07**

Hirai, Kumano, Nagai, PRC76(2007)065207, arXiv:0709.3038

- **AT'12**

Atashbar Tehrani, PRC86(2012)064301

Available nuclear PDFs (NNLO)

- KA'15

Khanpour, Atashbar Tehrani, PRD93(2016)014026, arXiv:1601.00939

Main differences

- **Used data sets**

- **charged lepton-nucleus DIS, pA DY**: All groups (but **different cuts!**)
(EPPS'16 uses also π -A DY data)
- **RHIC single pion production**: EPPS'16, nCTEQ'15, DSSZ'11
(EPPS now with weight = 1; DSSZ includes nuclear corrections to FFs)
- **neutrino-Pb DIS** (CHORUS): EPPS'16
- **LHC data** (dijet production, W/Z production): EPPS'16

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- **Parametrization**

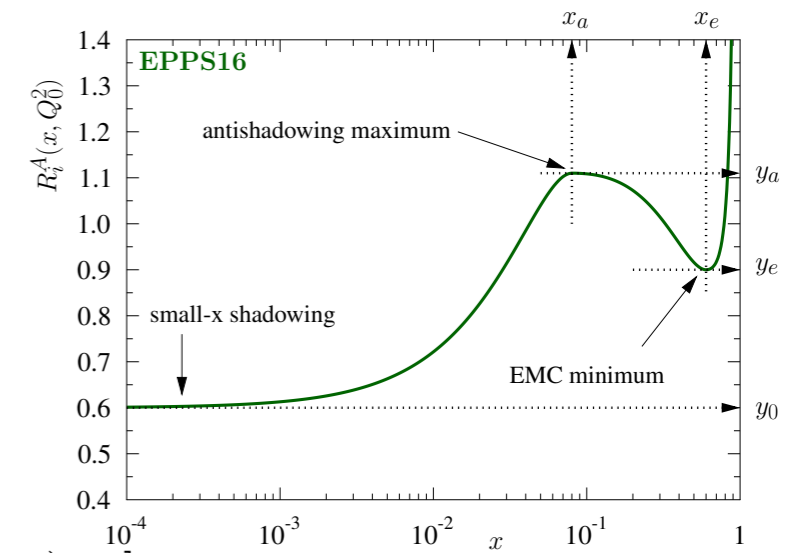
- Multiplicative nuclear correction factors: EPPS'16, DSSZ'11, HKN'07, AT'12, KA'15
(requires proton baseline, parametrization can be quite complicated)
- Native nuclear PDFs (same treatment as proton PDFs): nCTEQ'16

EPPS'16 framework

- NLO PDFs with errors (Hessian method, $\Delta\chi^2 = 52$)
- Parametrization ($x_N < 1$, $Q_0 = 1.3$ GeV, $i = u_v, d_v, \text{ubar}, \text{dbar}, s, g$)

$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A, Z) f_i(x_N, \mu_0),$$

$$R_i(x, A, Z) = \begin{cases} a_0 + (a_1 + a_2 x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x)(1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$



A-dependence of fit parameters: $y_i(A) = y_i(A_{\text{ref}}) \left(\frac{A}{A_{\text{ref}}} \right)^{\gamma_i [y_i(A_{\text{ref}}) - 1]}$

- CT14NLO free proton baseline, D ($A=2$) taken as free
- Data: IA DIS, DY, nu-A DIS, π^0 @RHIC, LHC:dijets, W/Z

EPPS'16 framework: Data

- DIS cut: $Q > 1.3 \text{ GeV}$
- No cut on W
- Underlying assumption: structure function ratios less sensitive to higher twist and TMC

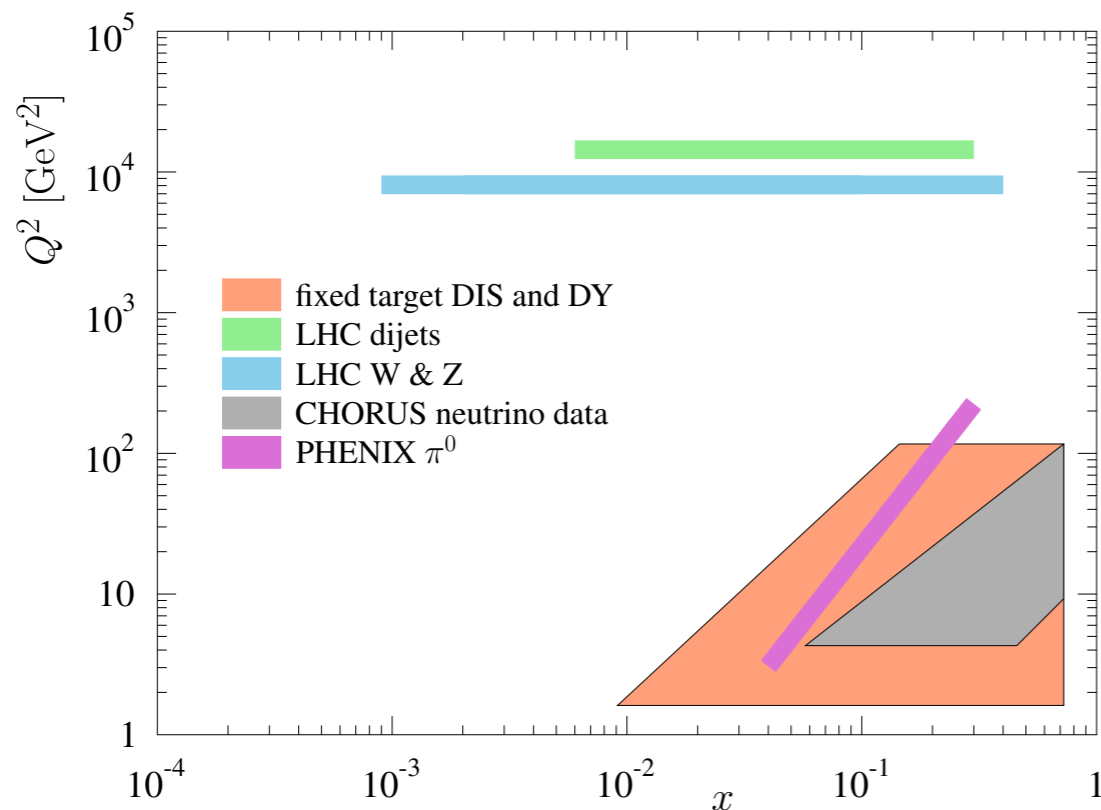
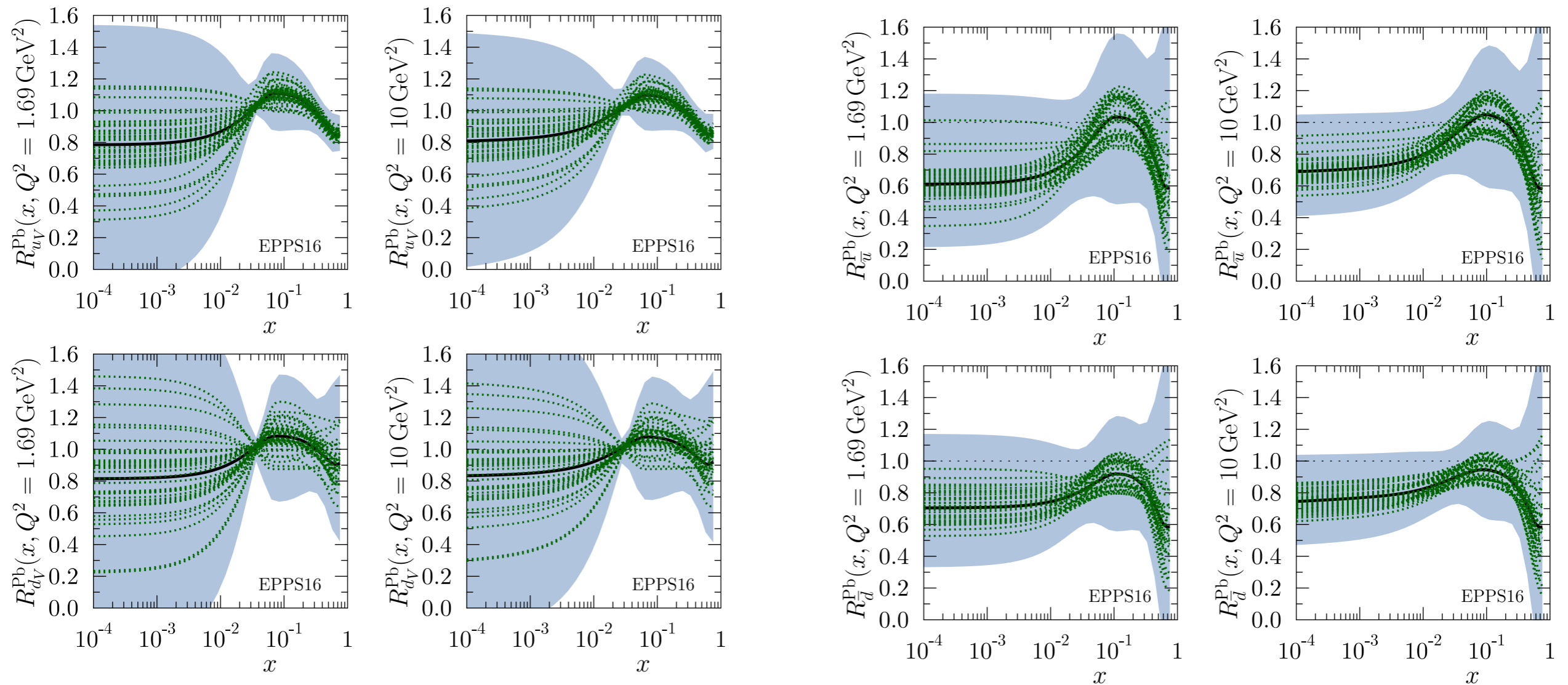


Fig. 2 The approximate regions in the (x, Q^2) plane at which different data in the EPPS16 fit probe the nuclear PDFs.

Experiment	Observable	Collisions	Data points	χ^2
SLAC E139	DIS	$e^- \text{He}(4), e^- \text{D}$	21	12.2
CERN NMC 95, re.	DIS	$\mu^- \text{He}(4), \mu^- \text{D}$	16	18.0
CERN NMC 95	DIS	$\mu^- \text{Li}(6), \mu^- \text{D}$	15	18.4
CERN NMC 95, Q^2 dep.	DIS	$\mu^- \text{Li}(6), \mu^- \text{D}$	153	161.2
SLAC E139	DIS	$e^- \text{Be}(9), e^- \text{D}$	20	12.9
CERN NMC 96	DIS	$\mu^- \text{Be}(9), \mu^- \text{C}$	15	4.4
SLAC E139	DIS	$e^- \text{C}(12), e^- \text{D}$	7	6.4
CERN NMC 95	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	15	9.0
CERN NMC 95, Q^2 dep.	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	165	133.6
CERN NMC 95, re.	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	16	16.7
CERN NMC 95, re.	DIS	$\mu^- \text{C}(12), \mu^- \text{Li}(6)$	20	27.9
FNAL E772	DY	$p\text{C}(12), p\text{D}$	9	11.3
SLAC E139	DIS	$e^- \text{Al}(27), e^- \text{D}$	20	13.7
CERN NMC 96	DIS	$\mu^- \text{Al}(27), \mu^- \text{C}(12)$	15	5.6
SLAC E139	DIS	$e^- \text{Ca}(40), e^- \text{D}$	7	4.8
FNAL E772	DY	$p\text{Ca}(40), p\text{D}$	9	3.33
CERN NMC 95, re.	DIS	$\mu^- \text{Ca}(40), \mu^- \text{D}$	15	27.6
CERN NMC 95, re.	DIS	$\mu^- \text{Ca}(40), \mu^- \text{Li}(6)$	20	19.5
CERN NMC 96	DIS	$\mu^- \text{Ca}(40), \mu^- \text{C}(12)$	15	6.4
SLAC E139	DIS	$e^- \text{Fe}(56), e^- \text{D}$	26	22.6
FNAL E772	DY	$e^- \text{Fe}(56), e^- \text{D}$	9	3.0
CERN NMC 96	DIS	$\mu^- \text{Fe}(56), \mu^- \text{C}(12)$	15	10.8
FNAL E866	DY	$p\text{Fe}(56), p\text{Be}(9)$	28	20.1
CERN EMC	DIS	$\mu^- \text{Cu}(64), \mu^- \text{D}$	19	15.4
SLAC E139	DIS	$e^- \text{Ag}(108), e^- \text{D}$	7	8.0
CERN NMC 96	DIS	$\mu^- \text{Sn}(117), \mu^- \text{C}(12)$	15	12.5
CERN NMC 96, Q^2 dep.	DIS	$\mu^- \text{Sn}(117), \mu^- \text{C}(12)$	144	87.6
FNAL E772	DY	$p\text{W}(184), p\text{D}$	9	7.2
FNAL E866	DY	$p\text{W}(184), p\text{Be}(9)$	28	26.1
CERN NA10*	DY	$\pi^- \text{W}(184), \pi^- \text{D}$	10	11.6
FNAL E615*	DY	$\pi^+ \text{W}(184), \pi^- \text{W}(184)$	11	10.2
CERN NA3*	DY	$\pi^- \text{Pt}(195), \pi^- \text{H}$	7	4.6
SLAC E139	DIS	$e^- \text{Au}(197), e^- \text{D}$	21	8.4
RHIC PHENIX	π^0	$d\text{Au}(197), pp$	20	6.9
CERN NMC 96	DIS	$\mu^- \text{Pb}(207), \mu^- \text{C}(12)$	15	4.1
CERN CMS*	W^\pm	$p\text{Pb}(208)$	10	8.8
CERN CMS*	Z	$p\text{Pb}(208)$	6	5.8
CERN ATLAS*	Z	$p\text{Pb}(208)$	7	9.6
CERN CMS*	dijet	$p\text{Pb}(208)$	7	5.5
CERN CHORUS*	DIS	$\nu\text{Pb}(208), \bar{\nu}\text{Pb}(208)$	824	998.6
Total			1811	1789

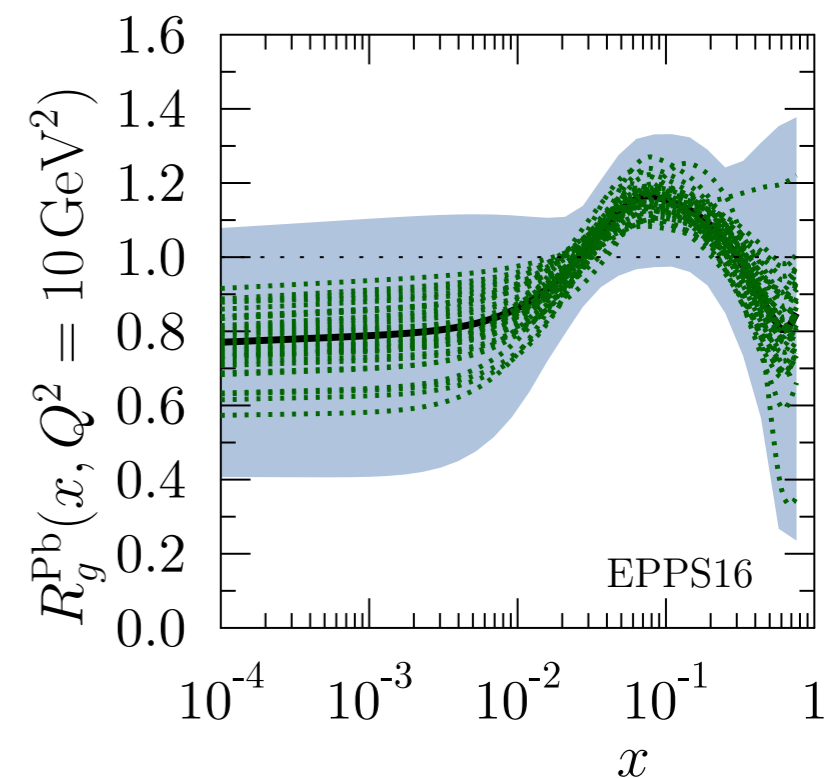
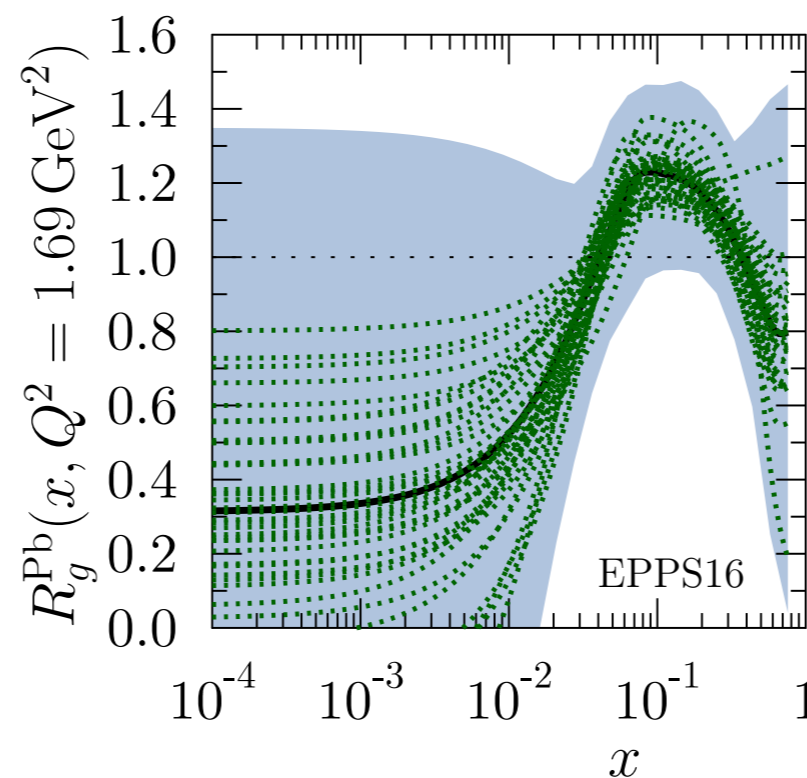
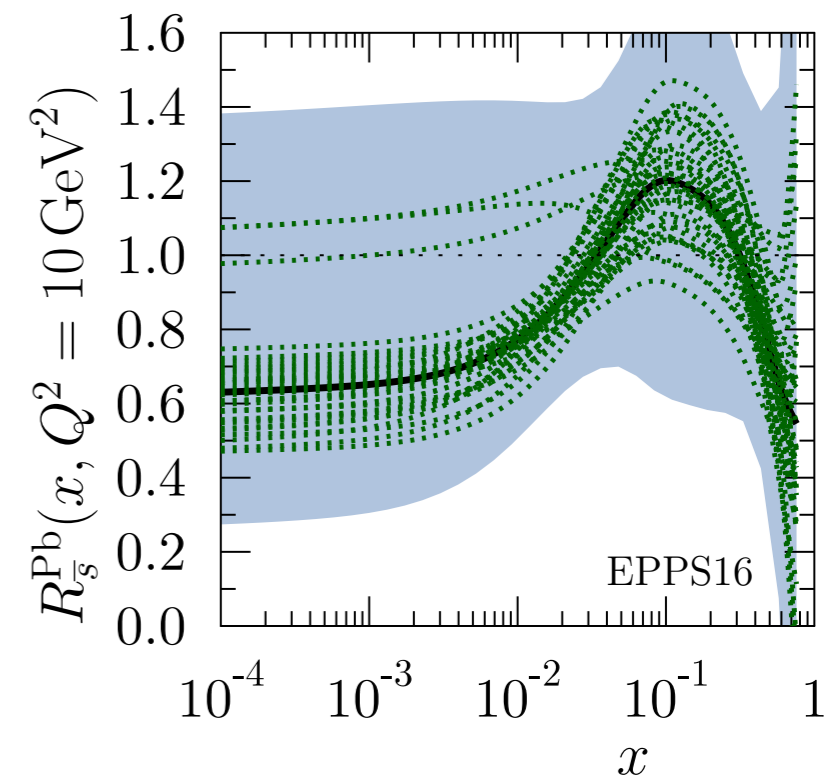
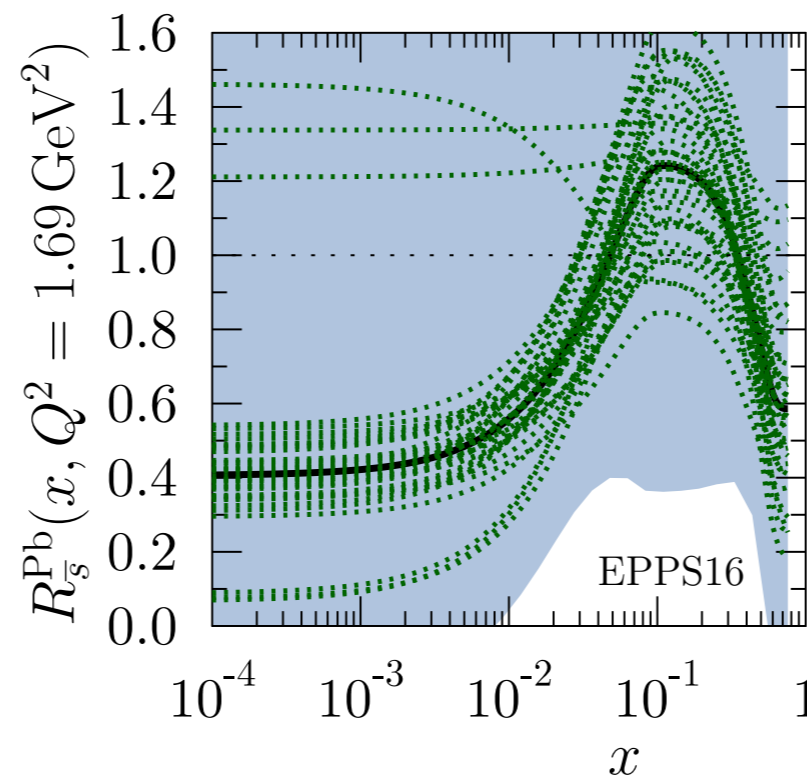
EPPS'16 framework: Results



- Considerably larger uncertainties than EPS'09 despite more data (more flexible param., larger tolerance). Main impact from CHORUS and CMS dijet data.
- No notable tensions with previous data sets. **Supports validity of theoretical framework!**
- Still some parametrization bias (shape of PDFs), still quite a number of assumptions on parametrization
- Some aggressive choices (low DIS cuts, π -A DY data, RHIC π^0 data)

EPPS'16 framework: Results

- Large uncertainties for nuclear gluon distribution
- Nuclear strange PDF poorly constrained
- Clearly more LHC pPb data required
 - from LHC5
 - from LHC8 (much higher statistics)



- Functional form of the **bound proton PDF** same as for the free proton (CTEQ6M, x restricted to $0 < x < 1$)

$$x f_i^{p/A}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}, \quad i = u_v, d_v, g, \dots$$

$$\bar{d}(x, Q_0)/\bar{u}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} + (1 + c_3 x)(1-x)^{c_4}$$

- A -dependent fit parameters (reduces to free proton for $A = 1$)

$$c_k \rightarrow c_k(A) \equiv c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}}), \quad k = \{1, \dots, 5\}$$

- PDFs for nucleus (A, Z)

$$f_i^{(A,Z)}(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{A-Z}{A} f_i^{n/A}(x, Q)$$

(bound neutron PDF $f_i^{n/A}$ by isospin symmetry)

nCTEQ'15 framework: Data sets

- NC DIS & DY

CERN BCDMS & EMC & NMC

$N = (\text{D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W})$

FNAL E-665

$N = (\text{D, C, Ca, Pb, Xe})$

DESY Hermes

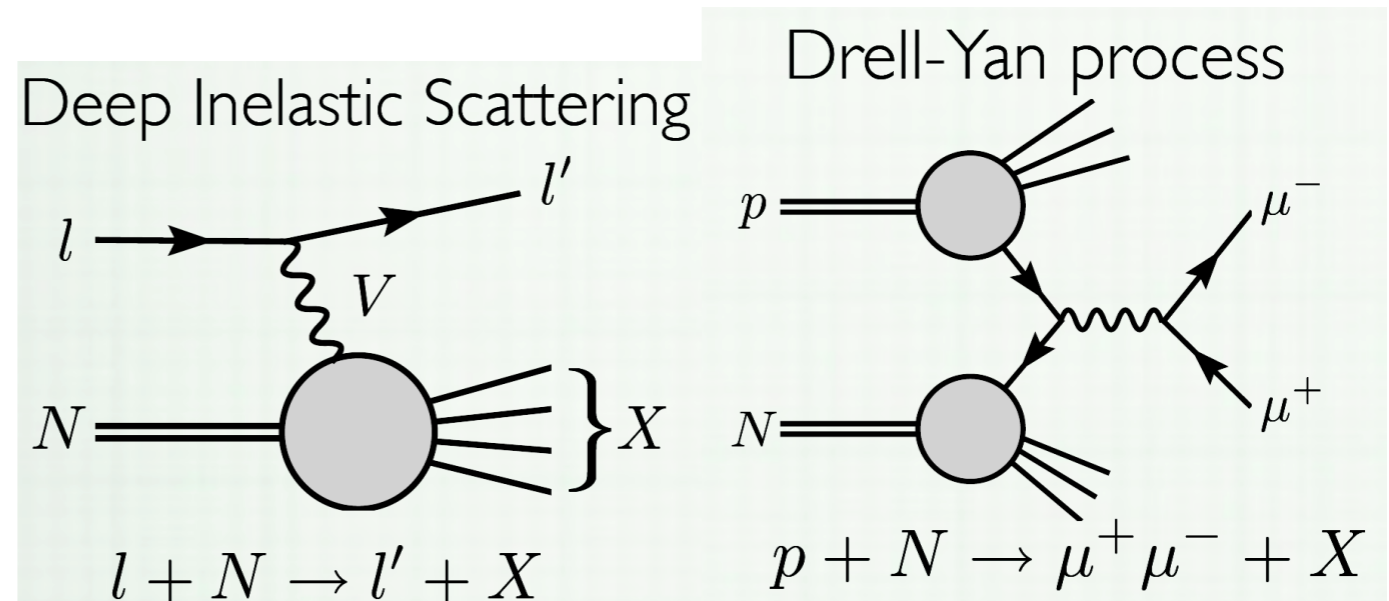
$N = (\text{D, He, N, Kr})$

SLAC E-139 & E-049

$N = (\text{D, Ag, Al, Au, Be, C, Ca, Fe, He})$

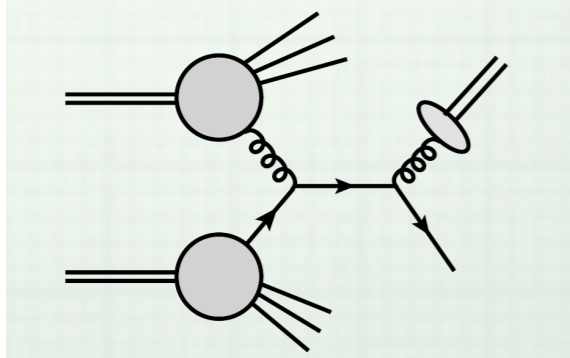
FNAL E-772 & E-886

$N = (\text{D, C, Ca, Fe, W})$



- Single pion production (new)

Single pion production

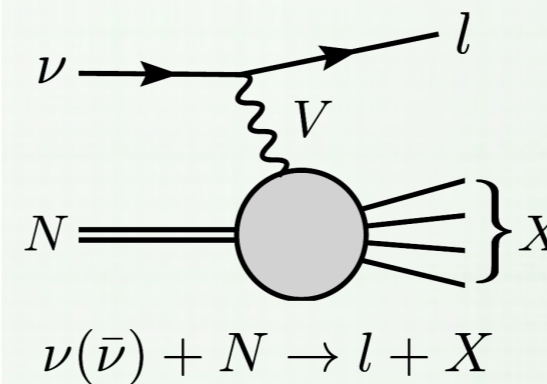


RHIC - PHENIX & STAR

$N = \text{Au}$

- Neutrino (to be included later)

Deep Inelastic Scattering



CHORUS CCFR & NuTeV

$N = \text{Pb } N = \text{Fe}$

Fit properties:

- fit @NLO
- $Q_0 = 1.3\text{GeV}$
- using ACOT heavy quark scheme
- kinematic cuts:
 $Q > 2\text{GeV}$, $W > 3.5\text{GeV}$
 $p_T > 1.7\text{ GeV}$
- 708 (DIS & DY) + 32 (single π^0)
= 740 data points after cuts
- 16+2 free parameters
 - 7 gluon
 - 7 valence
 - 2 sea
 - 2 pion data normalizations
- $\chi^2 = 587$, giving $\chi^2/\text{dof} = 0.81$

Error analysis:

- use Hessian method

$$\chi^2 = \chi_0^2 + \frac{1}{2} H_{ij} (a_i - a_i^0)(a_j - a_j^0)$$

$$H_{ij} = \frac{\partial^2 \chi^2}{\partial a_i \partial a_j}$$

- tolerance $\Delta\chi^2 = 35$ (every nuclear target within 90% C.L.)
- eigenvalues span 10 orders of magnitude \rightarrow require numerical precision
- use noise reducing derivatives

Fit properties

- fit @M
- $Q_0 =$
- using
- kinem
- $Q > 2$
- $p_T >$
- 708 (1
- = 740
- 16+2
-
-
-
- $\chi^2 =$

Kinematic cuts

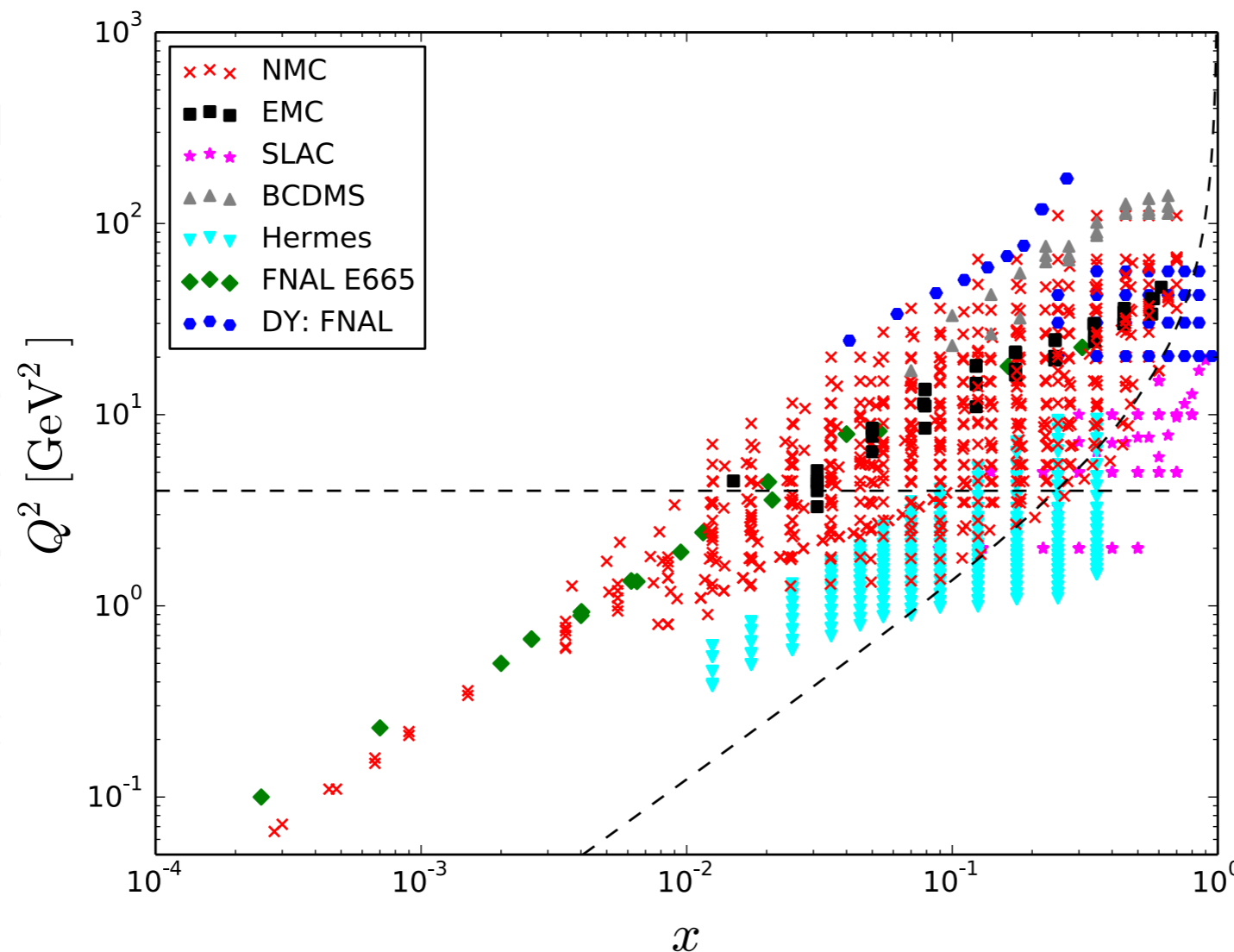
nCTEQ:

$$\begin{cases} Q > 2 \text{ GeV} \\ W > 3.5 \text{ GeV} \end{cases}$$

EPS: $Q > 1.3 \text{ GeV}$

HKN: $Q > 1 \text{ GeV}$

DSSZ: $Q > 1 \text{ GeV}$



$\Delta\chi^2 = 35$ (every
target within 90% C.L.)

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le \rightarrow require numerical

nCTEQ: 740 data points
reducing derivatives
EPS09: 929 data points

Fit properties:

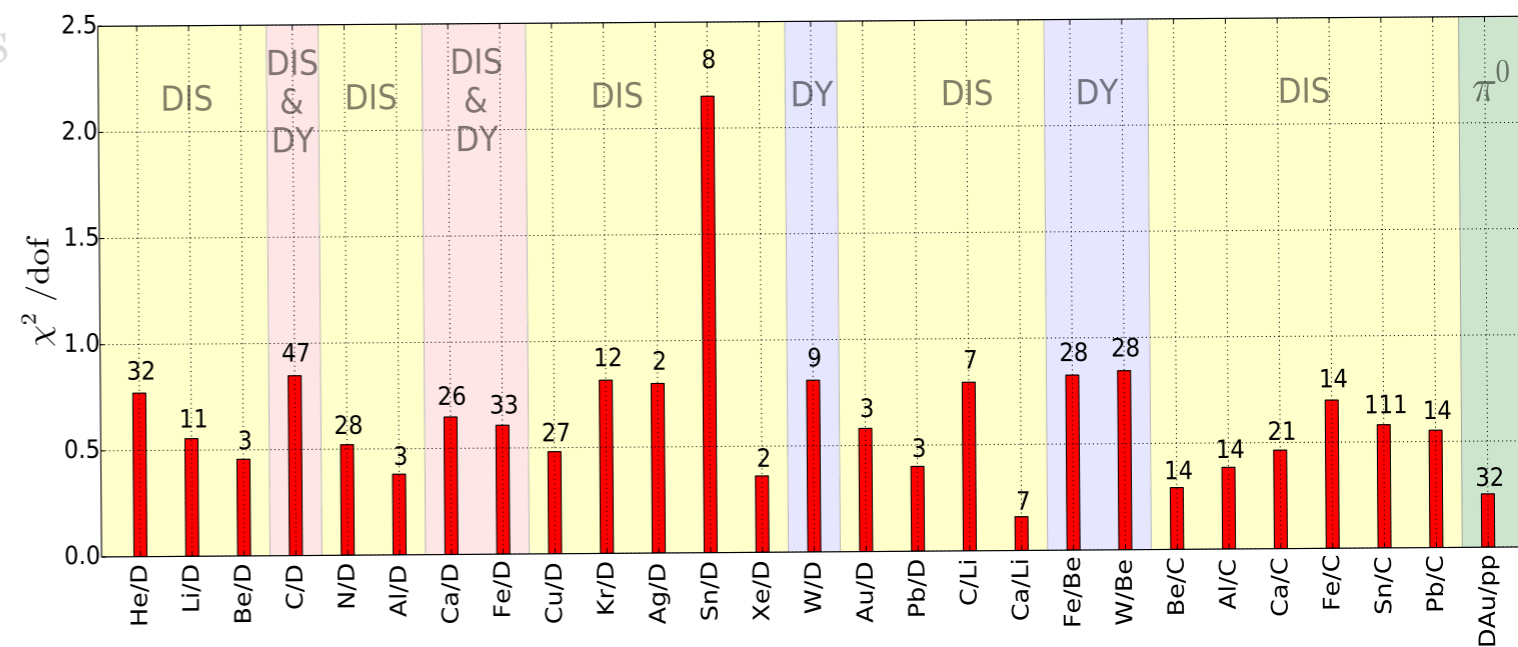
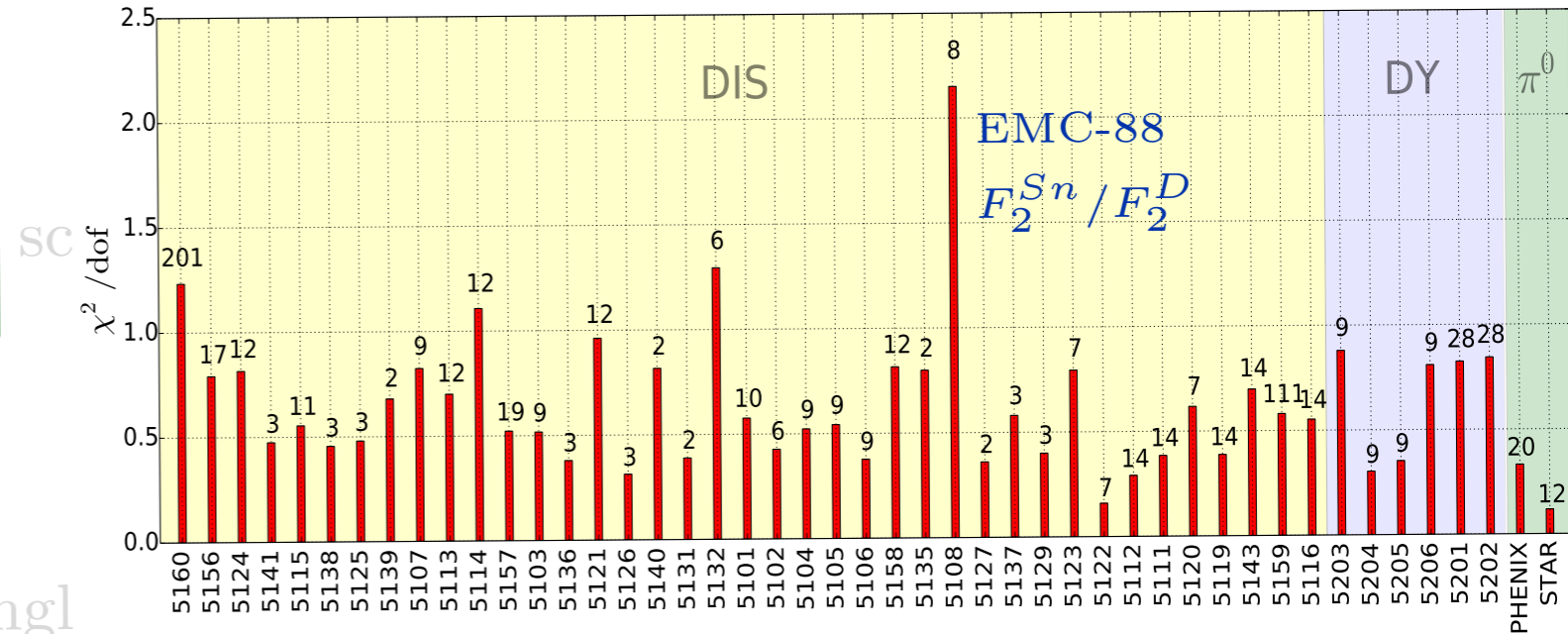
Error analysis:

Fit quality

- $\chi^2/dof = 0.81$

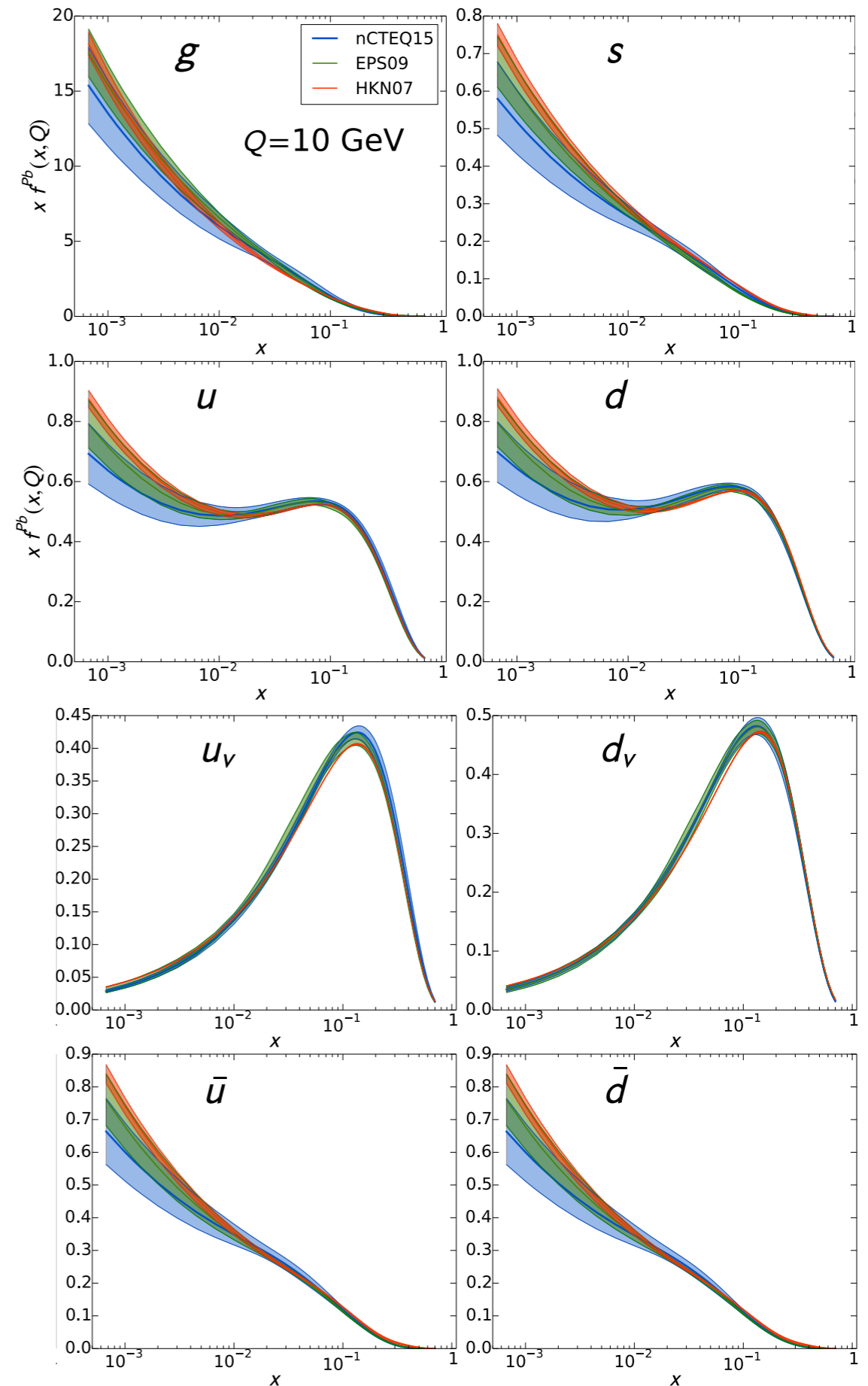
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nCTEQ results

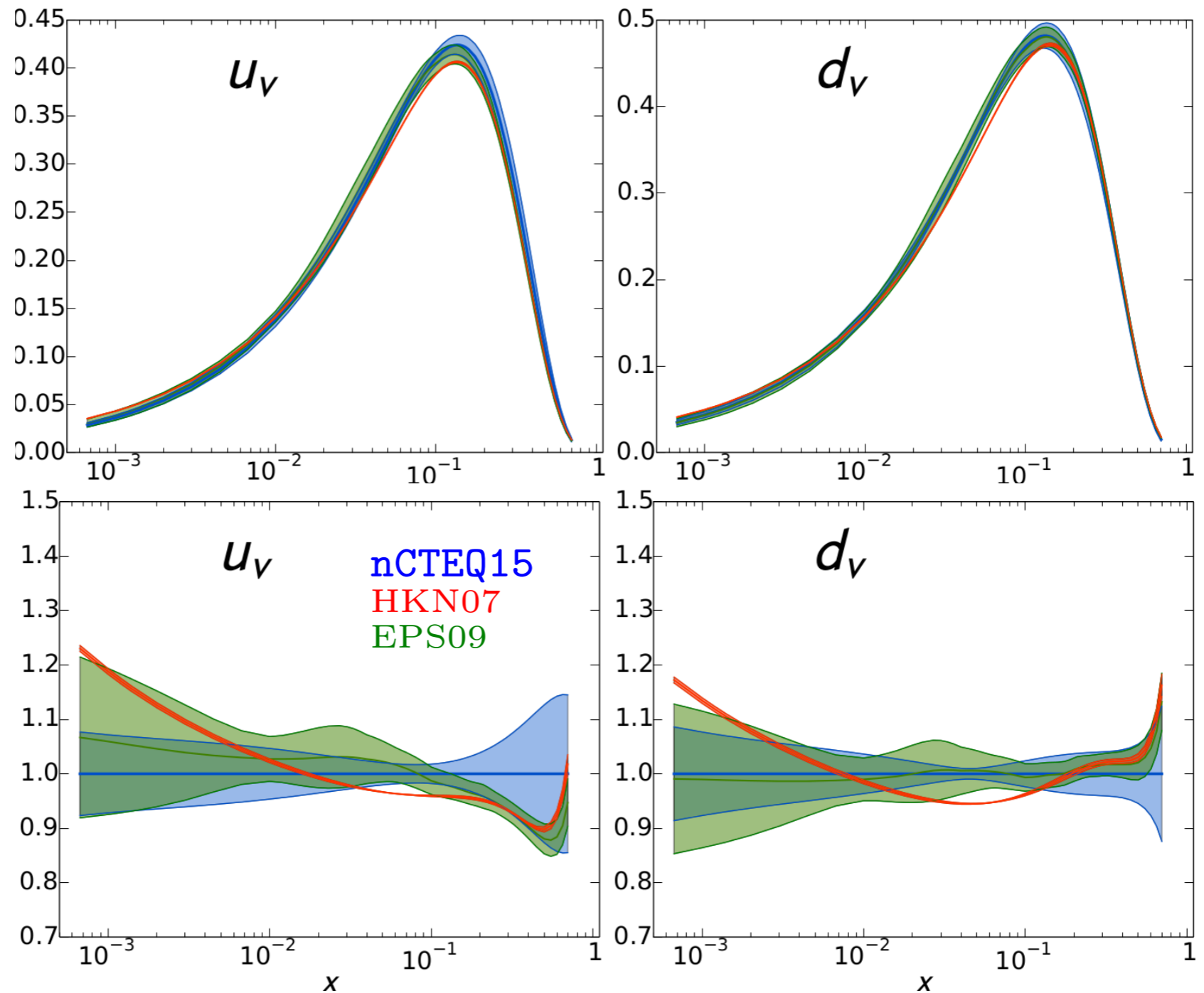
- First global analysis with Hessian error PDFs: [PRD93(2016)085037]
- Figure: PDFs inside lead at $Q=10$ GeV vs x
- nCTEQ features larger uncertainties than previous nPDFs
- better agreement between different groups



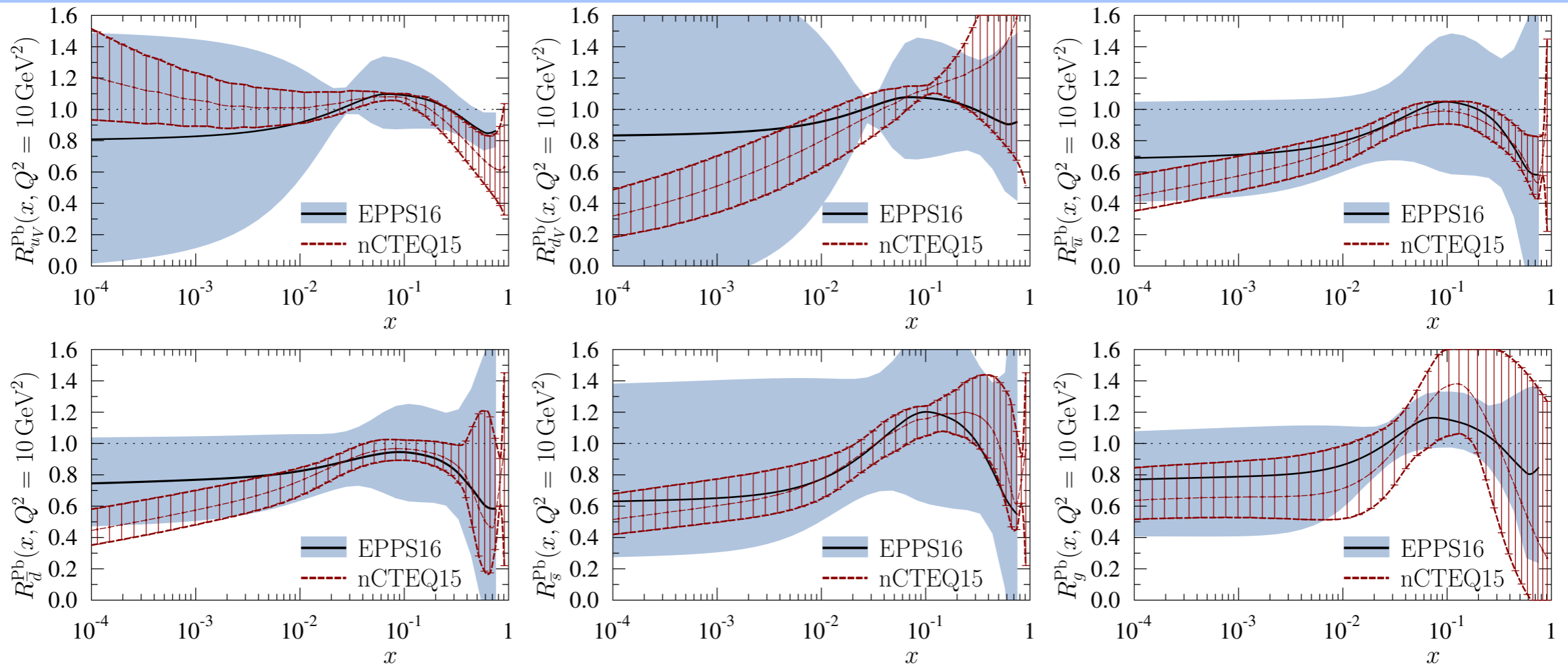
Valence distributions

Full lead nucleus distribution:

$$f^{Pb} = \frac{82}{208} f^{p/Pb} + \frac{208 - 82}{208} f^{n/Pb}$$

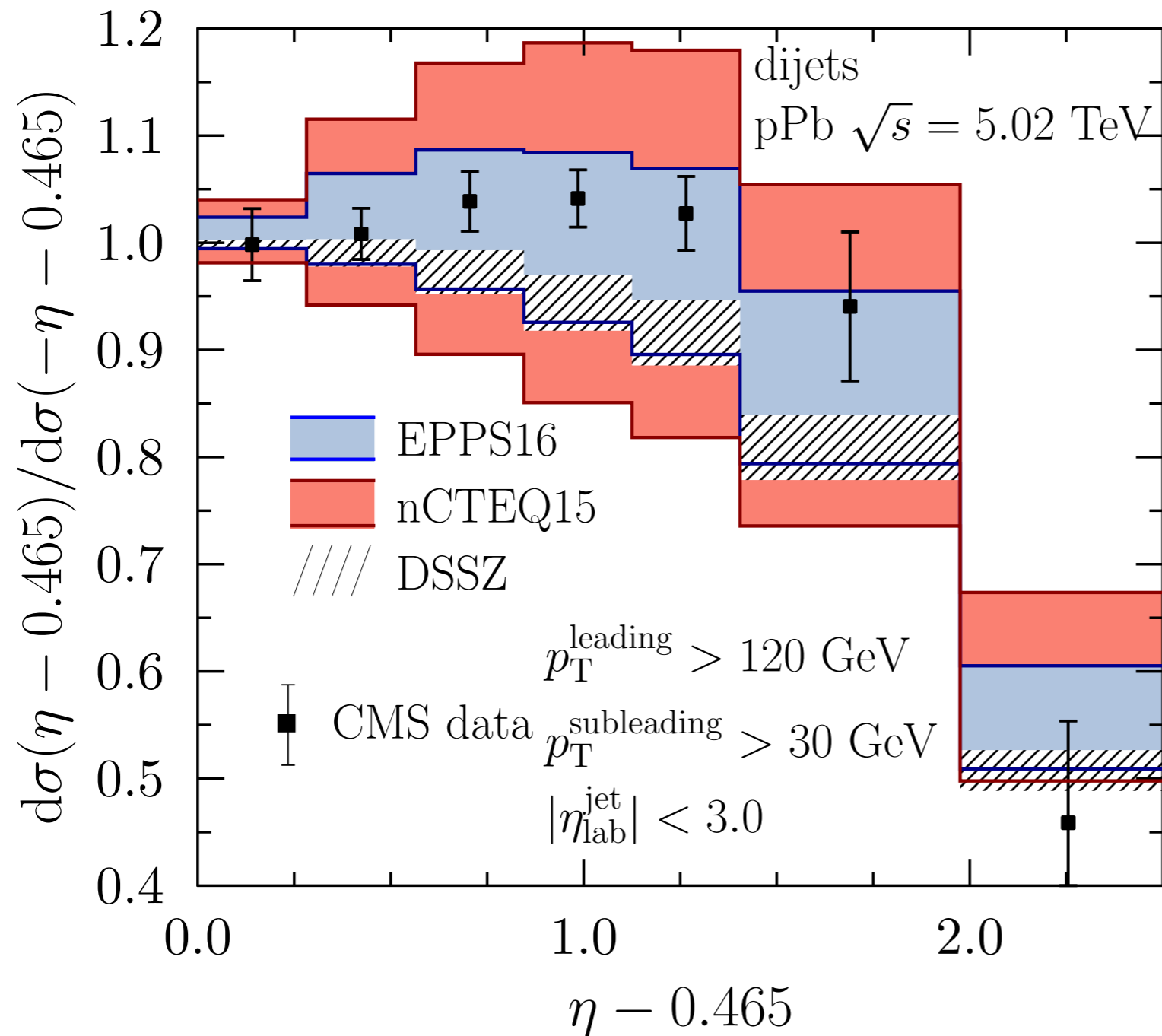


EPPS'16 vs nCTEQ'15 @ $Q^2=10 \text{ GeV}^2$



- Generally good agreement for $x > 0.01$ (nCTEQ has no data constraints for $x < 0.01$)
 $\Delta\chi^2 = 35$ (nCTEQ'15), $\Delta\chi^2 = 52$ (EPPS'16)
- Valence bands at large- x partly differ (valence at small- $x < 10^{-2}$ irrelevant);
 influence from CHORUS data?
- EPPS'16 bands for light sea more realistic; nCTEQ'15 has fewer fit parameters for sea
- Still quite some parametrization bias even for EPPS'16

Comparison with dijet data



- nCTEQ'15 in agreement with CMS data; including CMS dijet data in global analysis will help
- DSSZ gluon needs to be revised since not enough shadowed **OR** energy loss effects need to be included?

LHC p-Pb data useful for constraining nPDF

Available pPb LHC data useful for nPDF fits

- W/Z production
 - ATLAS [[arXiv:1507.06232](#), [ATLAS-CONF-2015-056](#)]
 - CMS [[arXiv:1512.06461](#), [arXiv:1503.05825](#)]
 - LHCb [[arXiv:1406.2885](#)]
 - ALICE [[arXiv:1511.06398](#)]
- Jets
 - ATLAS [[arXiv:1412.4092](#)]
 - CMS [[arXiv:1401.4433](#), [CMS-PAS-HIN-14-001](#)]
- Charged particle production (FFs dependence)
 - CMS [[CMS-PAS-HIN-12-017](#)]
 - ALICE [[arXiv:1405.2737](#), [arXiv:1505.04717](#)]
- Isolated photons (PbPb)
 - ATLAS [[arXiv:1506.08552](#)]
 - CMS [[arXiv:1201.3093](#)]
 - ALICE [[arXiv:1509.07324](#)]

Available pPb LHC data useful for nPDF fits

light sea,
strange sea

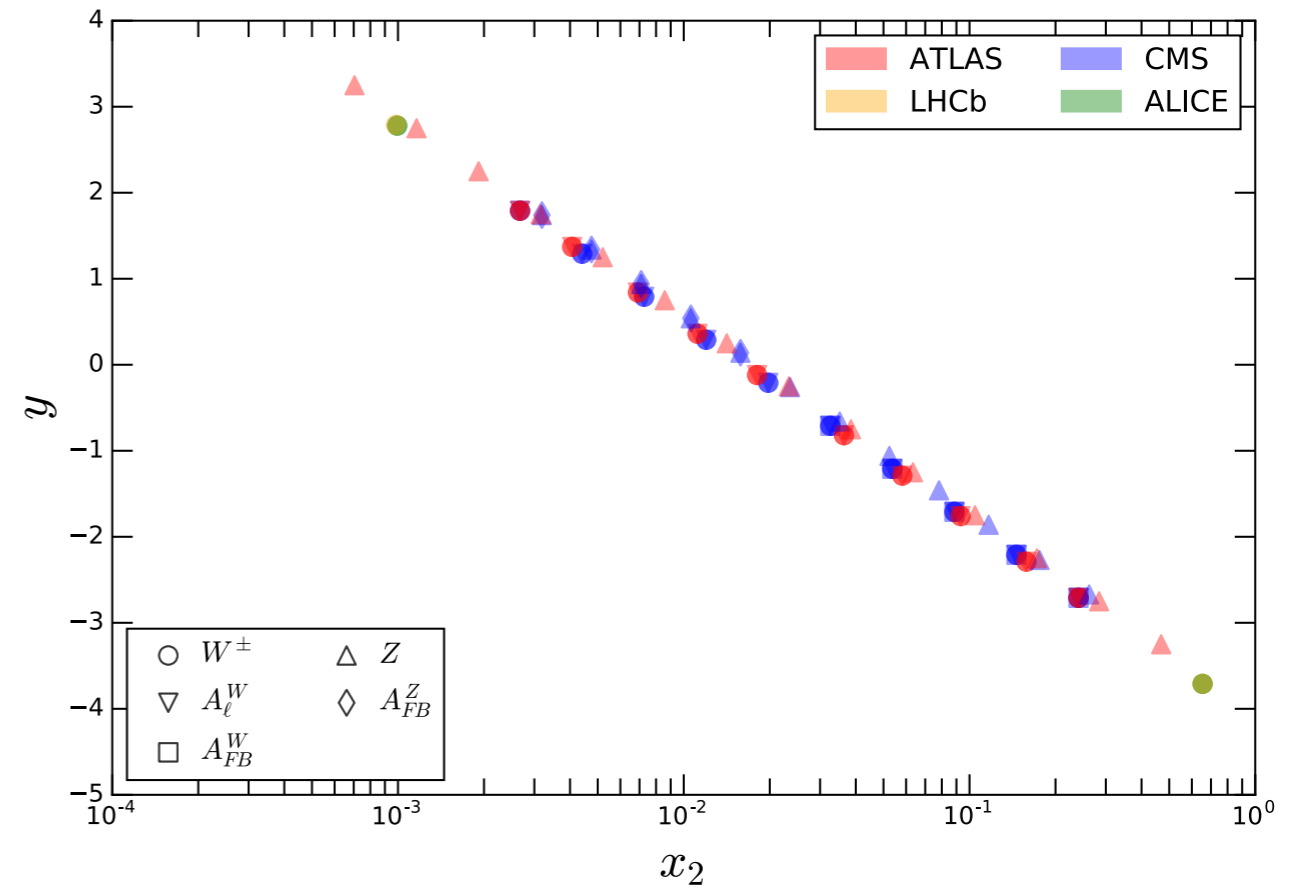
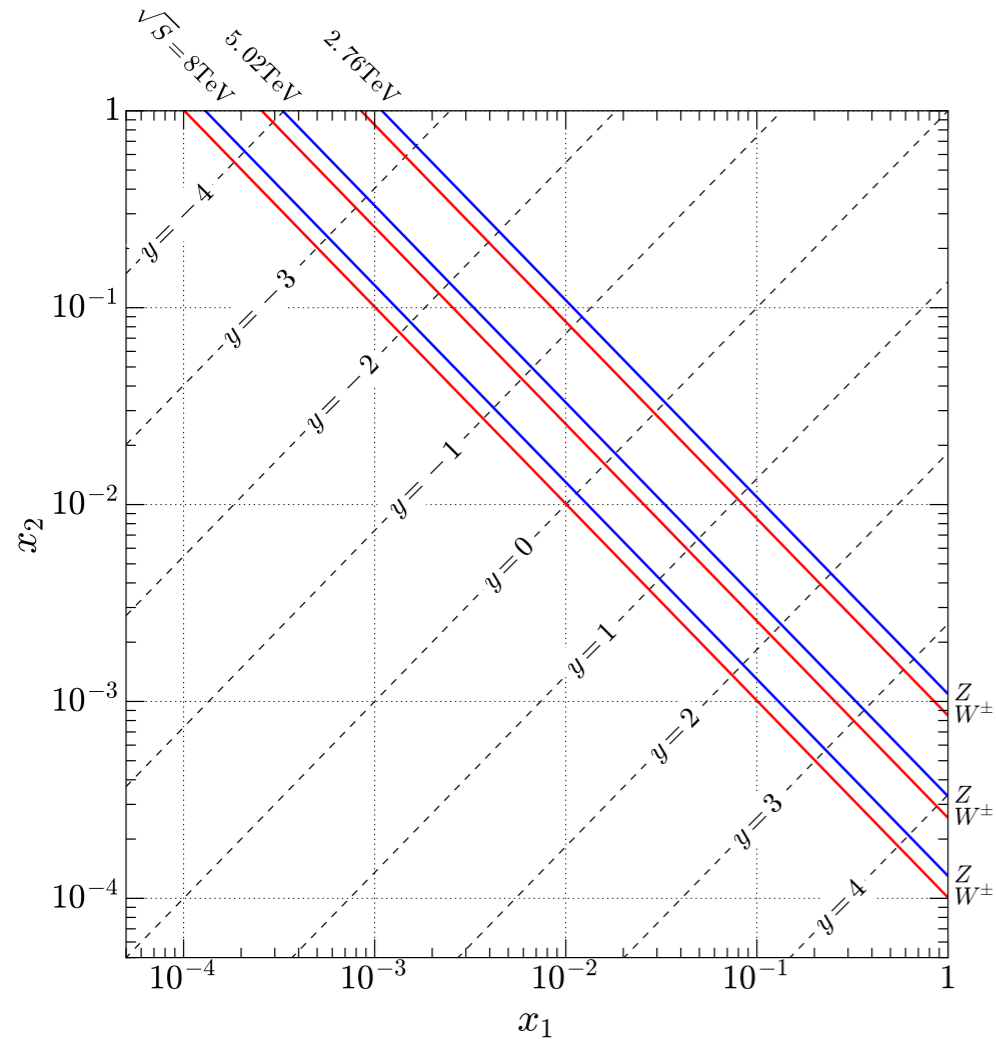
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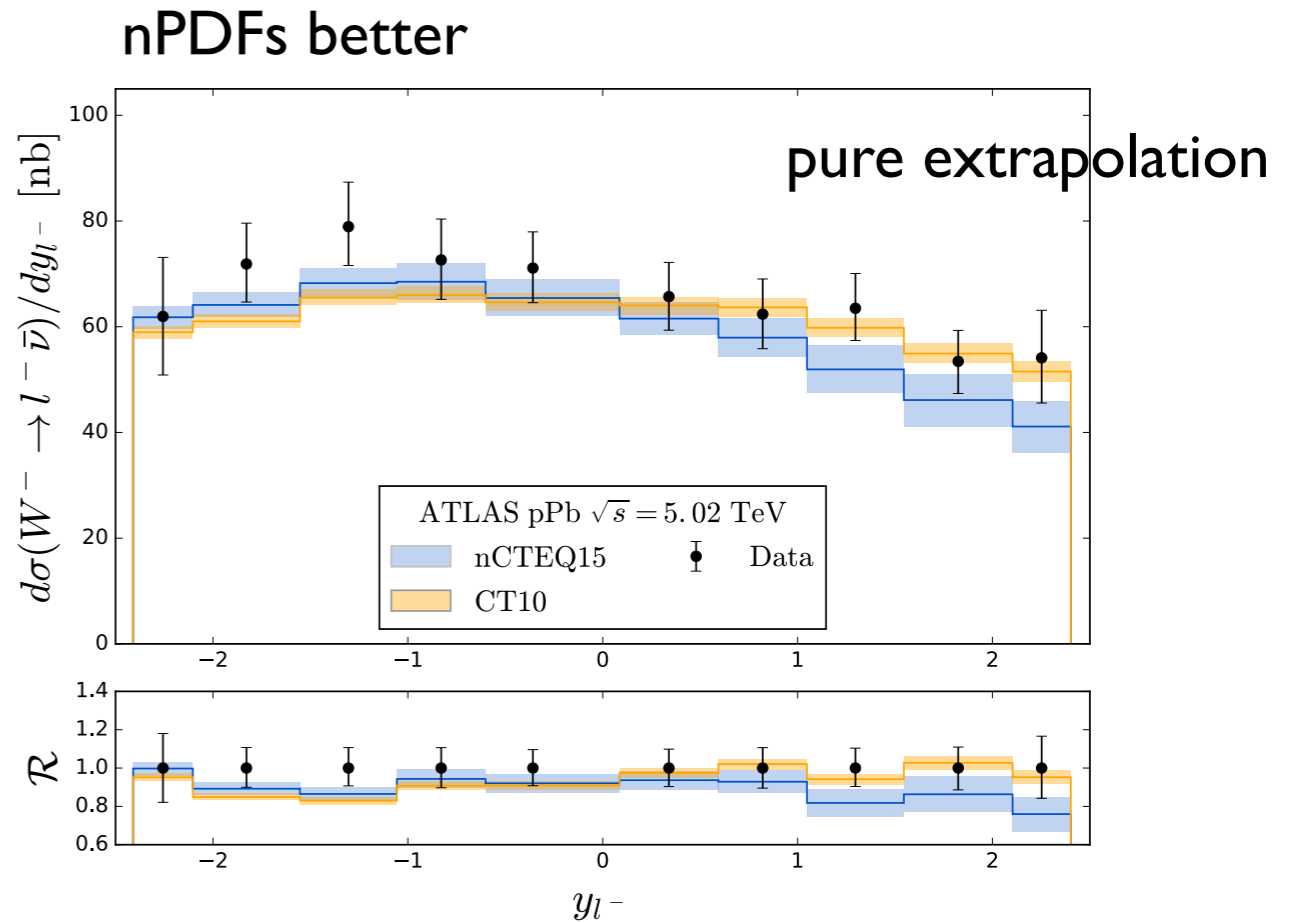
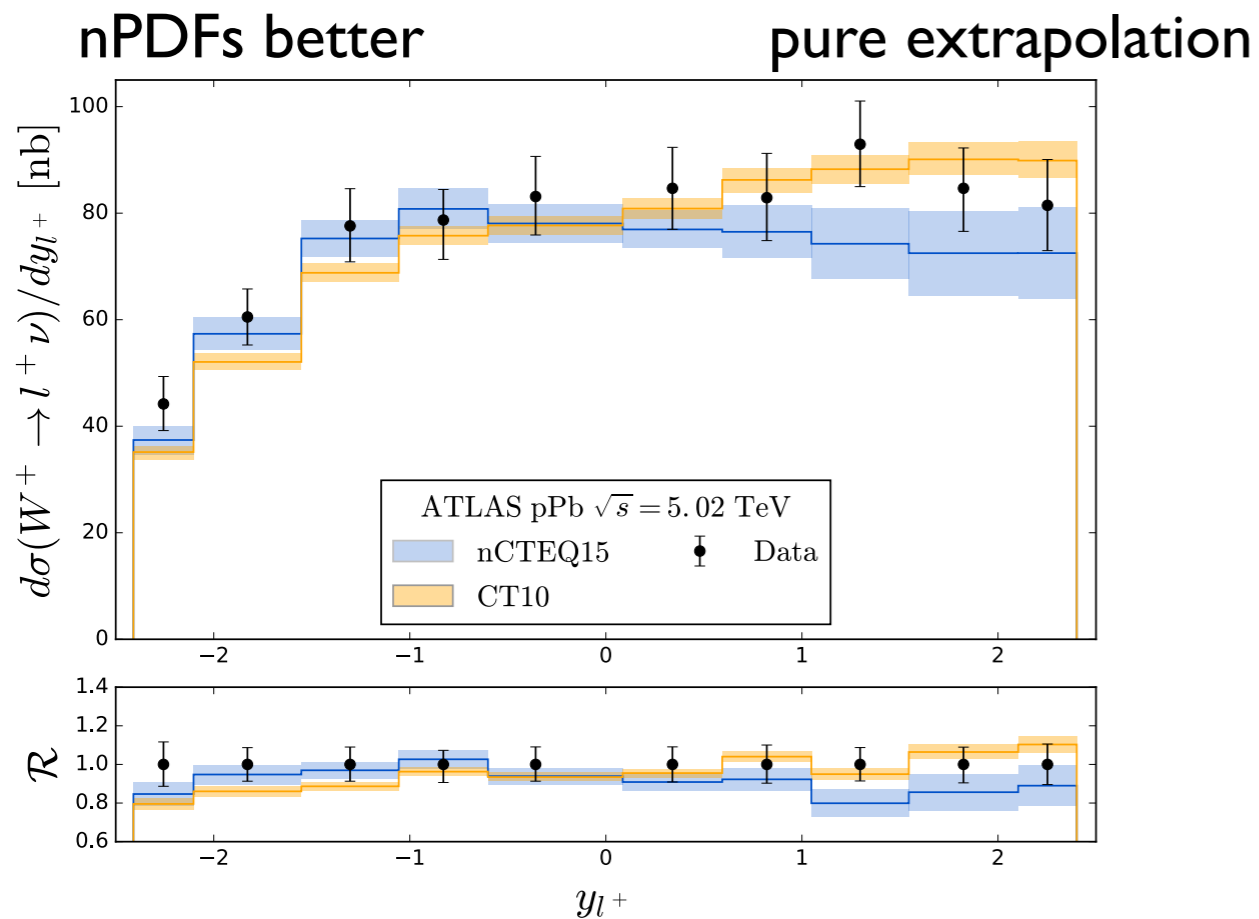
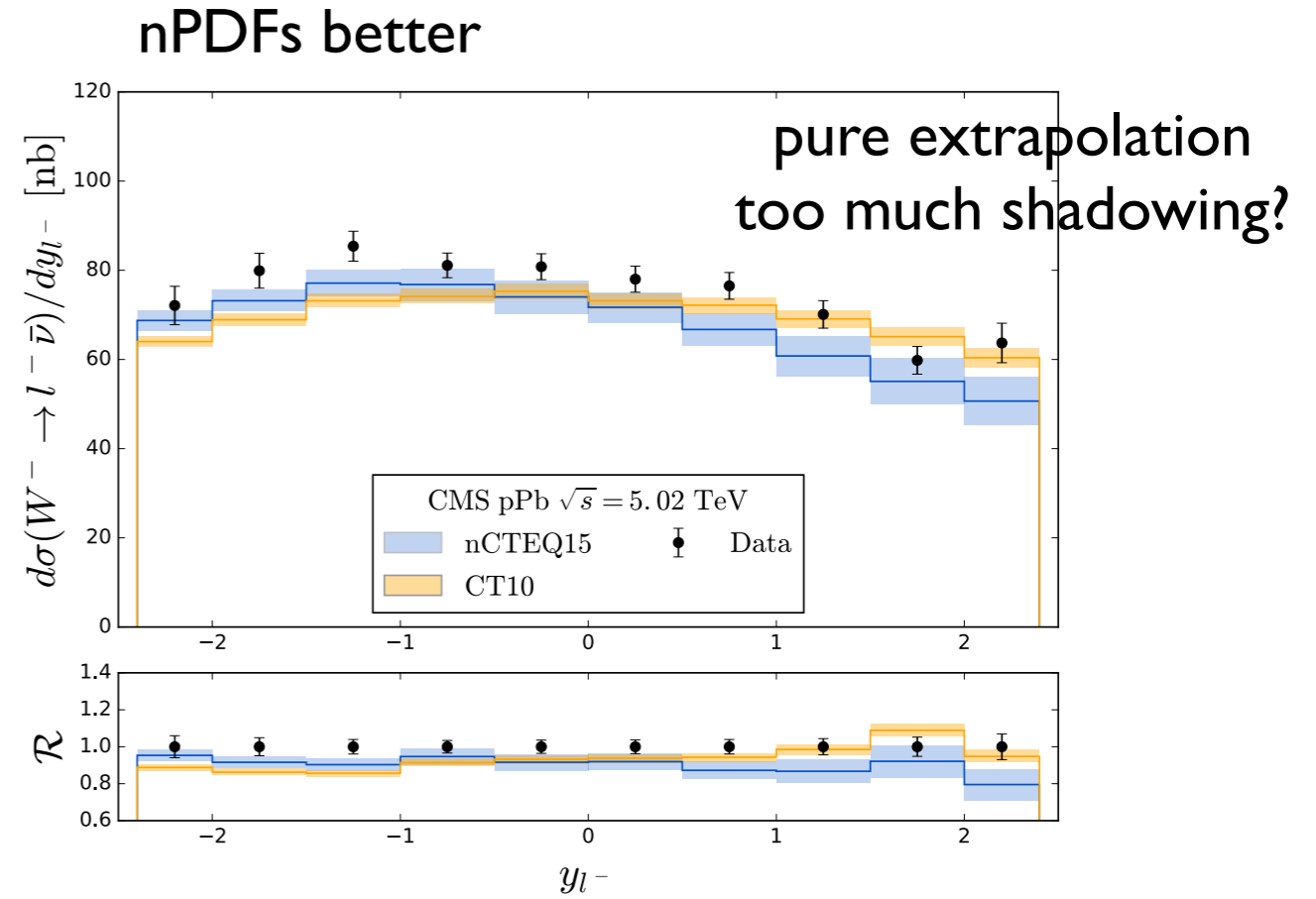
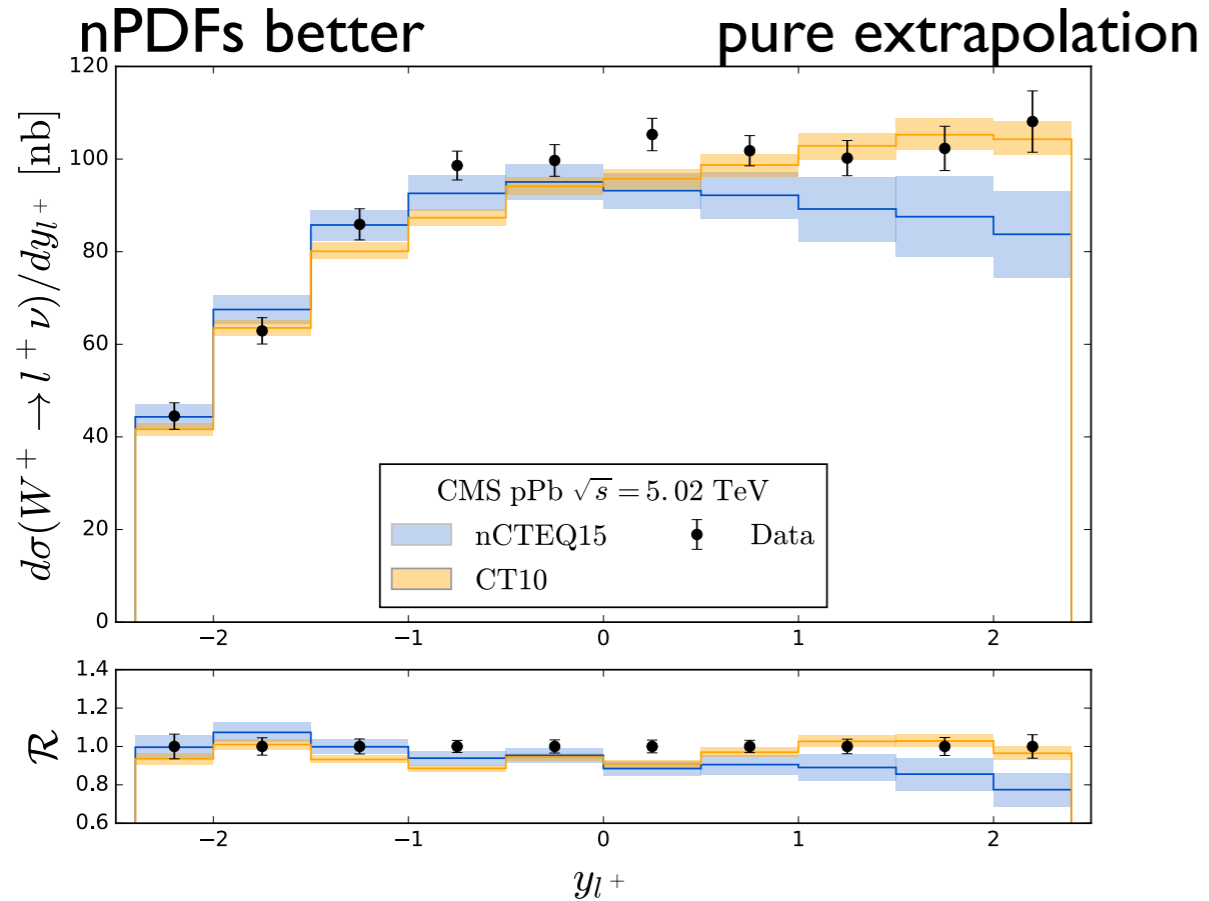
nCTEQ study of W,Z production at LHC

arXiv:1610.02925



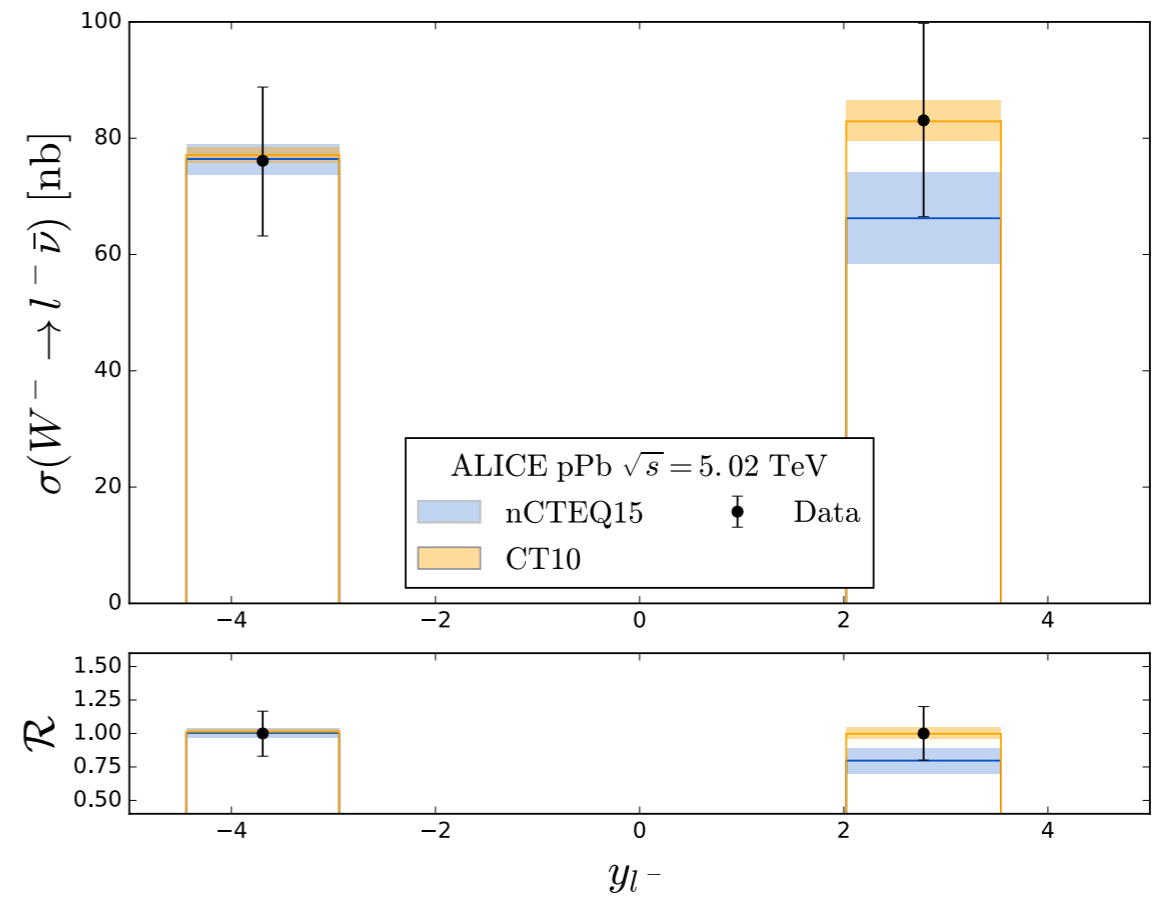
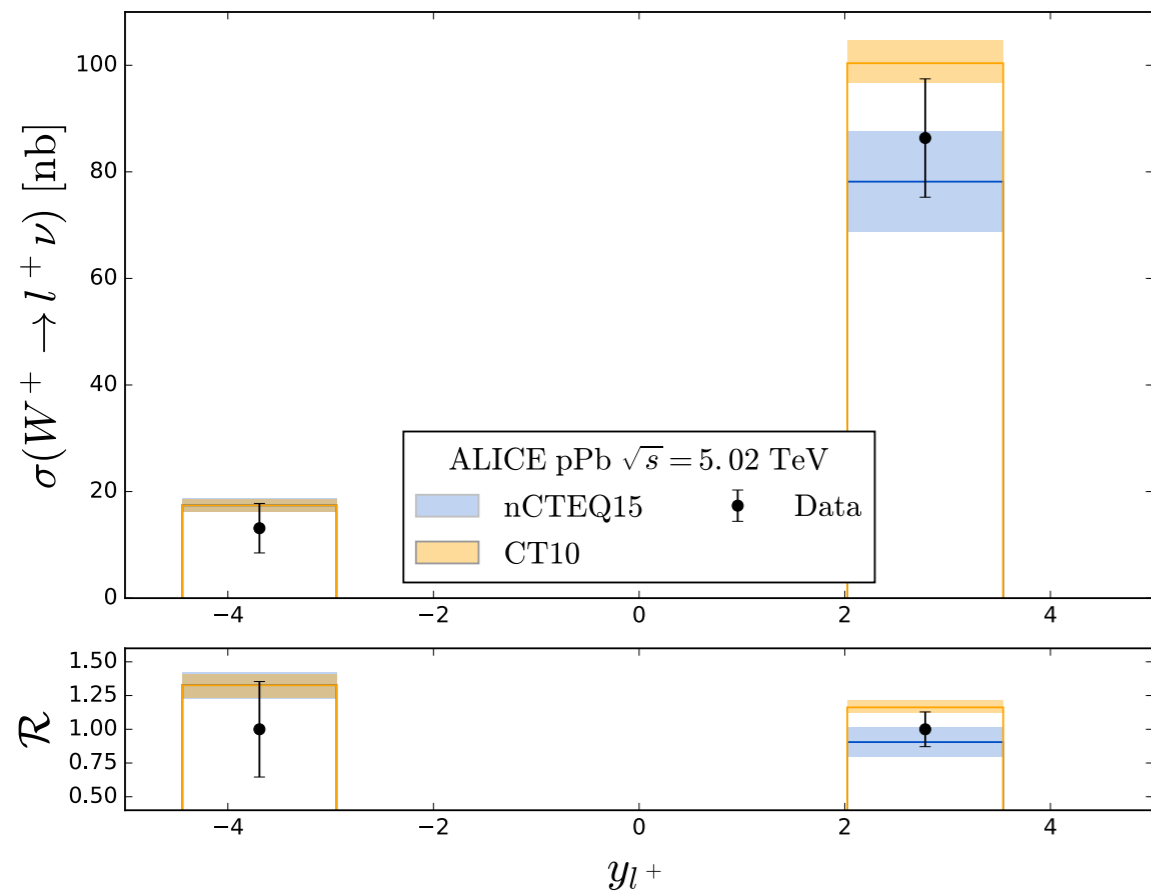
- $y < -1: x > 5 \times 10^{-2} \dots 0.3$ (region where nPDFs are constrained by data in global analysis)
- $|y| < 1: x \sim 10^{-2}$ (transition region from anti-shadowing to shadowing)
- $y > 1: x < 5 \times 10^{-3}$ (pure extrapolation!)

W-boson rapidity distributions

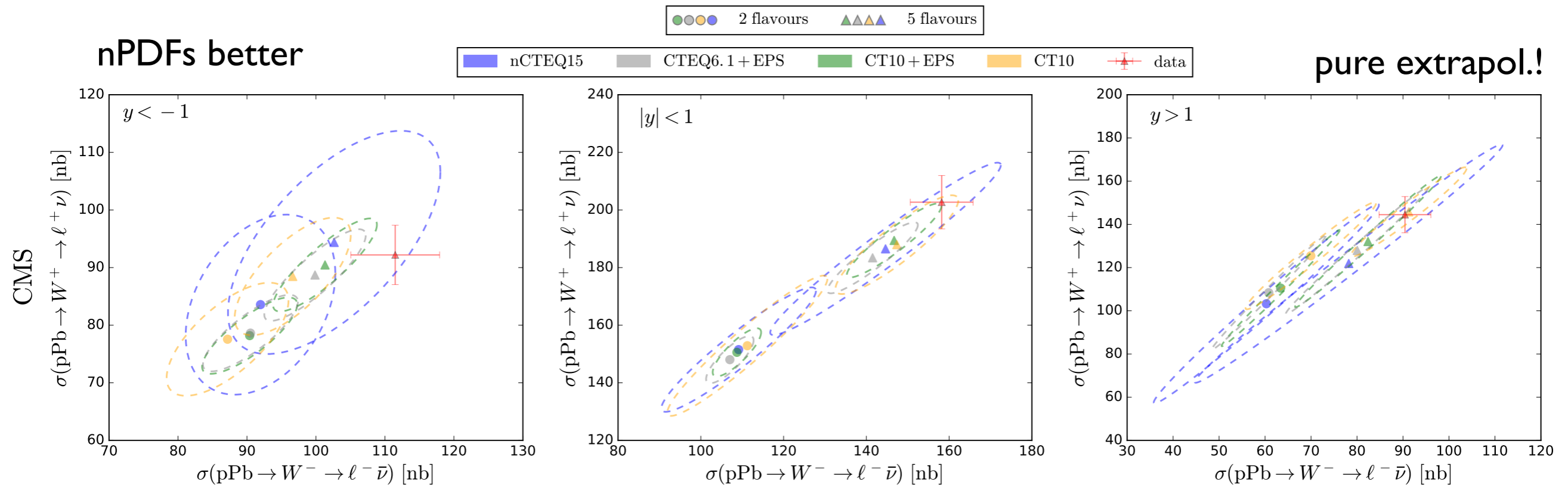


W-boson rapidity distributions

ALICE data:

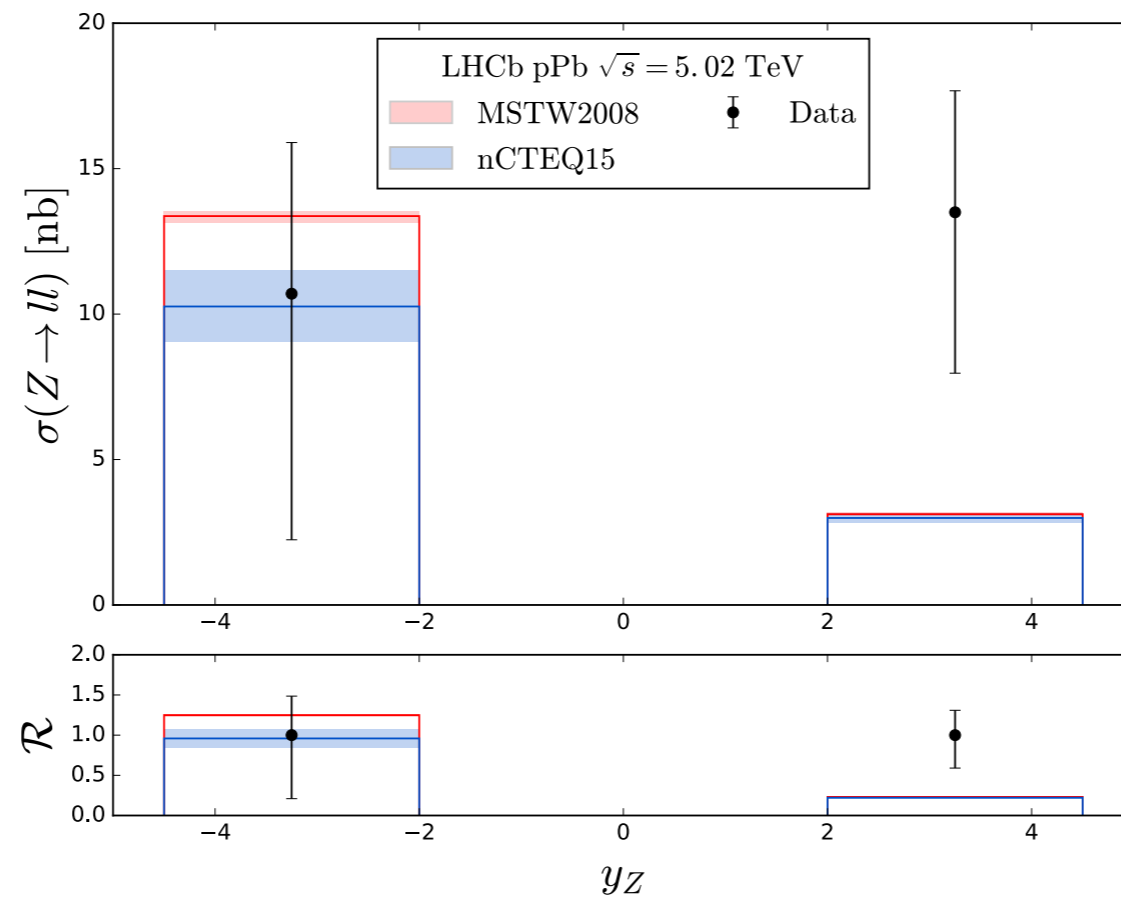
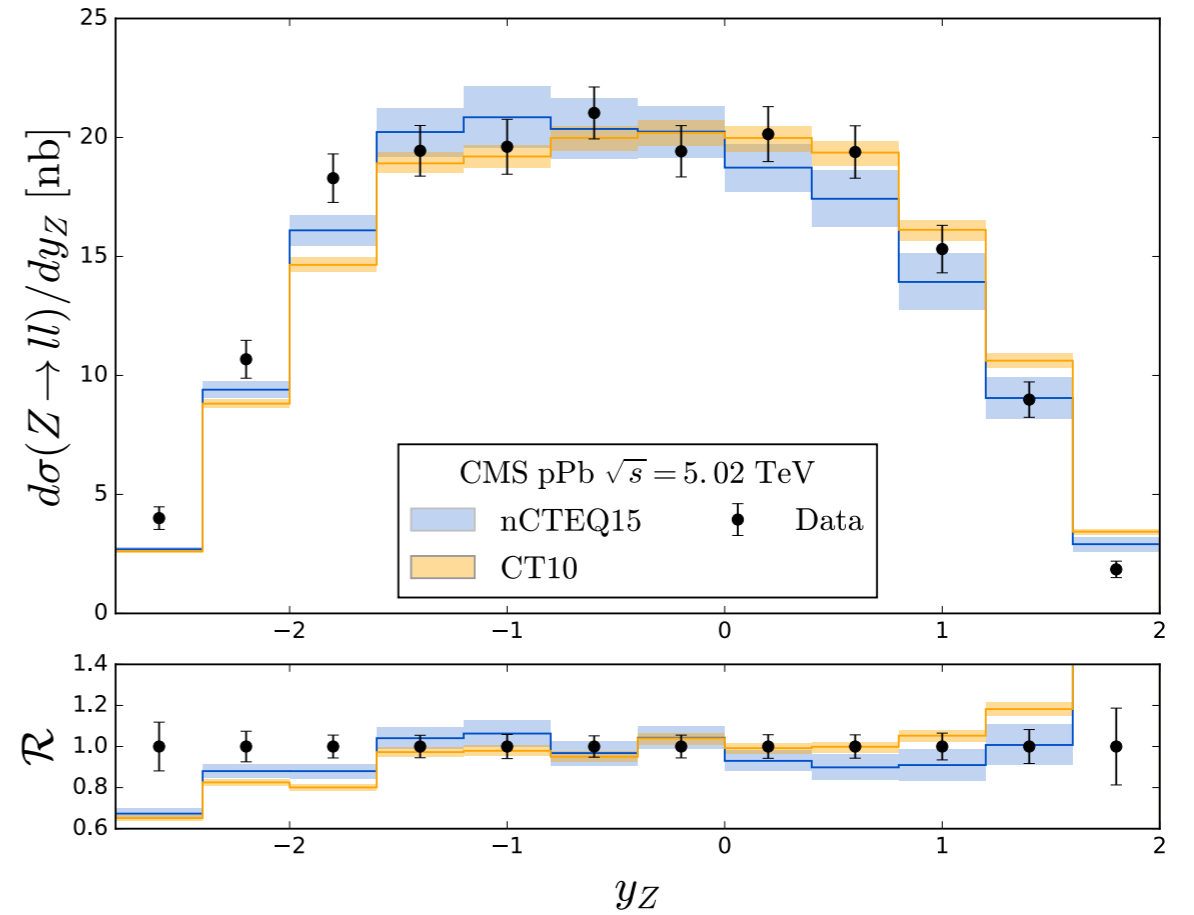
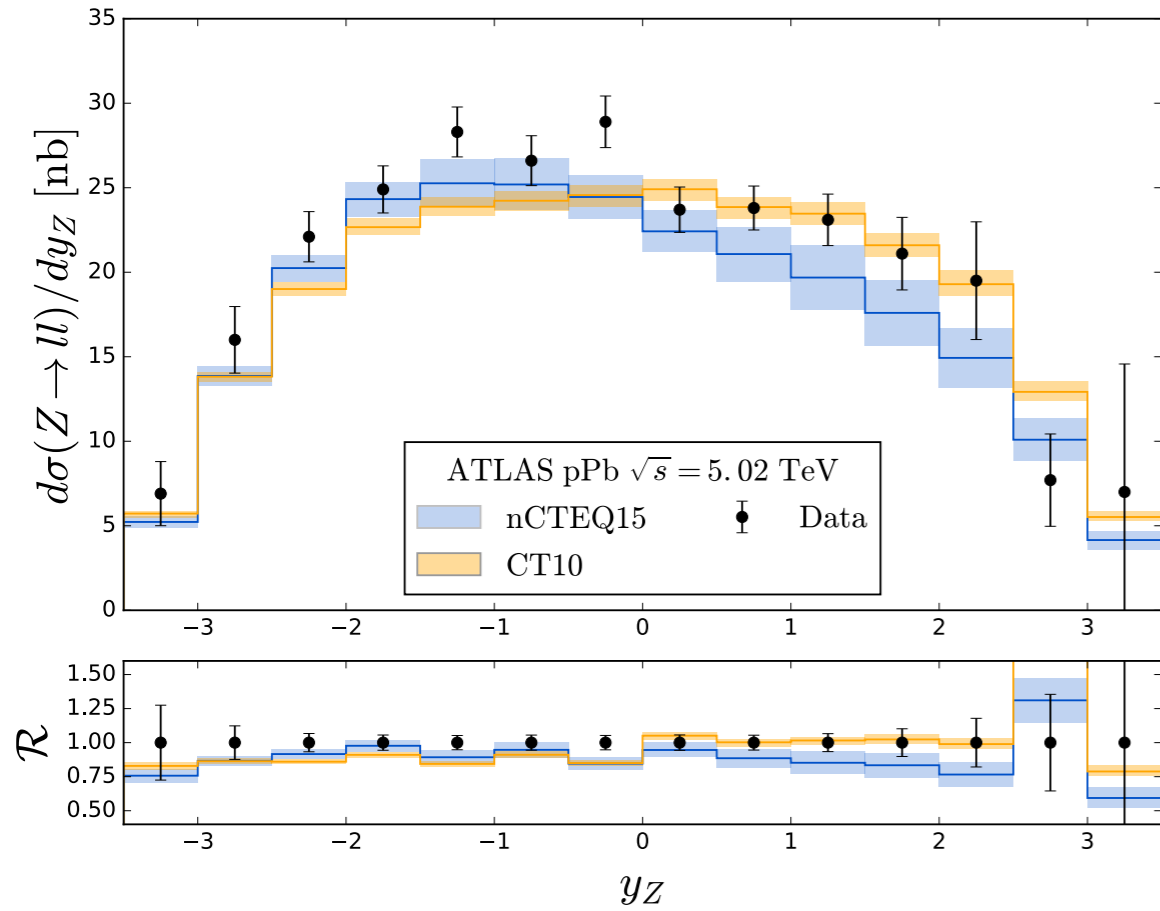


Importance of strange PDF



- $y < -1$ (large x): $s > \bar{s}$ could help!
- $|y| < 1$: delayed transition from anti-shadowing to shadowing could help **as seen in NuTeV neutrino data**
- $y > 1$: Extrapolation, **rather no shadowing at very small x ?**

Z-boson rapidity distributions



What about heavy quarks?

- Charmonium production

- Probes **gluon at small-x**
- Theory under control?

- Inclusive D-meson production

- Very sensitive to **gluon at small-x!**
see PROSA study (for the gluon in the proton): EPJC75(2015)396, arXiv: 1503.04581
- at large p_T and forward rapidities: probe of IC

works in pp case!

- Inclusive photon+charm production

- probe of **intrinsic charm**

work by T. Stavreva et al.

Conclusions

- Much recent progress (EPPS'16, NCTEQ'15, W/Z analysis)
- nPDF uncertainties still substantial
(more realistic larger uncertainties now with EPPS'16)
- Need more precise LHC pA data from as many hard processes as possible! **Lead-only analysis possible!**
- Coloured and un-coloured final states to test shadowing vs energy loss effects
- Bright future: future fixed target experiments, EIC, LHeC, π -A data from COMPASS
- A lot of room for theoretical progress

Part II: D-meson production in the GM-VFNS

Factorization Formula:

[1]

$$d\sigma(p\bar{p} \rightarrow D^* X) = \sum_{i,j,k} \int dx_1 dx_2 dz f_i^p(x_1) f_j^{\bar{p}}(x_2) \times \\ d\hat{\sigma}(ij \rightarrow kX) D_k^{D^*}(z) + \mathcal{O}(\alpha_s^{n+1}, (\frac{\Lambda}{Q})^p)$$

Q : hard scale, $p = 1, 2$

-
- $d\hat{\sigma}(\mu_F, \mu'_F, \alpha_s(\mu_R), \frac{m_h}{p_T})$: hard scattering cross sections free of long-distance physics $\rightarrow m_h$ kept
 - PDFs $f_i^p(x_1, \mu_F), f_j^{\bar{p}}(x_2, \mu_F)$: $i, j = g, q, c$ [$q = u, d, s$]
 - FFs $D_k^{D^*}(z, \mu'_F)$: $k = g, q, c$

\Rightarrow need short distance coefficients including heavy quark masses

[1] J. Collins, 'Hard-scattering factorization with heavy quarks: A general treatment',
PRD58(1998)094002

List of subprocesses in the GM-VFNS

Only light lines

- ① $gg \rightarrow qX$
- ② $gg \rightarrow gX$
- ③ $qg \rightarrow gX$
- ④ $qg \rightarrow qX$
- ⑤ $q\bar{q} \rightarrow gX$
- ⑥ $q\bar{q} \rightarrow qX$
- ⑦ $qg \rightarrow \bar{q}X$
- ⑧ $qg \rightarrow \bar{q}'X$
- ⑨ $qg \rightarrow q'X$
- ⑩ $qq \rightarrow gX$
- ⑪ $qq \rightarrow qX$
- ⑫ $q\bar{q} \rightarrow q'X$
- ⑬ $q\bar{q}' \rightarrow gX$
- ⑭ $q\bar{q}' \rightarrow qX$
- ⑮ $qq' \rightarrow gX$
- ⑯ $qq' \rightarrow qX$

Heavy quark initiated ($m_Q = 0$)

- ① -
- ② -
- ③ $Qg \rightarrow gX$
- ④ $Qg \rightarrow QX$
- ⑤ $Q\bar{Q} \rightarrow gX$
- ⑥ $Q\bar{Q} \rightarrow QX$
- ⑦ $Qg \rightarrow \bar{Q}X$
- ⑧ $Qg \rightarrow \bar{q}X$
- ⑨ $Qg \rightarrow qX$
- ⑩ $QQ \rightarrow gX$
- ⑪ $QQ \rightarrow QX$
- ⑫ $Q\bar{Q} \rightarrow qX$
- ⑬ $Q\bar{q} \rightarrow gX, q\bar{Q} \rightarrow gX$
- ⑭ $Q\bar{q} \rightarrow QX, q\bar{Q} \rightarrow qX$
- ⑮ $Qq \rightarrow gX, qQ \rightarrow gX$
- ⑯ $Qq \rightarrow QX, qQ \rightarrow qX$

Mass effects: $m_Q \neq 0$

- ① $gg \rightarrow QX$
- ② -
- ③ -
- ④ -
- ⑤ -
- ⑥ -
- ⑦ -
- ⑧ $qg \rightarrow \bar{Q}X$
- ⑨ $qg \rightarrow QX$
- ⑩ -
- ⑪ -
- ⑫ $q\bar{q} \rightarrow QX$
- ⑬ -
- ⑭ -
- ⑮ -
- ⑯ -

⊕ charge conjugated processes

Limiting cases

- **GM-VFNS** → **ZM-VFNS** for $p_T \gg m$
(this is the case by construction)
- **GM-VFNS** → **FFNS** for $p_T \sim m$
(formally this can be shown; numerically problematic in the S-ACOT scheme)

Termes in the perturbation series

$$L = \ln(m/p_T)$$
$$a = \alpha_s/(2\pi)$$

Resummed



Fixed Order →

	LL	NLL	NNLL	...
LO	1			
NLO	aL	a		
NNLO	(aL) ²	a(aL)	a ²	
...

FFNS/Fixed Order NLO

Resummed



	LL	NLL	NNLL	...
LO $m \neq 0$	1			
NLO $m \neq 0$	aL	a		
NNLO	$(aL)^2$	$a(aL)$	a^2	
...

Fixed Order →

ZM-VFNS/Resummed NLO

Resummed



Fixed Order →

	LL $m=0$	NLL $m=0$	NNLL	...
LO	I			
NLO	aL	a		
NNLO	$(aL)^2$	$a(aL)$	a^2	
...

GM-VFNS/FONLL (NLO+NLL)

Resummed



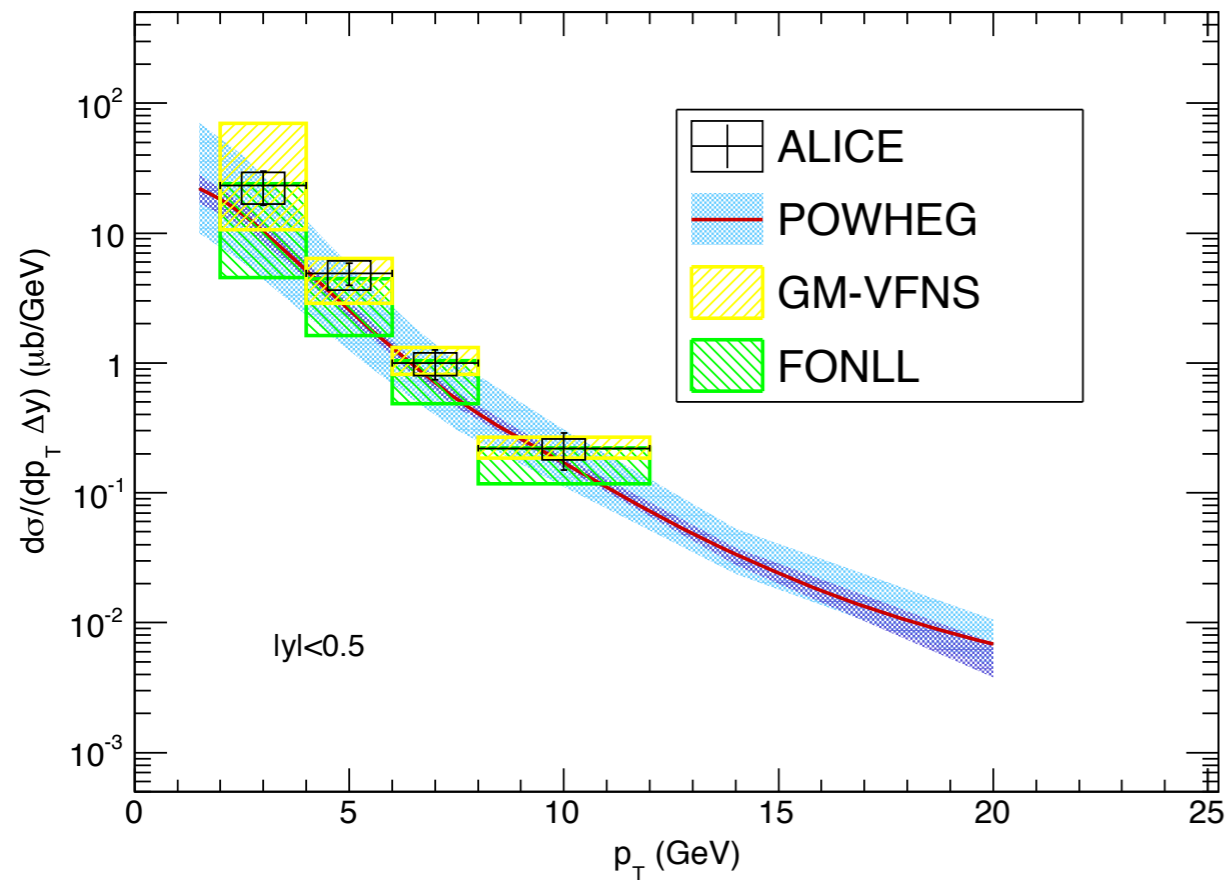
Fixed Order →

	LL	NLL	NNLL	...
LO	$1_{m \neq 0}$			
NLO	$aL_{m \neq 0}$	$a_{m \neq 0}$		
NNLO	$(aL)_{m=0}^2$	$a(aL)_{m=0}$	a^2	
...	$\dots_{m=0}$	$\dots_{m=0}$	\dots	\dots

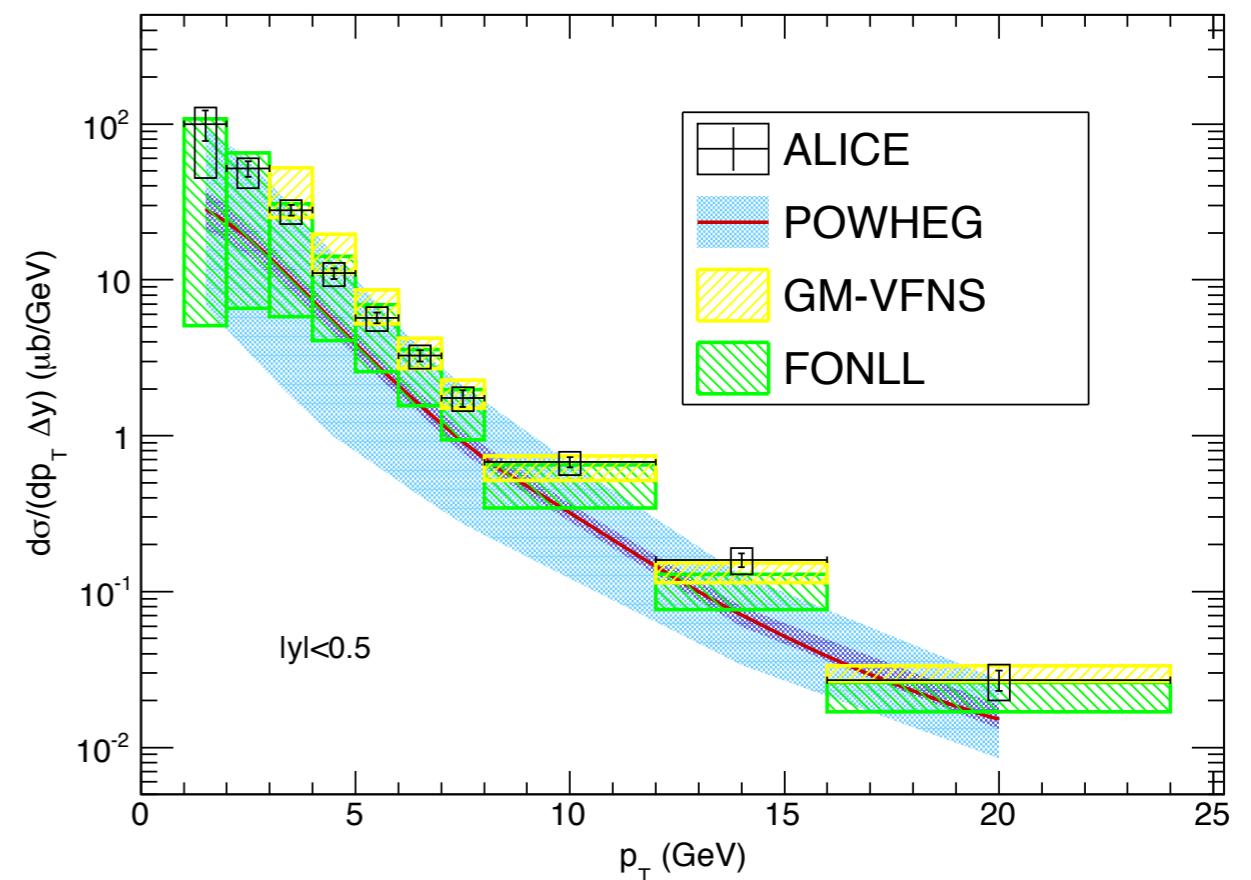
Comparison with ALICE data

arXiv:1405.3083

$pp \rightarrow D^{*+}+X$ at $\sqrt{s} = 2.76$ TeV



$pp \rightarrow D^{*+}+X$ at $\sqrt{s} = 7$ TeV



Central scale choice: $\mu_R = \mu_F = \mu_{F'} = m_T$

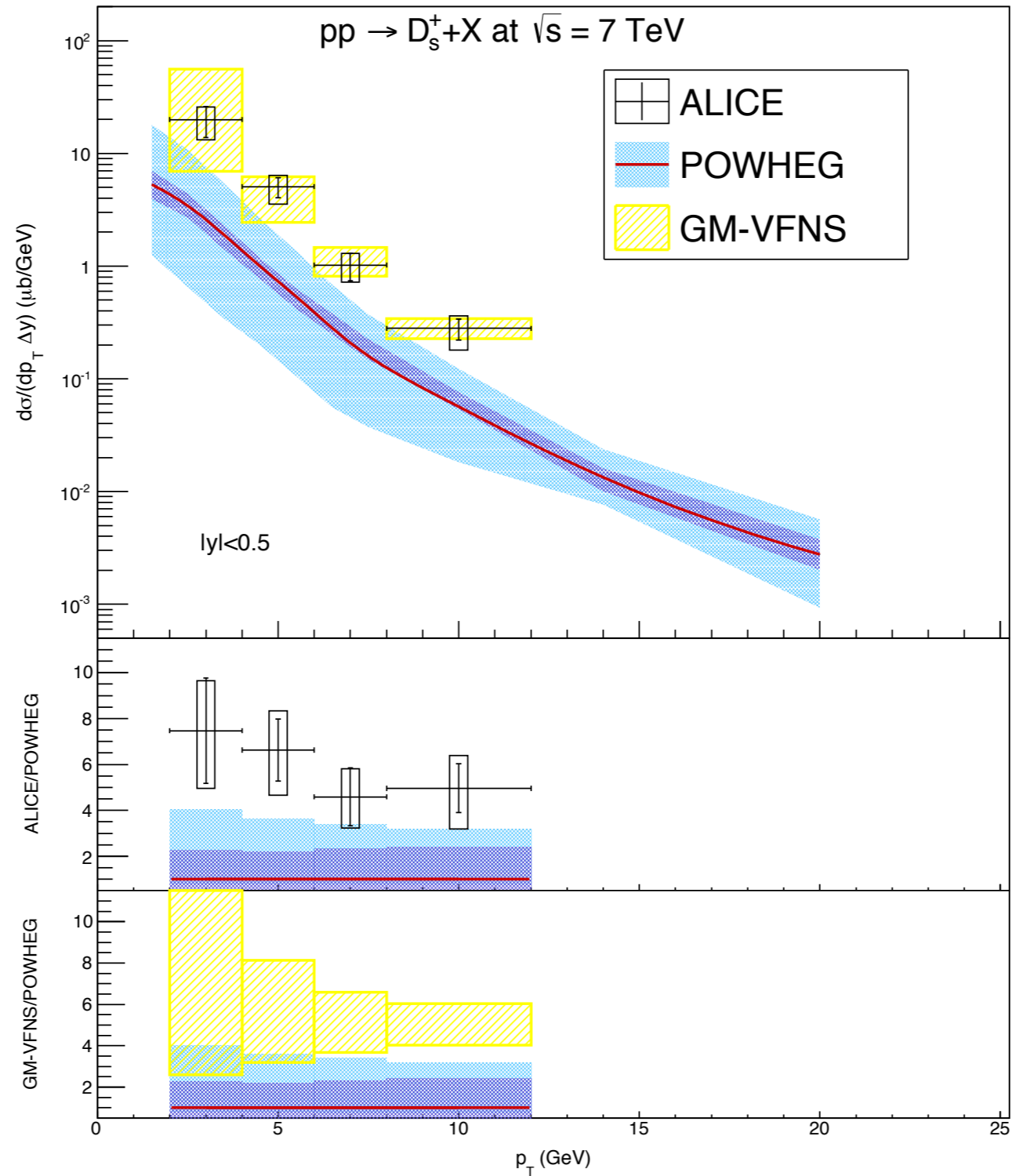
Uncertainty band: varying the scales by a factor 2 up/down

CT10 PDFs, KKKS FFs, $m_c = 1.5$ GeV

Comparison with ALICE data

D_s FFs from Kniehl, Kramer'06

arXiv:1405.3083

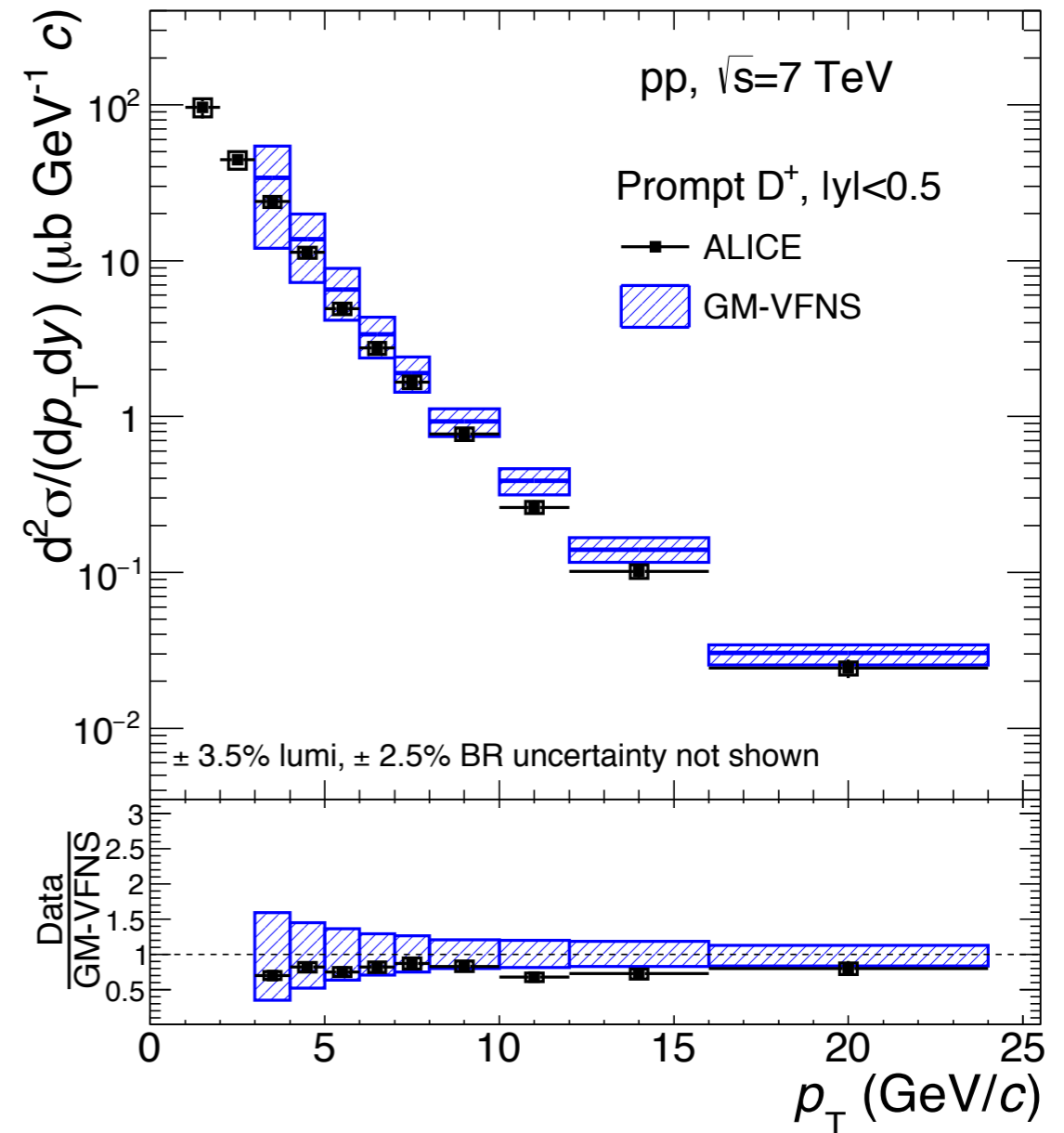
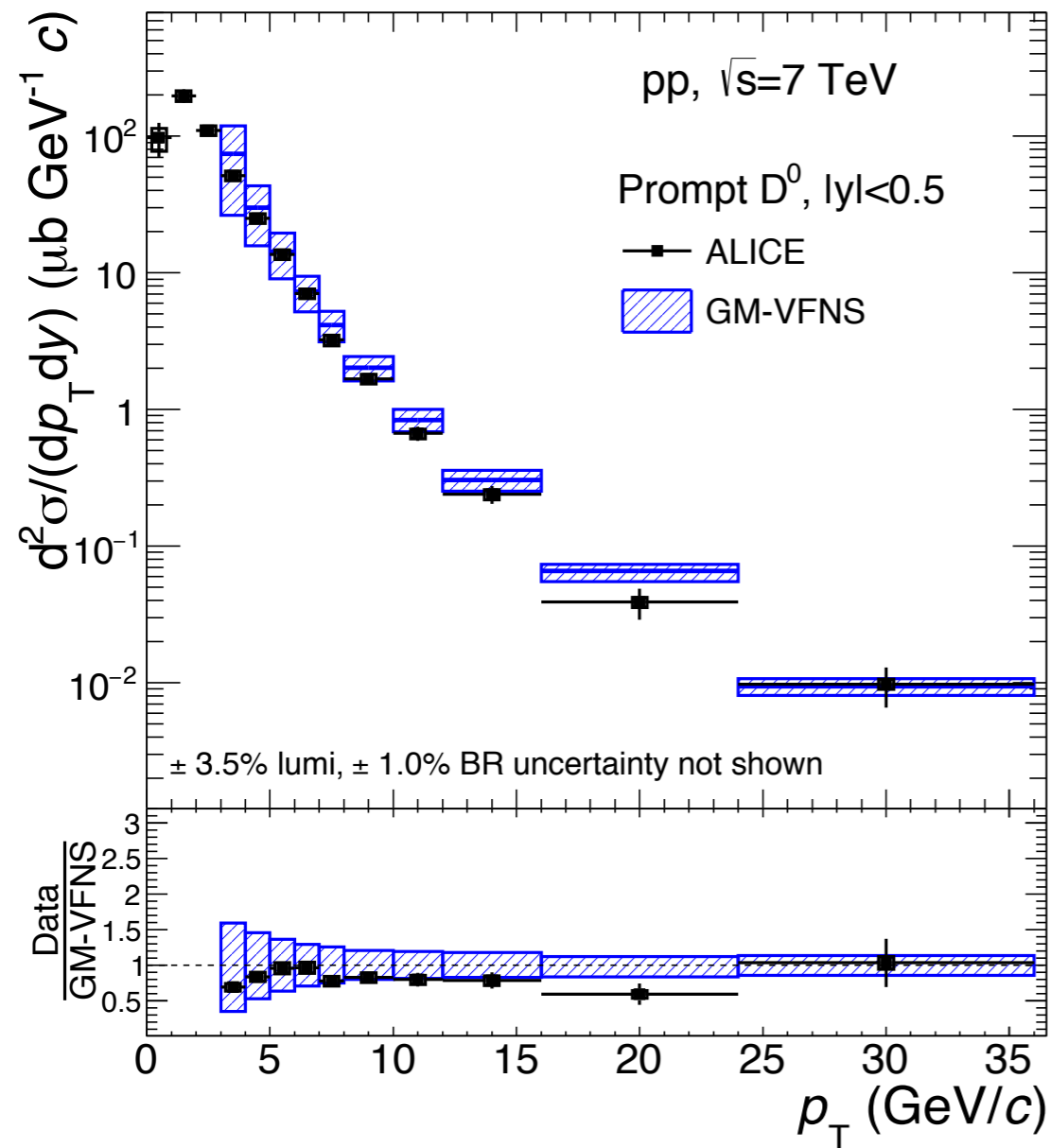


Recent numerical results

- a (D^*, D^0, D^+, D_s) in pp@7 TeV, $|y| < 0.5$, $p_T =$
- Ratio of D^0/D^+ (etc) predicted to be flat at $p_T > 2$ m
- Λ_c in pp@5 TeV
- Results for p-Pb in progress
- $d\sigma/dp_T$ sensitive to small-x nuclear gluon but large scale uncertainty
- R_{pA} will be sensitive to small-x nuclear gluon PDF with reduced scale uncertainty; careful study required

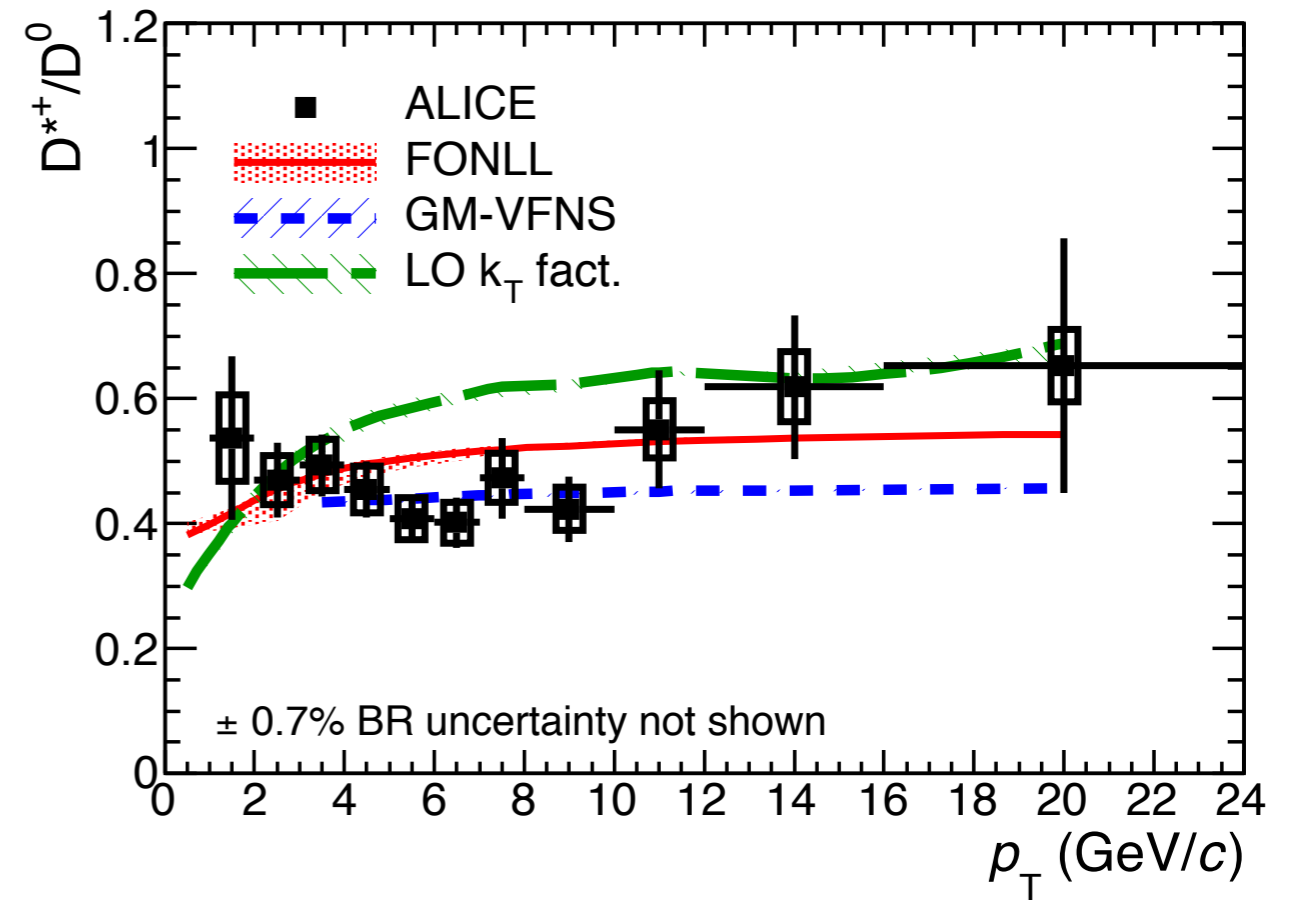
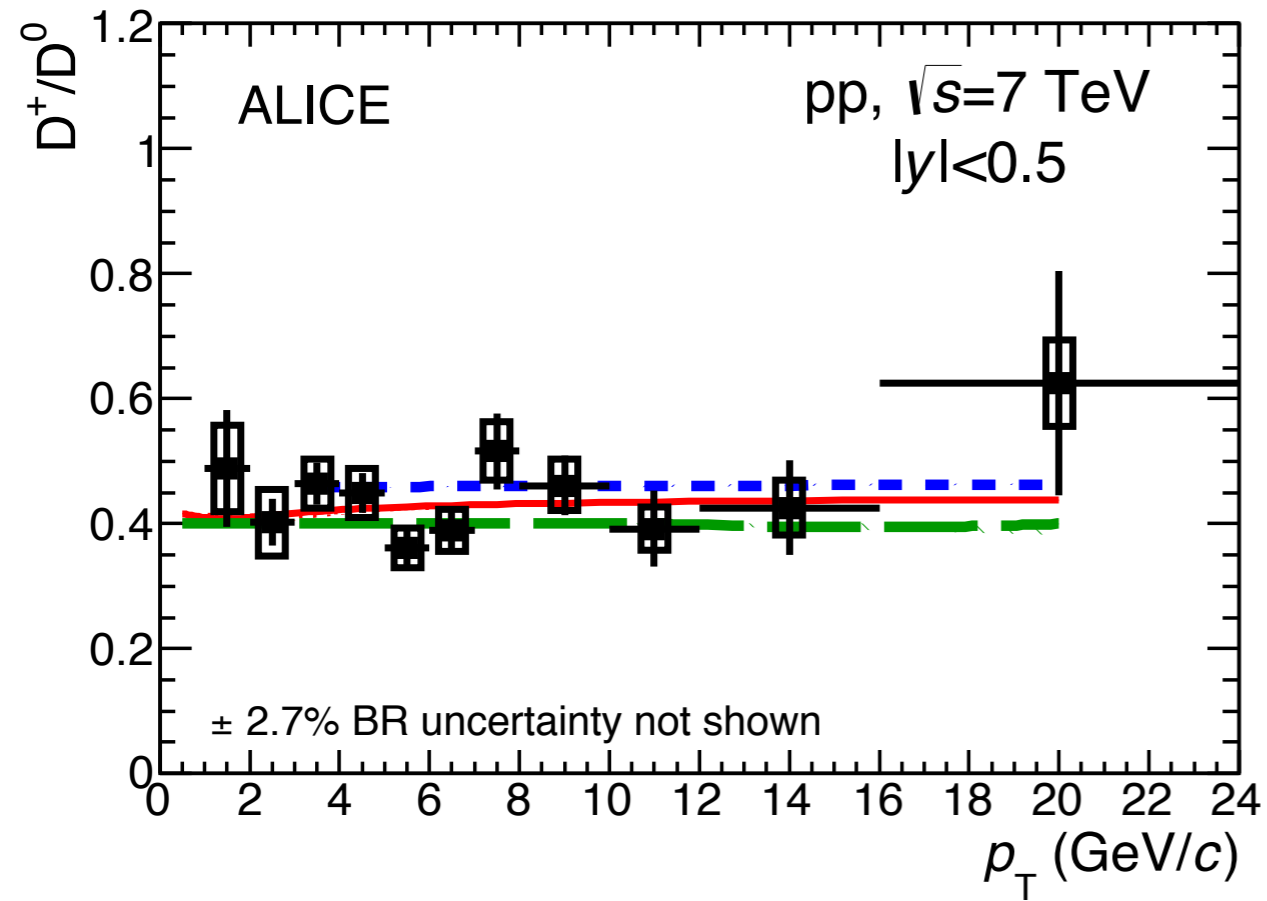
Comparison with most recent ALICE data

arXiv:1702.00766



Comparison with most recent ALICE data

arXiv:1702.00766

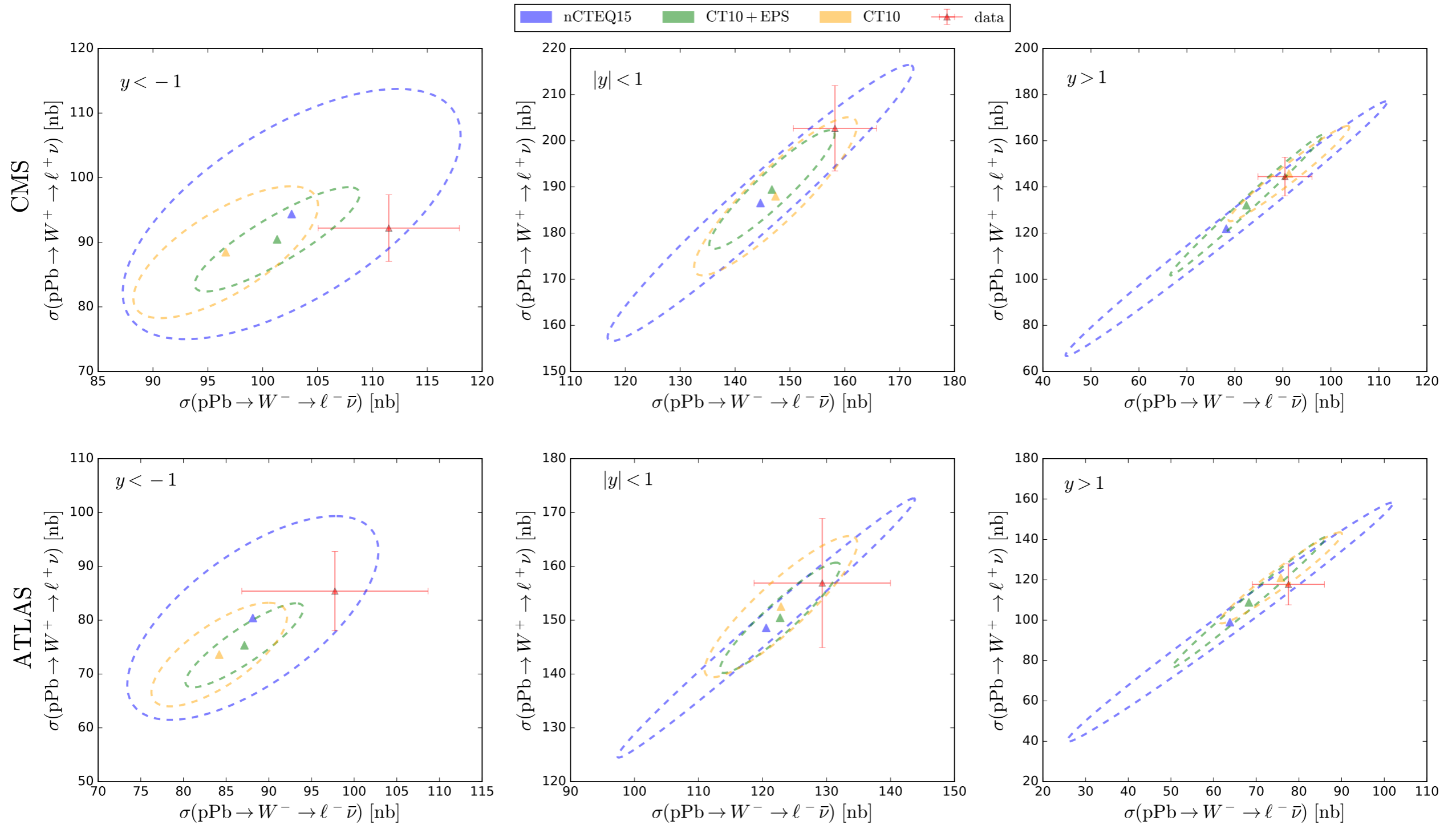


Conclusion

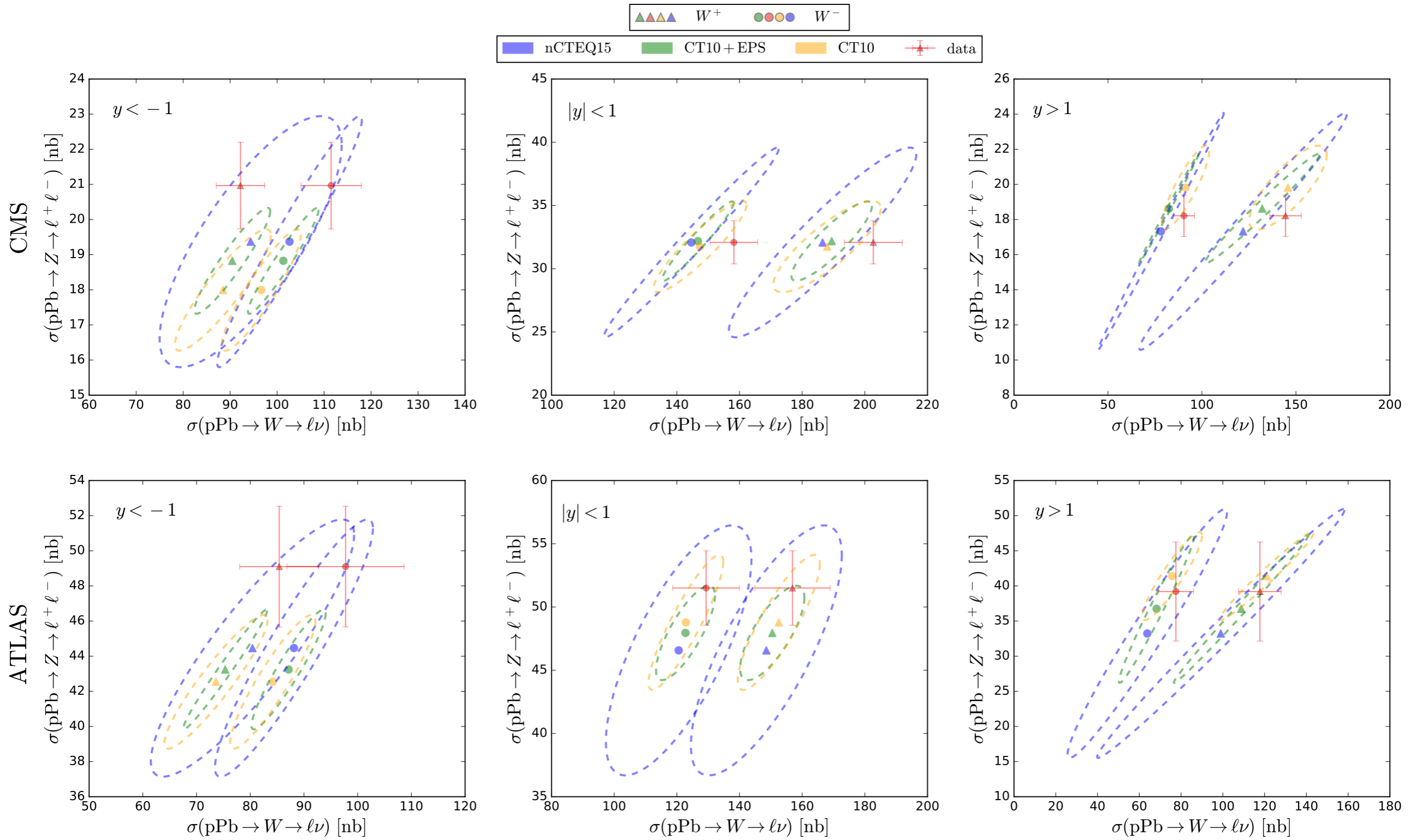
- GM-VFNS in good agreement with ALICE data for inclusive D meson production
- Large scale uncertainties!
To make progress need NNLO
- p-Pb heavy quark data (D,B) interesting to constrain the small-x nuclear gluon distribution
- More results to come. Stay tuned.

Backup

(W^+, W^-) Correlation



(Z,W) Correlation



FONLL=FO+NLL [1]

$$\text{FONLL} = \text{FO} + (\text{RS} - \text{FOM0})G(m, p_T)$$

FO: Fixed Order; FOM0: Massless limit of FO; RS: Resummed

$$G(m, p_T) = \frac{p_T^2}{p_T^2 + 25m^2} \simeq \begin{cases} 0.04 & : p_T = m \\ 0.25 & : p_T = 3m \\ 0.50 & : p_T = 5m \\ 0.66 & : p_T = 7m \\ 0.80 & : p_T = 10m \end{cases}$$

$$\Rightarrow \text{FONLL} = \begin{cases} \text{FO} & : p_T \lesssim 3m \\ \text{RS} & : p_T \gtrsim 10m \end{cases}$$

[1] Cacciari, Greco, Nason, JHEP05(1998)007

FONLL

- FFs in N-space in the PFF approach

- RS-FOM0 gets very large at small p_T :

$$G(m, p_T) = p_T^2 / (p_T^2 + a^2 m^2) \text{ with } \mathbf{a=5}$$

needed to suppress this contribution sufficiently rapidly

- Central scale choice for FO, RS, FOM0: m_T
- Error bands: $\mu_F = \mu_F'$ (only two scales varied)
- Predictions for LHC7 in [arXiv:1205.6344](#)