



Summary of the Heavy Flavours Working Group

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HF WG: Theory Talks

- **DIS** structure functions: Blümlein, Olness, Moch
- **Open c, b:**
 - Inclusive D and B mesons: Spiesberger
 - Jet production in the ACOT scheme: Kotko
 - Photon+Q: Kovarik
 - kT factorization + double parton scattering: Szczurek
- **Charmonium** production and polarization in NRQCD: Kniehl
- **Top:** Yang, Mitov, Bierrenbaum, Kidonakis, Moch, Kardos

DIS structure functions at $O(\alpha_s^3)$

DIS structure functions F_2^c, F_L^c

Charm contribution to the inclusive structure functions in fixed order:

Heavy quark Wilson coefficient
known to $O(\alpha_s^2)$
[Laenen, Riemersma, Smith, Neerven '93] PDFs

$$F^c(x, Q^2) = H_j(x, \frac{Q^2}{\mu^2}, \frac{m^2}{\mu^2}) \otimes f_j(x, \mu^2)$$

Mass factorization for $Q^2 \gg m^2$:

$$H_j = C_i(x, \frac{Q^2}{\mu^2}) \otimes A_{ij}(x, \frac{m^2}{\mu^2})$$

light flavor Wilson coefficients;
known to $O(\alpha_s^3)$
[Moch, Vermaseren, Vogt, NPB96]

OME's;
Known to $O(\alpha_s^2)$ [BMNS, NPB96]
Needed at $O(\alpha_s^3)$

Recent results on Three Loop Corrections to F_2^c, F_L^c

Mellin N space:
$$H_j = C_i(N, \frac{Q^2}{\mu^2}) A_{ij}(\frac{m^2}{\mu^2}, N) \quad (\text{for } Q^2 \gg m^2)$$

Partial results for $A_{ij} \mathcal{O}(\alpha_s^3)$

Variable Flavor Number Scheme

Main application: **Matching conditions** for the VFNS
needed in global analyses of PDFs

$$f_i^{(n_f+1)}(x, \mu^2) = A_{ij}(x, \frac{m^2}{\mu^2}) \otimes f_j^{(n_f)}(x, \mu^2)$$

Status of OME calculations

Leading Order: [Witten, 1976 Nucl.Phys.B; Babcock, Sivers, 1978 Phys.Rev.D; Shifman, Vainshtein, Zakharov, 1978 Nucl.Phys.B; Leveille, Weiler, 1979 Nucl.Phys.B; Glück, Reya, 1979 Phys.Lett.B; Glück, Hoffmann, Reya, 1982 Z.Phys.C.]

Next-to-Leading Order : [Laenen, van Neerven, Riemersma, Smith, 1993 Nucl. Phys. B]

[Large Q^2/m^2 : Buza, Matiounine, Smith, Migneron, van Neerven, 1996 Nucl.Phys.B] IBP

[Bierenbaum, Blümlein, Klein, 2007 Nucl.Phys.B] via ${}_pF_q$'s, more compact results

[Bierenbaum, Blümlein, Klein 2008 Nucl.Phys.B, 2009 Phys.Lett.B]: $O(\alpha_s^2 \varepsilon)$ contributions (all N)

NNLO: [Bierenbaum, Blümlein, Klein 2009 Nucl.Phys.B] Moments for F_2 : $N = 2 \dots 10(14)$

[Blümlein, Klein, Tödtli 2009 Phys. Rev. D] contrib. to transversity: $N = 1 \dots 13$

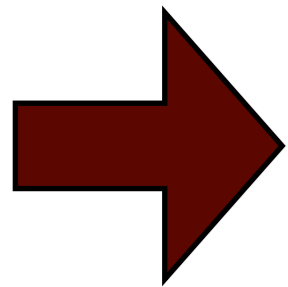
[Ablinger, Blümlein, Klein, Schneider, Wißbrock 2011 Nucl.Phys.B] contrib. $\propto n_f$ to F_2 (all N):

At 3-loop order known:

- $A_{qq,Q}^{\text{PS}}, A_{qg,Q}$: complete
- $A_{Qg}, A_{Qq}^{\text{PS}}, A_{qq,Q}^{\text{NS}}, A_{qq,Q}^{\text{NS,TR}}$: all terms of $O(n_f T_F^2 C_{A/F})$
- $A_{Qq}^{\text{PS}}, A_{qq,Q}^{\text{NS}}, A_{qq,Q}^{\text{NS,TR}}$: all terms of $O(T_F^2 C_{A/F})$
- $A_{gq,Q}, A_{gg,Q}$: see [this talk](#) \longrightarrow all terms of $O(n_f T_F^2 C_{A/F})$

Plan

- Talk based on results on ...



- ... improved heavy-quark coefficient functions at NNLO
H. Kawamura , S.M., A. I. Presti and A. Vogt to appear
- ... a determination of the running charm-quark mass
S. Alekhin , K. Daum , K. Lipka and S.M. to appear
- ... a spin-off on top-quark hadro-production
S.M., P. Uwer and A. Vogt to appear

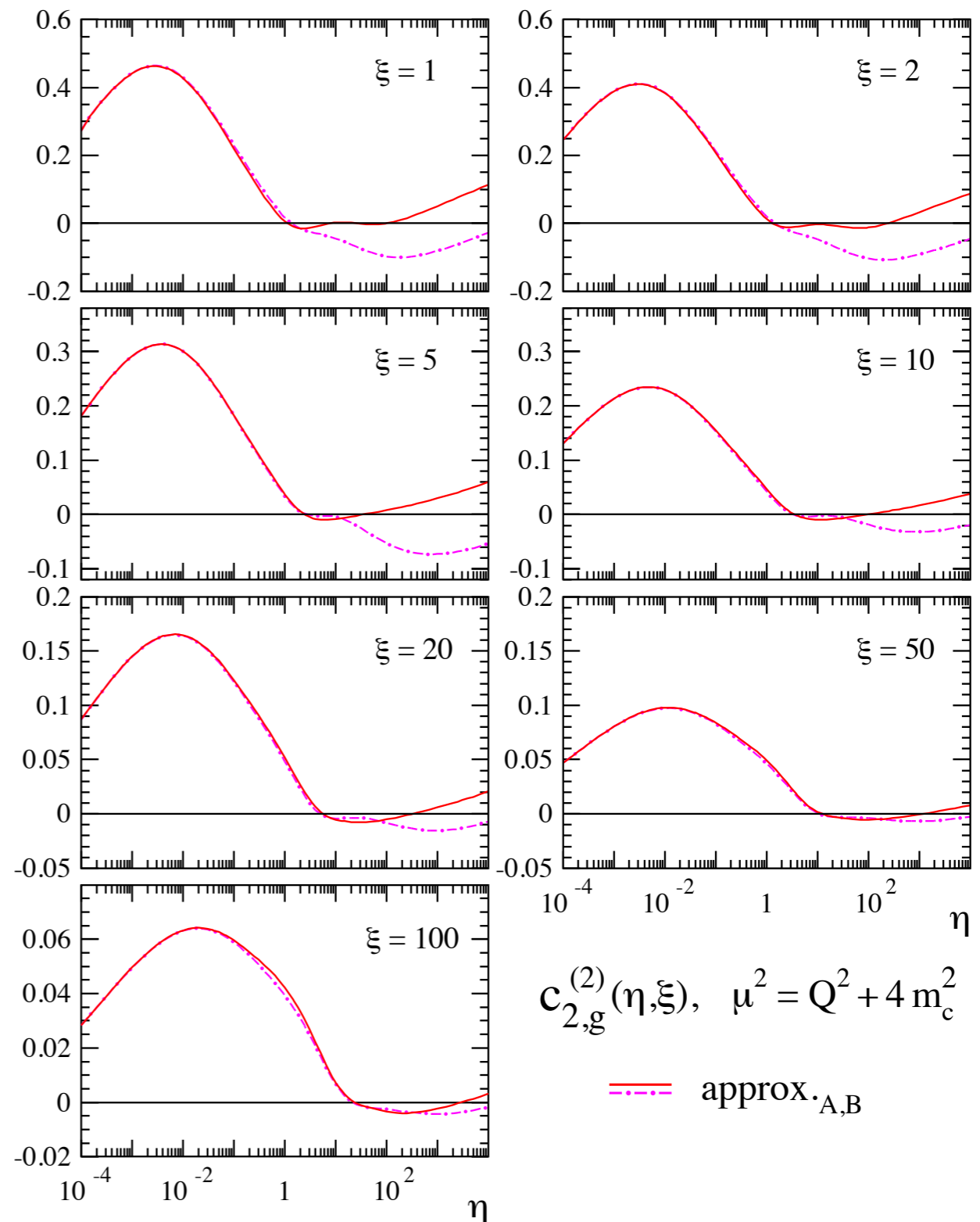
Construct approximate H_i at $O(\alpha_s^3)$

- H_i known at $O(\alpha_s^2)$
- Threshold region dominated by Sudakov log's $\ln(\beta)$ where $\beta=(1-4 m^2/s)^{1/2}$ close to threshold $\beta=0$
- Sudakov log's can be resummed. Predicts fixed orders in perturbation theory
- Asymptotic region $Q^2 \gg m^2$ (see talk by Blümlein)
complete functional dependence now known to $O(\alpha_s^3)$
[Presti,Kawamura,Moch,Vogt]
- High energy limit: k_T -factorization at small x
Information on leading and next-to-leading small- x log's
- **Combine all limits. Construct approximate result for full kinematic range**

Approximate coefficient functions at NNLO

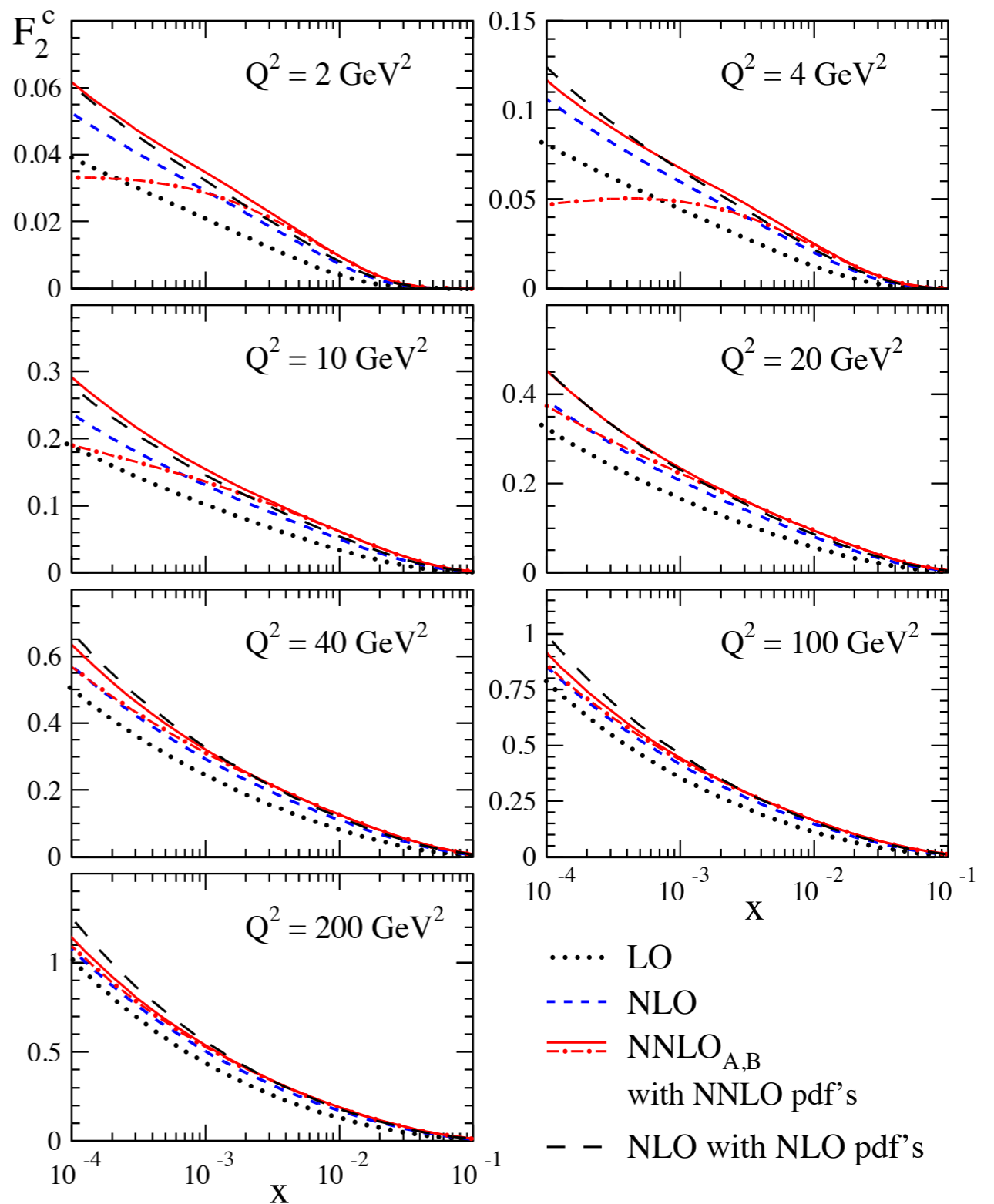
$$\eta = s/(4m^2) - 1, \quad \xi = Q^2/m^2$$

- New approximate NNLO result
 - very well constrained at large ξ
 - sizable uncertainties for $\xi \lesssim 10$
- Realistic estimate of uncertainty through combination of all limits
- Progress would require
 - more Mellin moments for A_{ji}
 - computation of $c_{2,k}^{\text{NLL}_x}$ (NLO impact factor for k_t -factorization)



Approximate charm structure functions at NNLO

- New approximate NNLO result
 - convolution with ABM11 PDF set
- Uncertainty on NNLO dominates kinematic region in Q^2 relevant for HERA
 - very well constrained at large Q^2
 - sizable uncertainties for $Q^2 \lesssim 20 \text{ GeV}^2$ (even at not so small x)
 - gluon PDF does not fall fast enough as η grows larger



Fixed Flavour and Variable Flavour Number Schemes

- Heavy Quark coefficient functions H_i not IR-safe:

$$H_i \rightarrow \infty \quad \text{for} \quad \frac{Q^2}{m^2} \rightarrow \infty$$

- VFNS:
Subtract large log's from H_i and resum via evolved heavy quark PDF; used in global analyses of PDFs
- Keep finite mass terms m^2/Q^2 in subtracted Wilson coefficients \hat{H}_i

Heavy Quark Production in the ACOT scheme at NNLO and N³LO

- \hat{H}_i in the ACOT scheme known to $O(\alpha_s)$;
Need $O(\alpha_s^2)$ for PDF analyses at NNLO
- Idea: Combine **exact ACOT scheme at $O(\alpha_s)$**
with known massless Wilson coefficients C_i at $O(\alpha_s^2)$ and $O(\alpha_s^3)$
- Observation with exact ACOT at $O(\alpha_s)$:
mass effect due to χ -scaling more important than
powerlike mass terms m^2/Q^2 in the subtracted
massive Wilson coefficients
- Approximation for $O(\alpha_s^2)$ and $O(\alpha_s^3)$ terms:
Use C_i combined with χ -scaling prescription

$$\chi = x \left(1 + \frac{(nm)^2}{Q^2} \right)$$

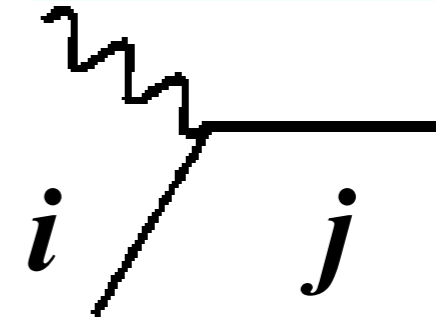
Master formula for decomposing the flavor components

T.P. Stavreva, I Schienbein

$$F = \sum_{i,j}^6 F^{ij}$$

needed to extract F^c

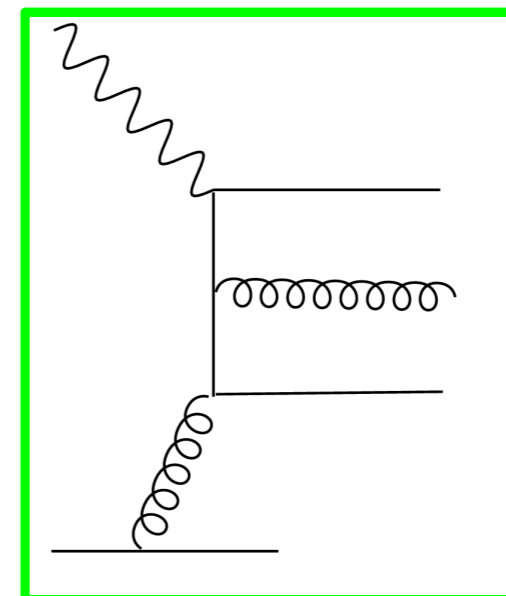
**The Goal: Convert from
{s, ns, ps} to {q,g, ...}**

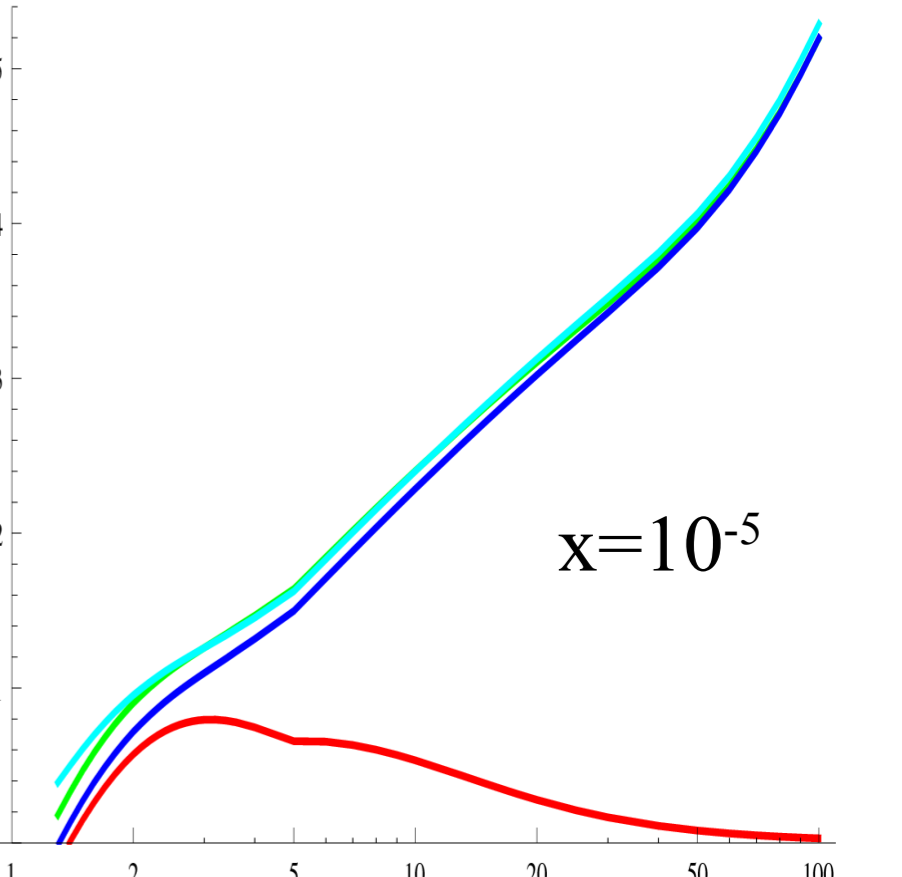
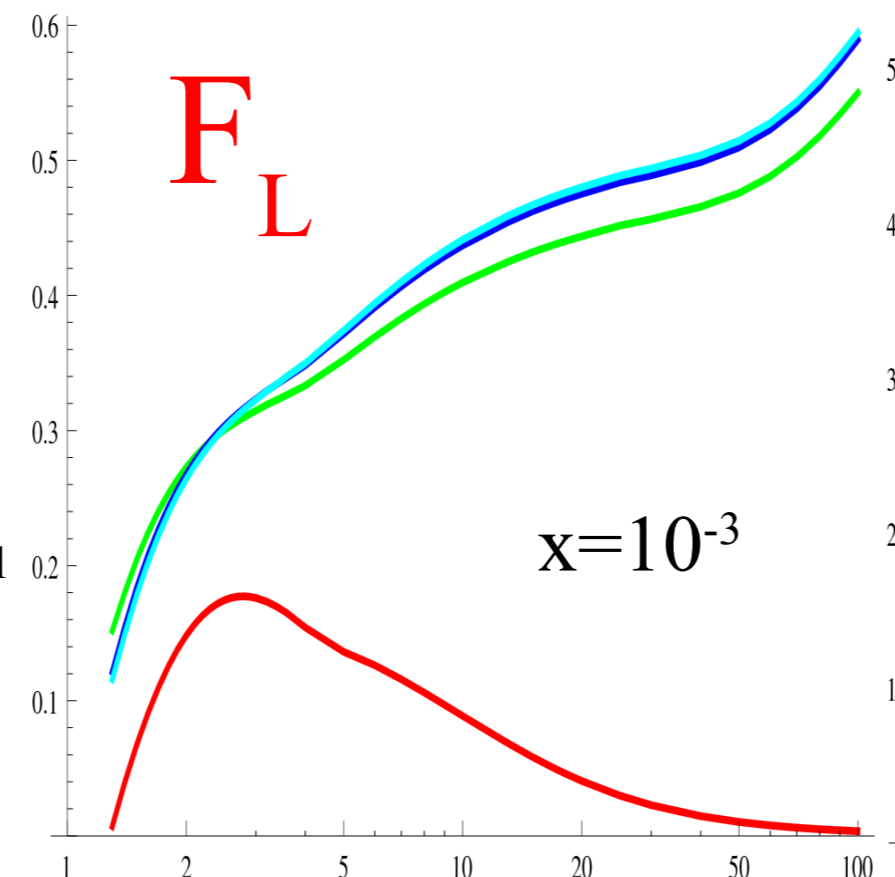
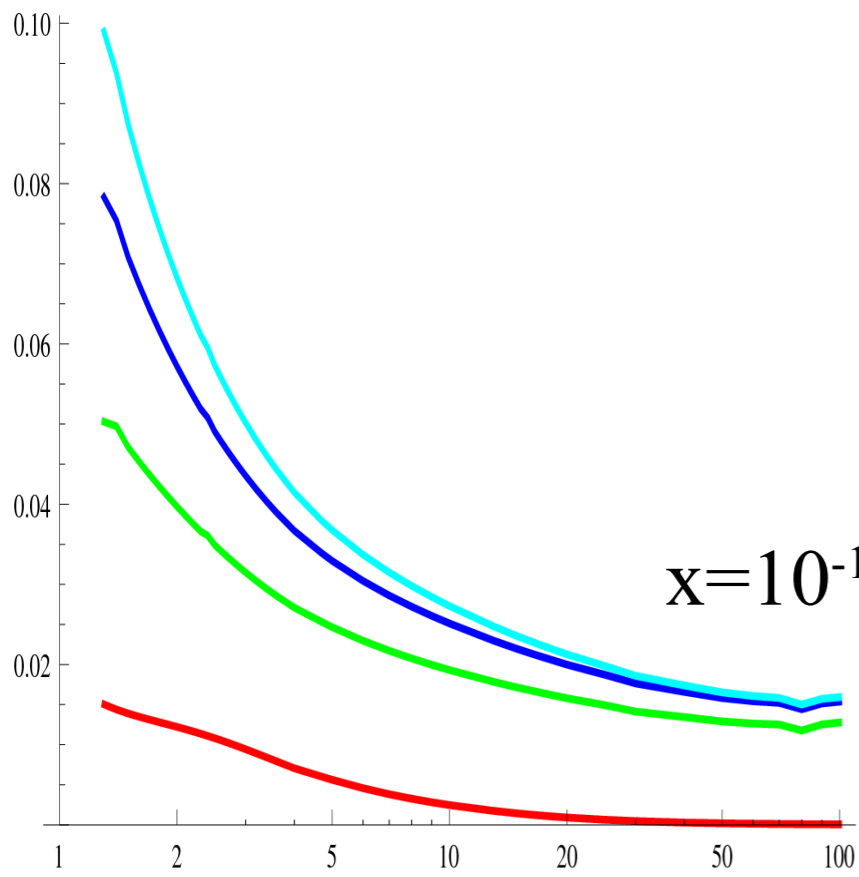
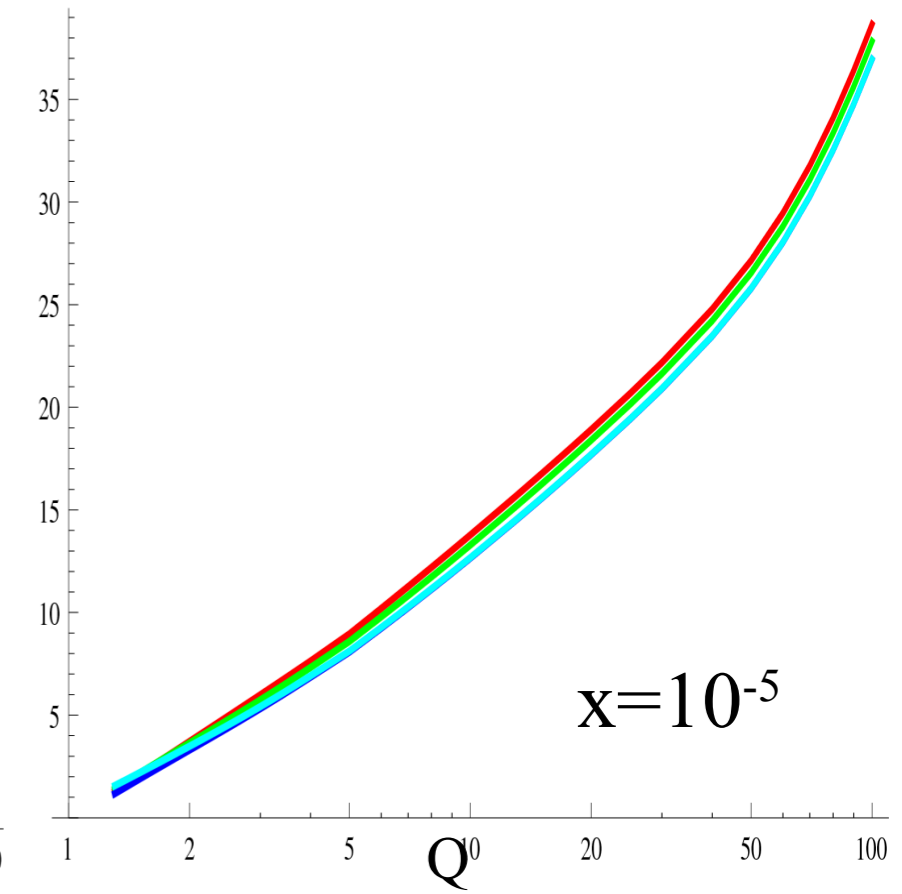
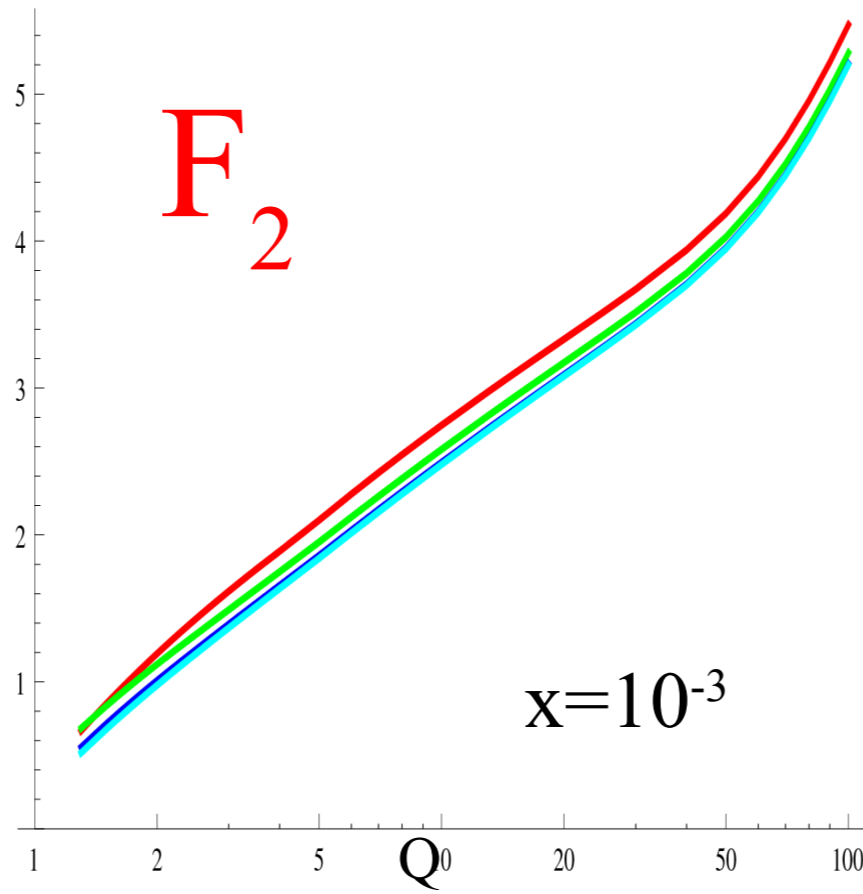
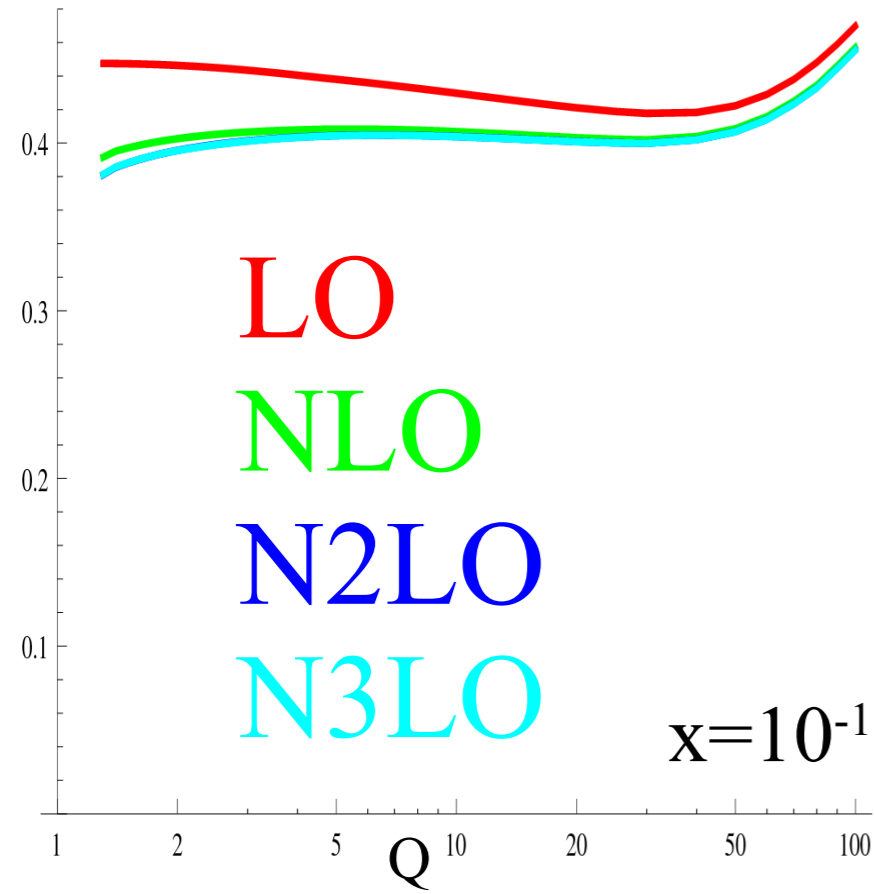


$$x^{-1} F_a^{ij} = q_i^+ \otimes \left\{ e_i^2 \left[C_{a,q}^{\text{ns}}(n_f = 0) \delta_{ij} + C_{a,q}^{\text{ns}}(j) - C_{a,q}^{\text{ns}}(j-1) \right] - \langle e^2 \rangle^{(j)} C_{a,q}^{\text{ps}}(j) - \langle e^2 \rangle^{(j-1)} C_{a,q}^{\text{ps}}(j-1) \right\}$$

Issues: Flavor separation:
New diagrams at this order

- c,b, goes down beam pipe
- both c & b in final state





Open charm and bottom

Less inclusive heavy quark production

- More observables, more tests of pQCD, experimentally more direct (less extrapolation)
- Heavy flavour schemes
 - Mainly for inclusive DIS; used in global analyses of PDFs
 - Schemes have to be applicable to less inclusive cases! [Spiesberger, Kotko](#) (otherwise not a general pQCD formalism)
- Exclusive processes useful to probe heavy flavour PDFs. [Spiesberger, Kovarik](#)

Most global analyses generate charm/bottom PDFs perturbatively. Should be tested! Important for various SM and BSM processes! (t-channel single top, top+charged Higgs, ..., whenever new physics couples to the SM fermions via the fermion mass)

- Theoretical framework:

the **G**eneral-**M**ass **V**ariable-**F**lavor-**N**umber **S**cheme for
1-particle inclusive heavy-meson production
measure p_T and η of observed heavy meson

GM-VFNS \approx ACOT

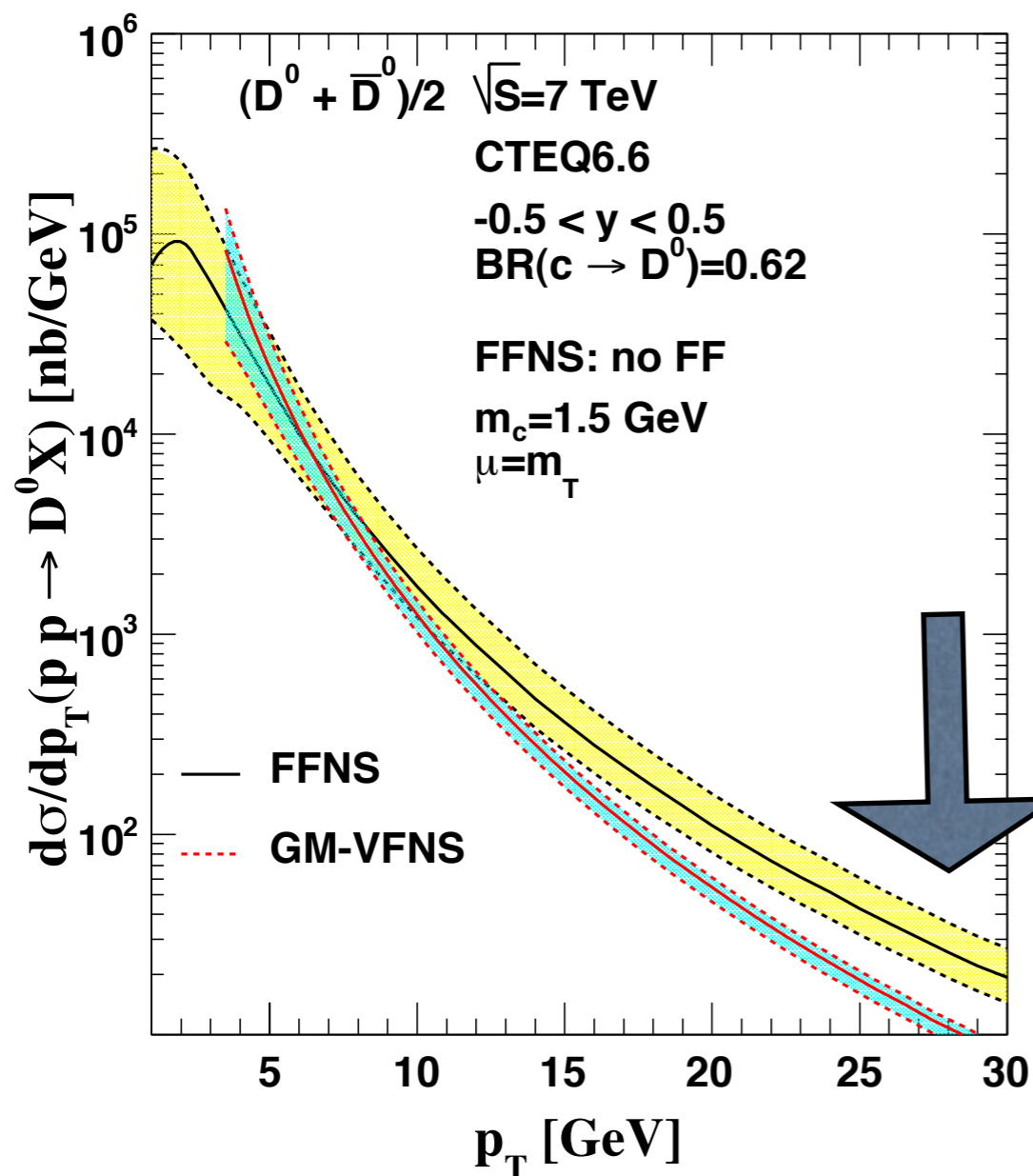
- Numerical results for D - and B -meson production:

$$p + p \rightarrow D + X, \quad (D = D^\pm, D^0, D^{*\pm}, D_s^\pm),$$

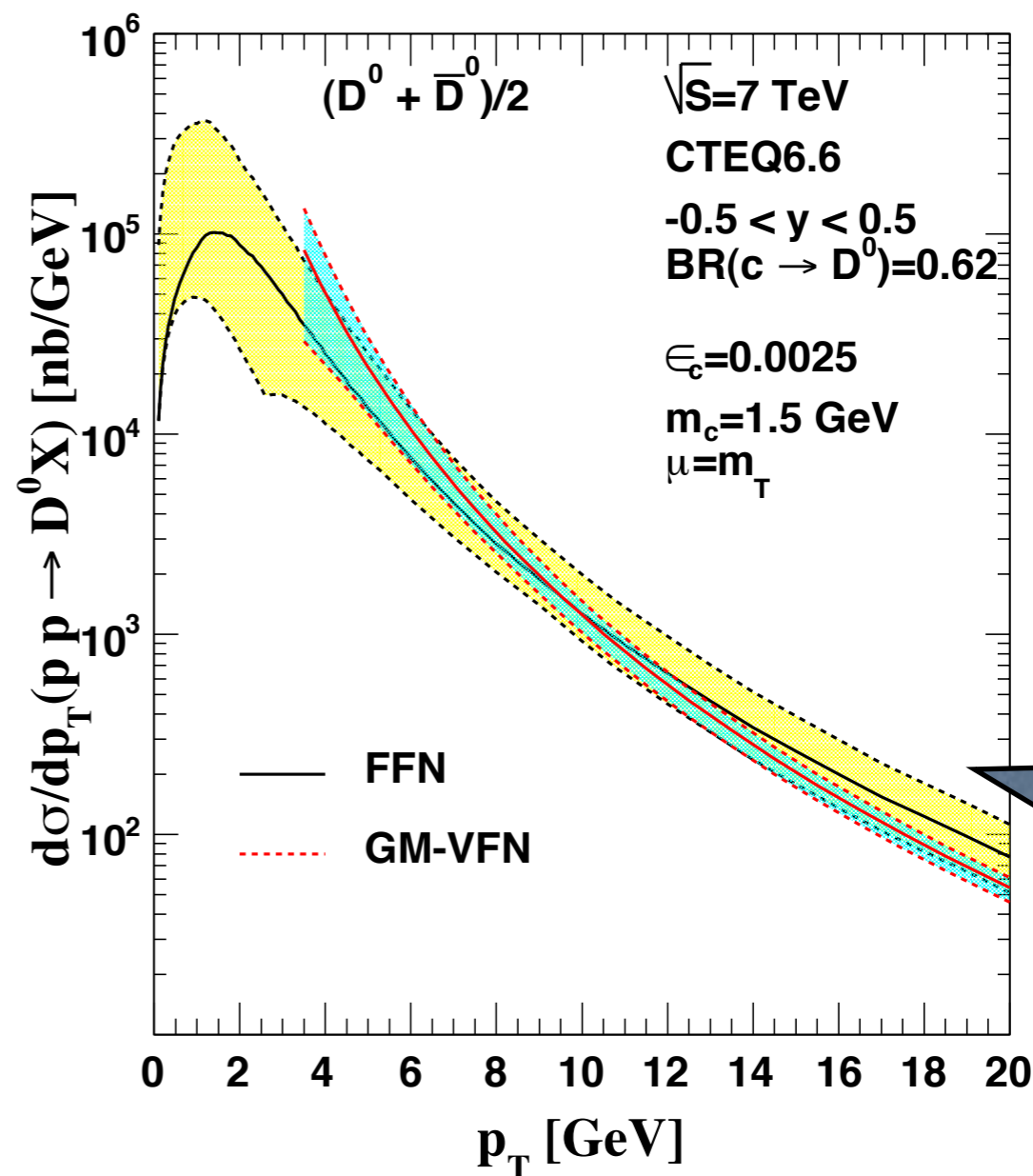
$$p + p \rightarrow B + X, \quad (B = B^\pm, B^0, B_s)$$

for comparison with LHC data from ATLAS, ALICE, LHCb, CMS

- At the LHC: expect higher statistics, higher transverse momentum
 - more reliable test of QCD,
 - better understanding of background for new physics searches



no evolved fragmentation function



Peterson FF: FFNS closer to GM-VFNS, but still too steep

A colleague: “If QCD is right, there has to be IC”
(which normalization?)

Intrinsic charm:

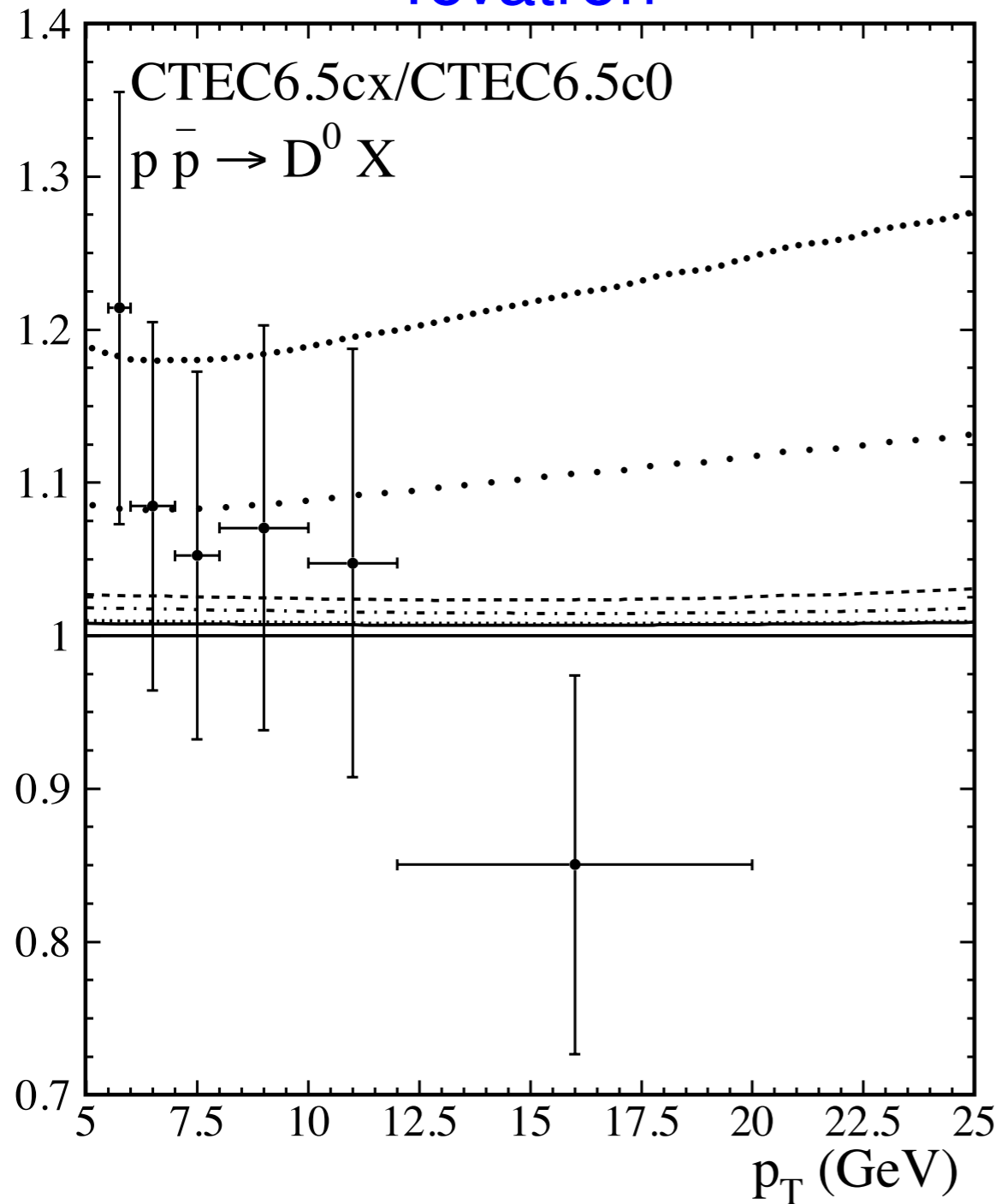
$c(x, \mu_0) \neq 0$ at initial scale $\mu_0 = m_c$

Models implemented in CTEQ 6.5C ([PRD75, 2007](#))

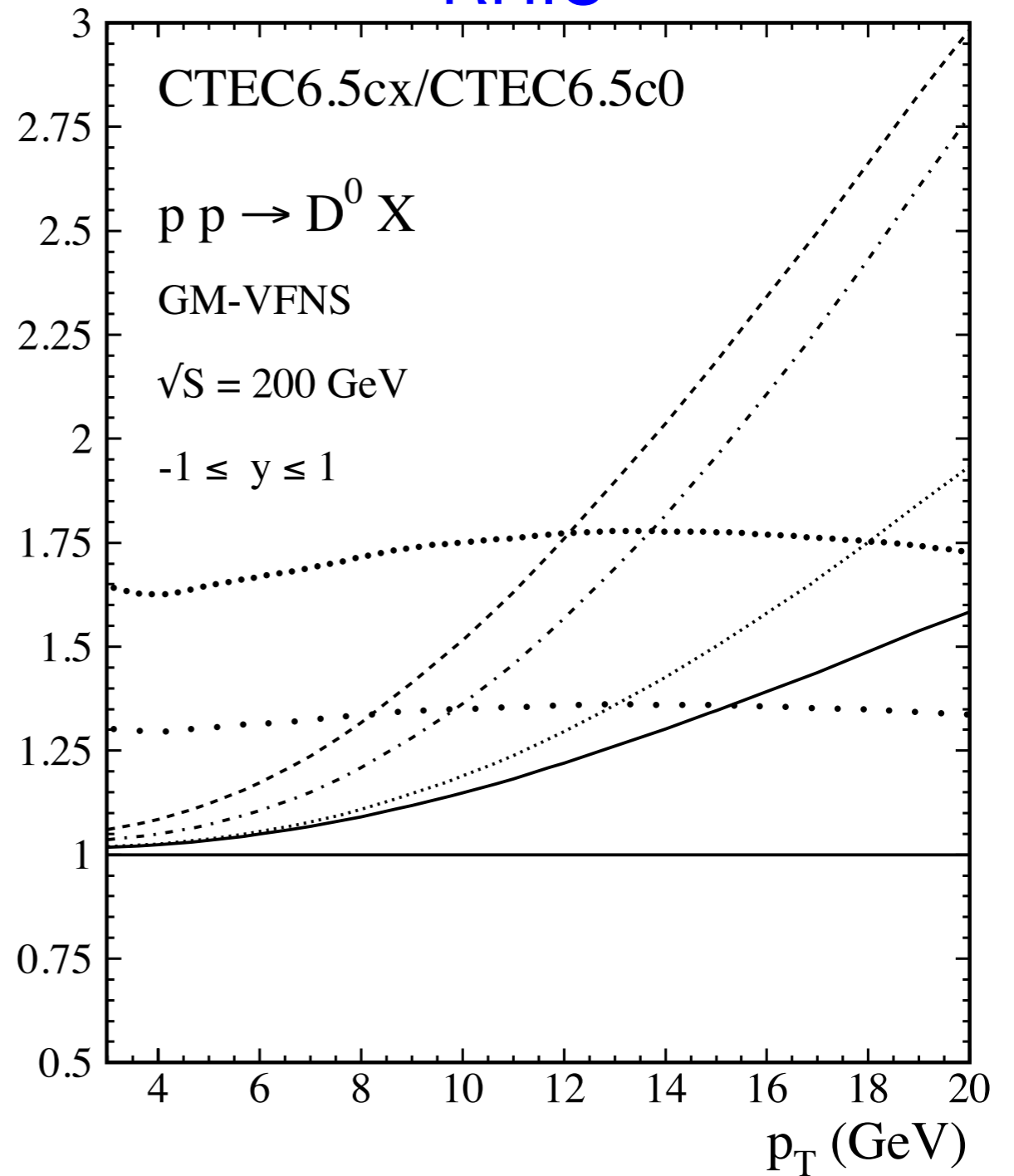
global fit allows average momentum $\langle x \rangle_{c+\bar{c}}$ or order 1 %

- 1 Light-cone Fock-space picture (Brodsky et al.), concentrated at large x
 $\langle x \rangle_{c+\bar{c}} = 0.57, 2.0 \%$
- 2 Meson-cloud model (Navarra et al.)
 $\langle x \rangle_{c+\bar{c}} = 0.96, 1.8 \%$
- 3 Phenomenological model: sea-like charm, broad in x
 $\langle x \rangle_{c+\bar{c}} = 1.1, 2.4 \%$

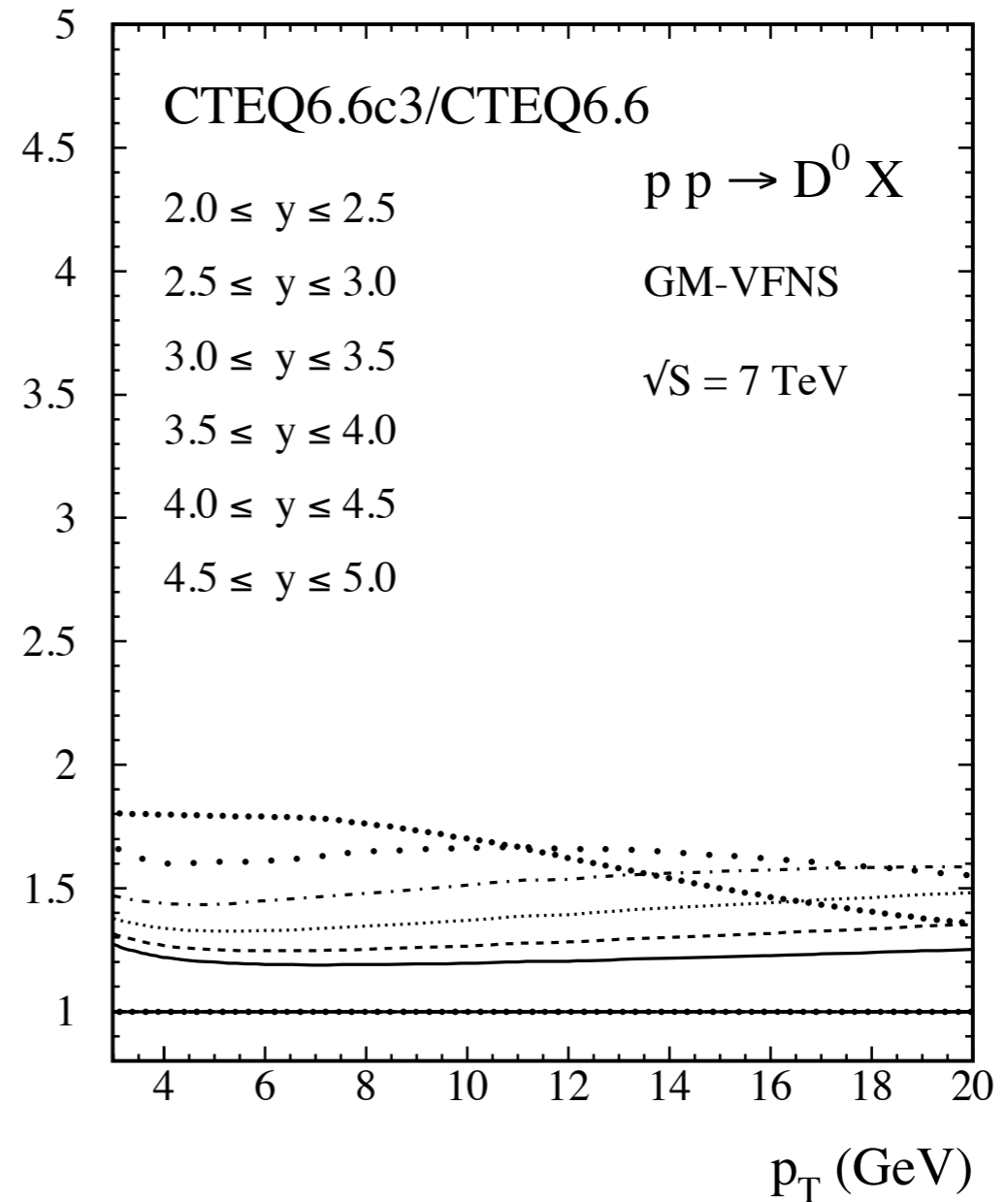
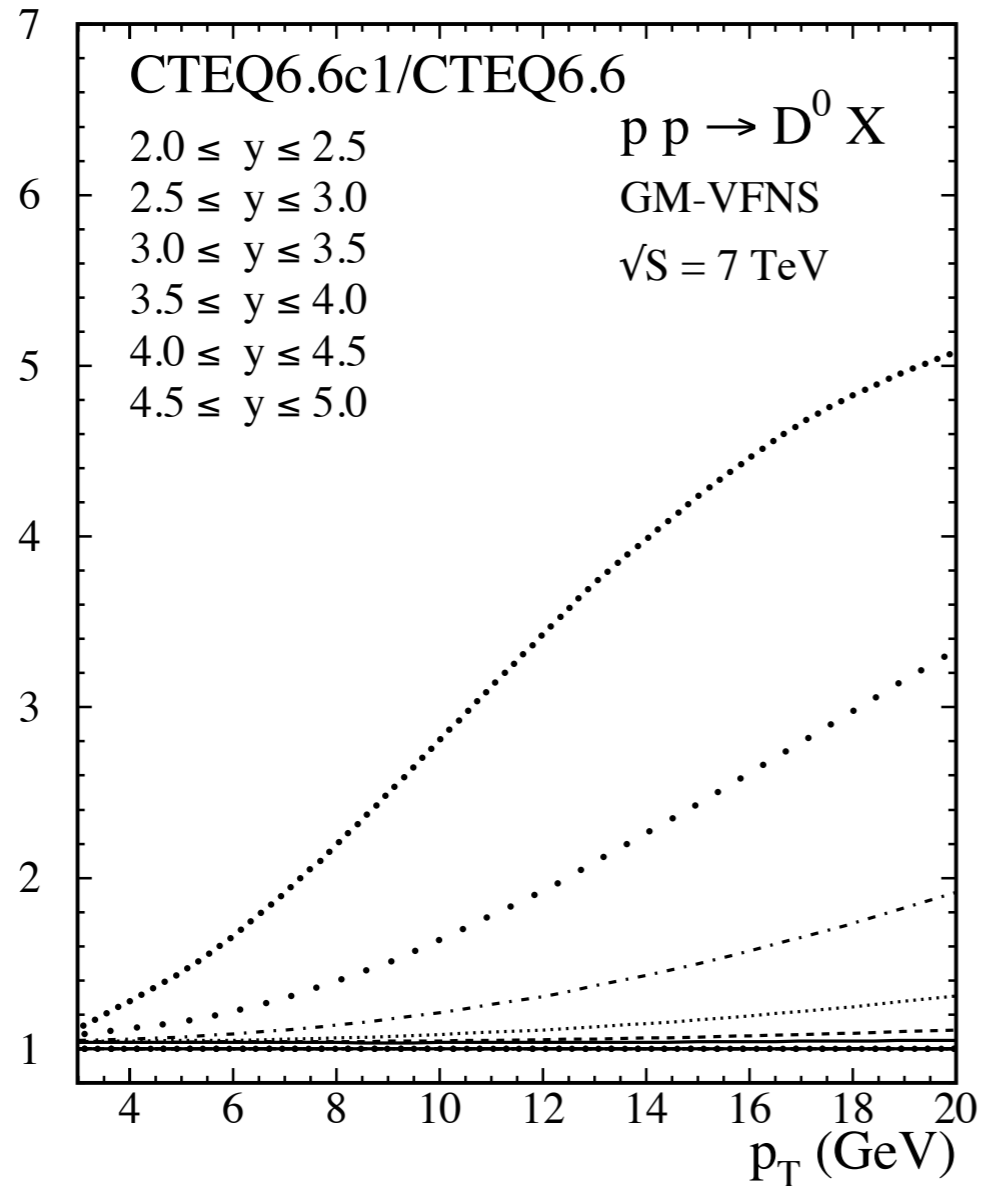
Tevatron



RHIC



PRD79, 2009



CTEQ6.6 updated:

BHPS, 3.5 % ($c + \bar{c}$) at $\mu = 1.3 \text{ GeV}$

high-strength sea-like charm

→ large effects expected at large rapidities

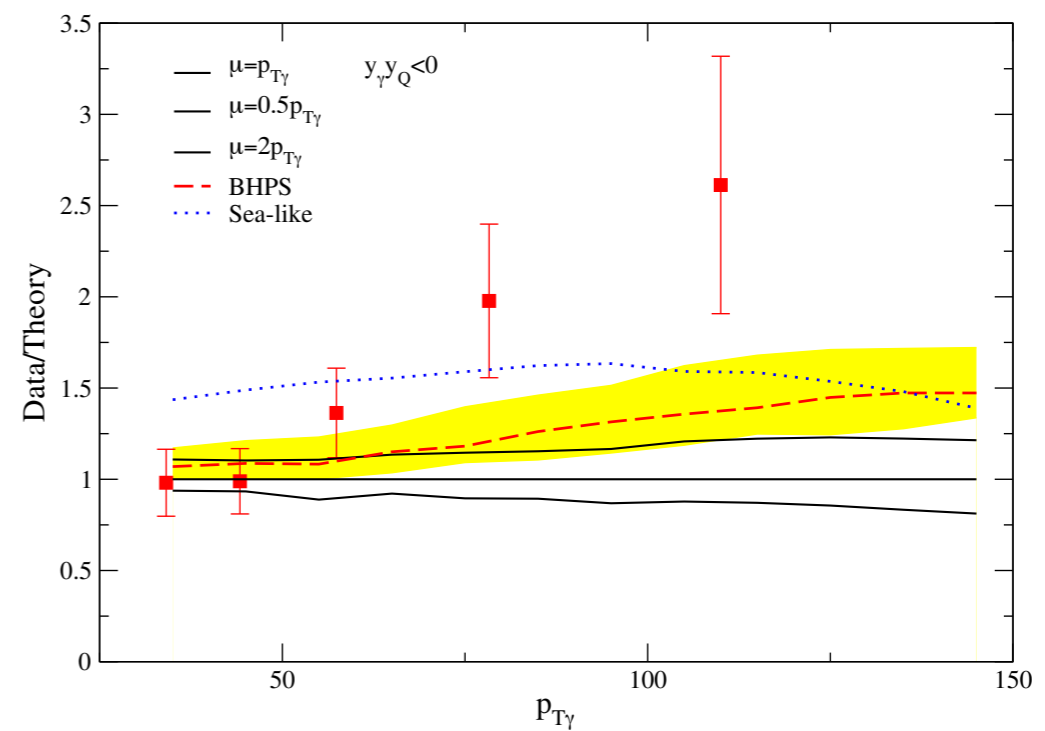
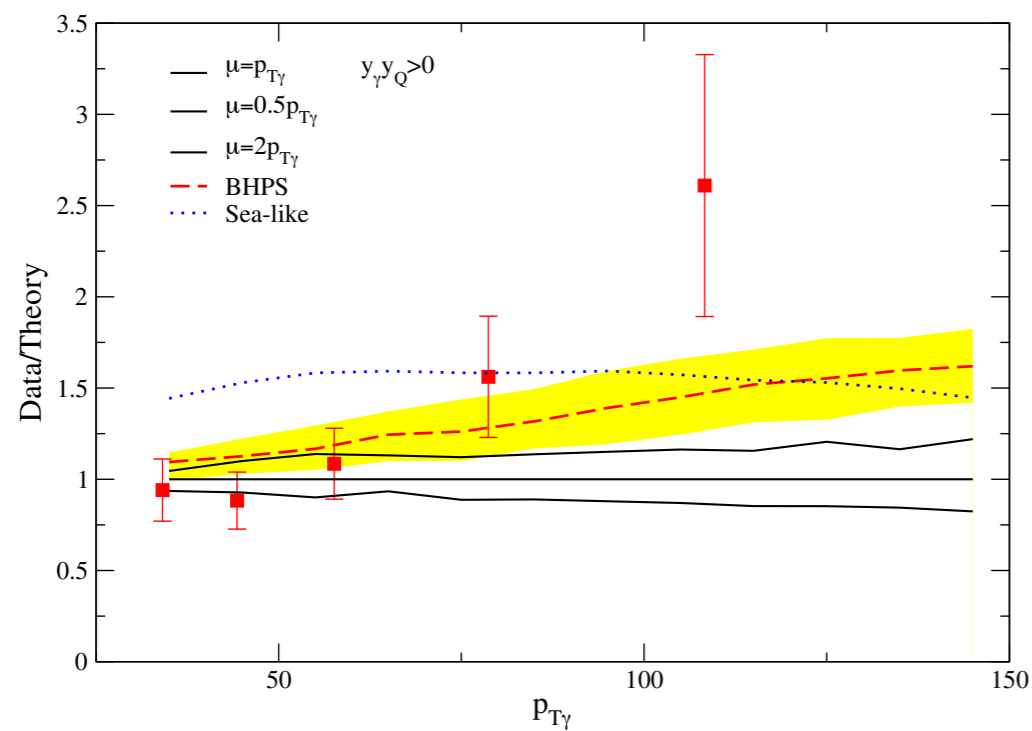
Intrinsic charm/bottom PDF via direct photon + heavy quark production

- LO: Compton hard scattering process $g + Q \rightarrow \gamma + Q$
direct access to the gluon PDF and the heavy quark PDF
- Full NLO calculation including photon fragmentation contribution
(photon isolation suppresses photon fragmentation)
[Owens, Stavreva, PRD79]
- In pA collisions useful to constrain nuclear gluon PDF [arXiv:1012.1178]
- In AA collisions probe of heavy quark energy loss
- In pp collisions probe of IC and IB

TEVATRON-DO

- Direct photon in association with charm / bottom quark jets @ D0
 - comparison of NLO theory predictions with D0 measurements [[arXiv:0901.3791](#), [arXiv:0901.0739](#)]
 - bottom quark agrees well but charm quark theory is off
 - discrepancy in photon+charm description allows for testing models of intrinsic charm

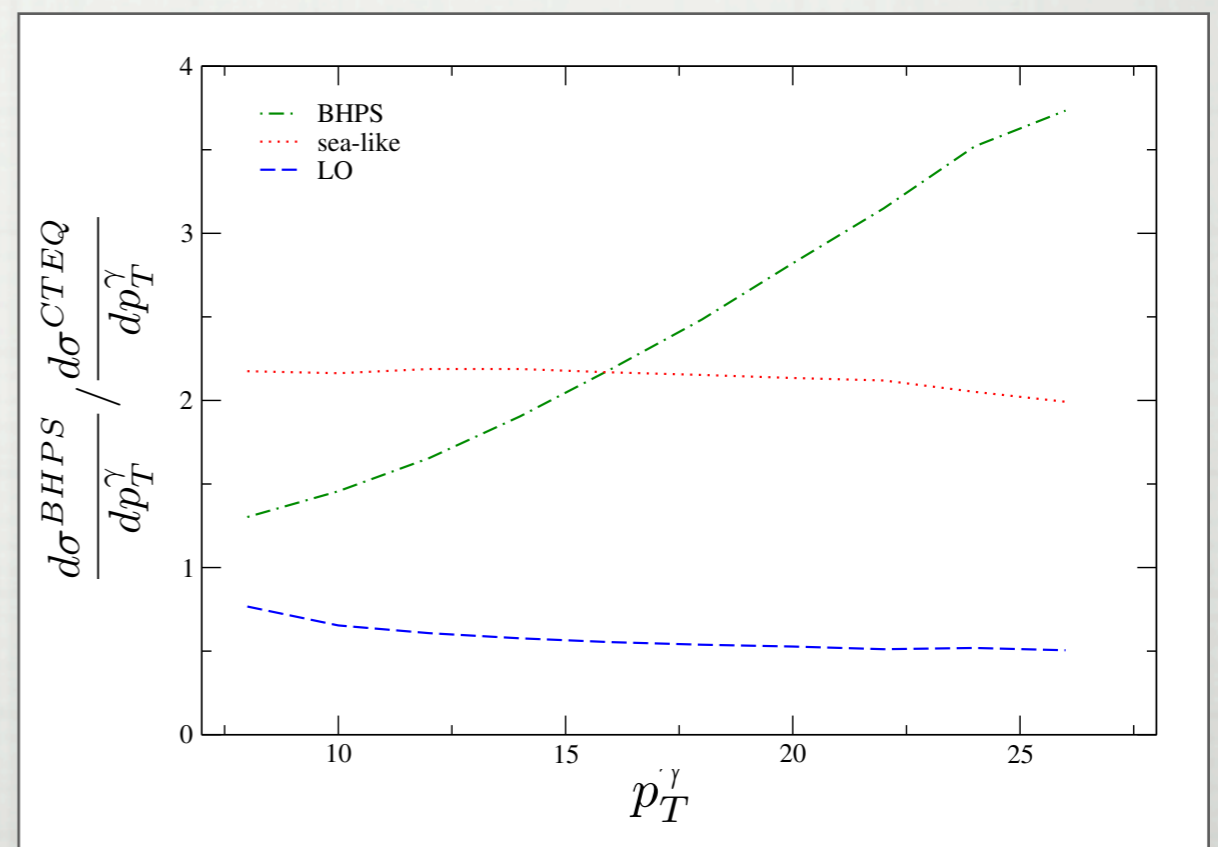
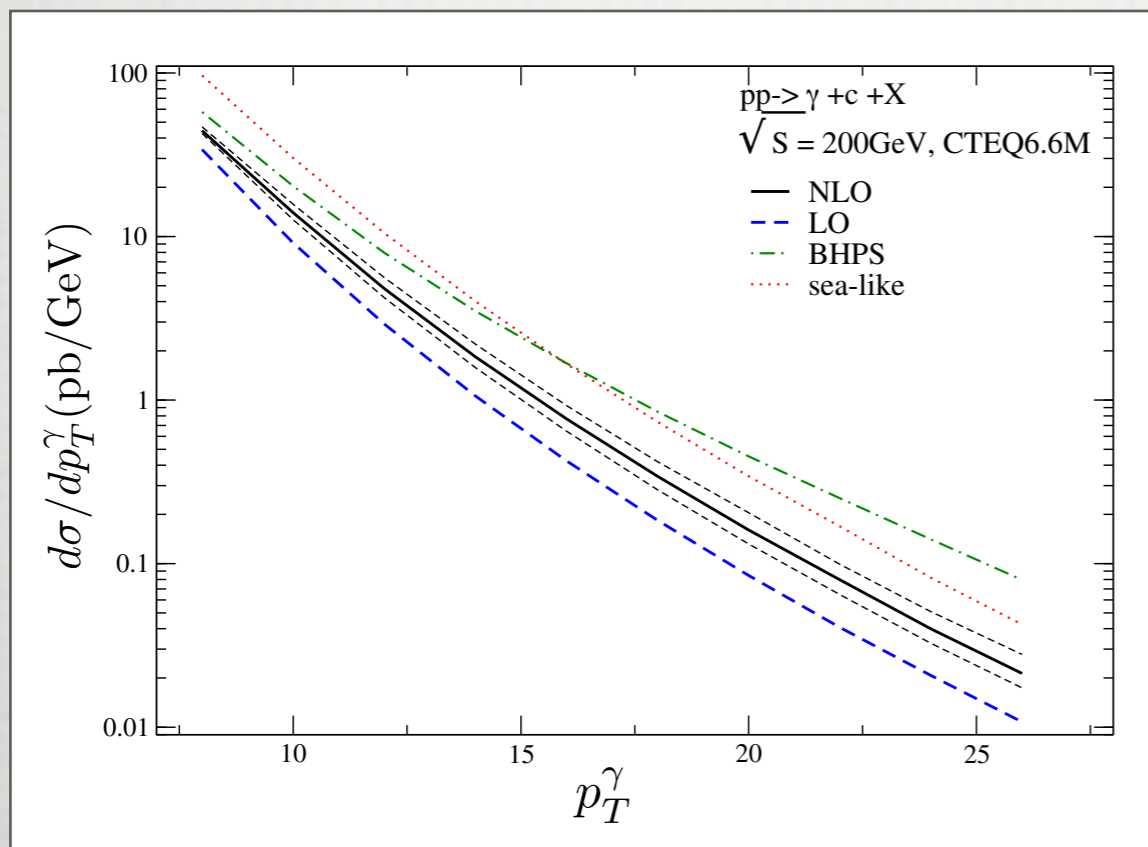
photon + charm



RHIC-PHENIX

- Direct photon in association with charm / bottom quark jets @ RHIC
 - smaller c.m.s energy @ RHIC probes higher x - very sensitive to intrinsic charm

	p_T min	Rapidity	Isolation
Photon	7 GeV	$ y_\gamma < 0.35$	$R=0.5, p_T = 0.7\text{GeV}$
Heavy Jet	5 GeV	$ y_Q < 0.8$	---

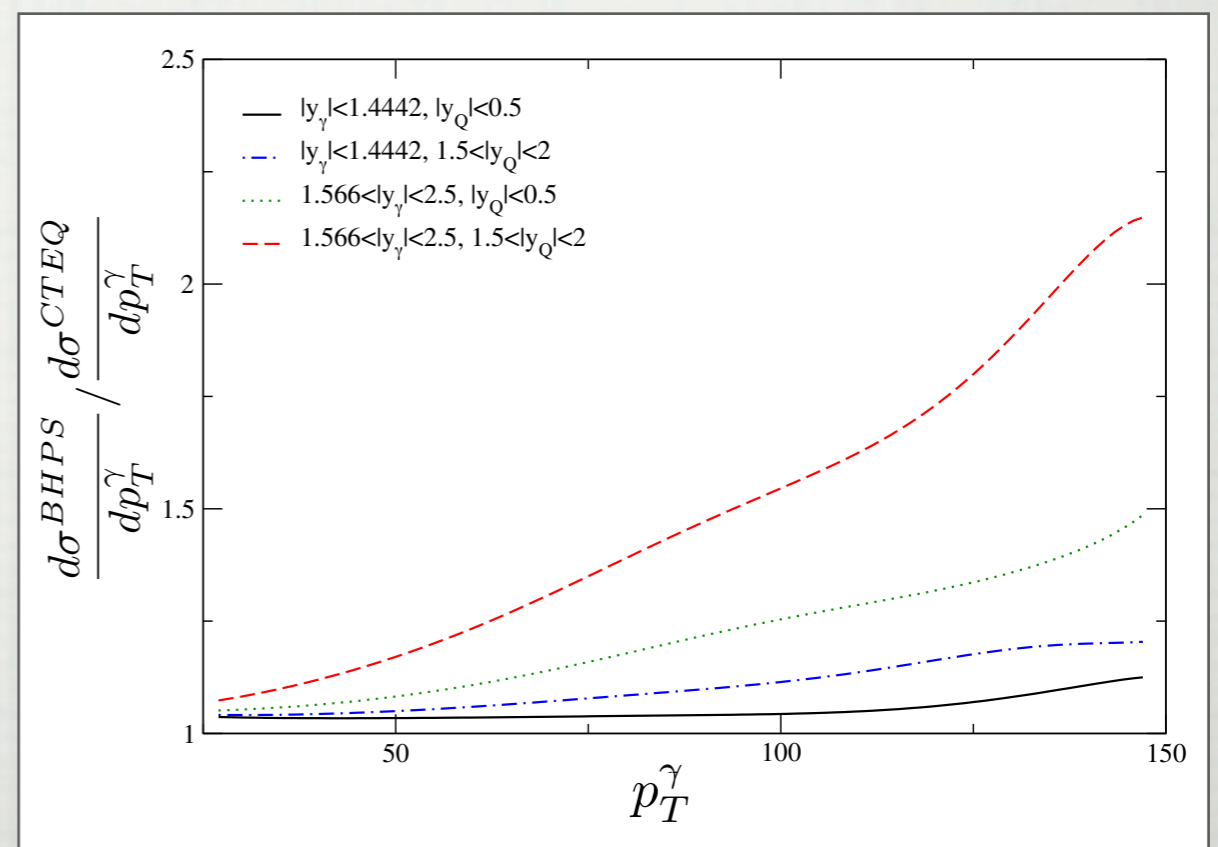
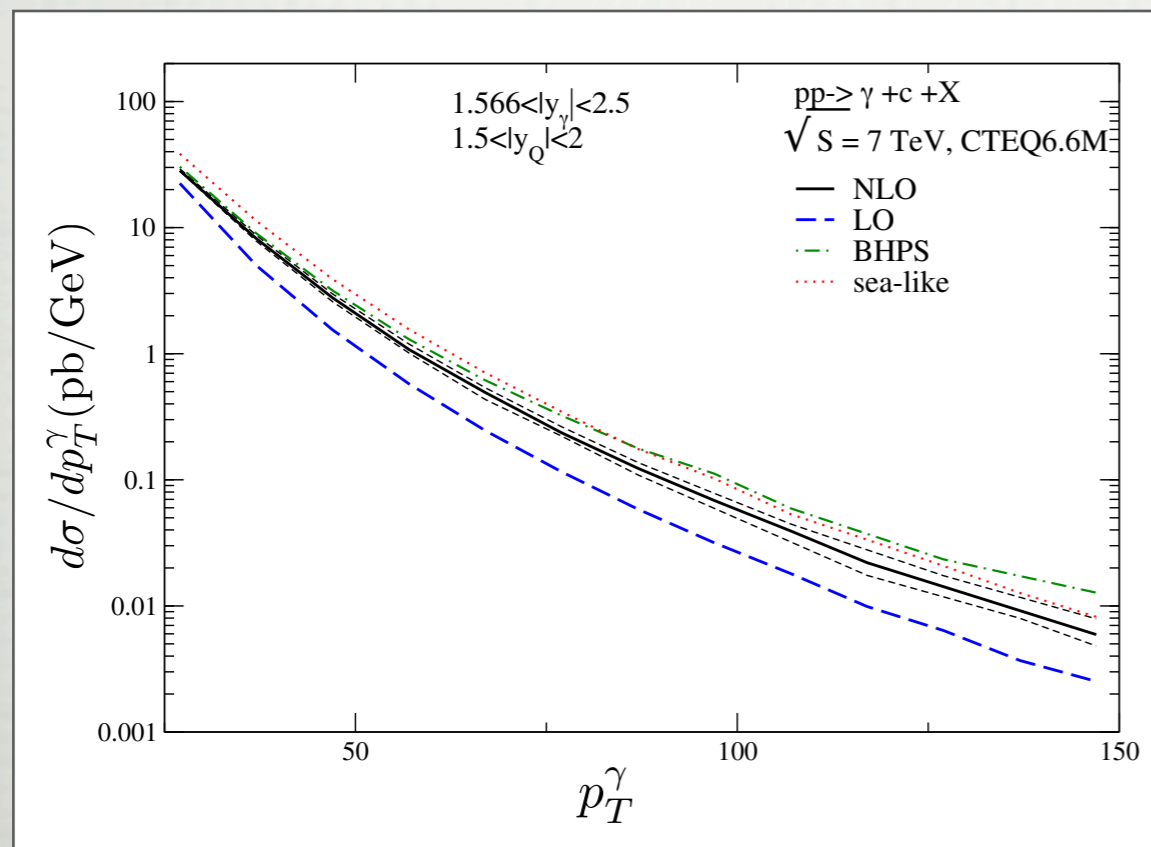


LHC-CMS

Direct photon in association with charm / bottom quark jets @ CMS

- CMS cuts on photon & HQ transverse momentum, rapidity & isolation cuts

	p_T min	Rapidity	Isolation
Photon	20 GeV	$ y_\gamma < 1.4442$	$R=0.4, p_T = 4.2\text{GeV}$
		$1.56 < y_\gamma < 2.5$	
Heavy Jet	18 GeV	$ y_Q < 2.0$	---



[CMS notes: CMS PAS EGM-10-005, CMS PAS BPH-10-009]

Charmonium

Testing NRQCD factorization with J/Ψ yield and polarization

B. Kniehl, M. Butenschön
PRL104,106,107,PRD84
arXiv:1201.1872

- NRQCD factorization:
 - Existence of CO states
 - Calculable short distance cross sections
 - Universal Long Distance Matrix Elements (LDMEs)
- **First global analysis of unpolarized world J/Ψ data at NLO**

NRQCD factorization in a nutshell

Factorization theorem: $\sigma_{J/\psi} = \sum_n \sigma_{c\bar{c}[n]} \cdot \langle O^{J/\psi}[n] \rangle$

- n : every possible Fock state, including **color-octet** states.
- $\sigma_{c\bar{c}[n]}$: production rate of $c\bar{c}[n]$, calculated in perturbative QCD.
- $\langle O^{J/\psi}[n] \rangle$: long-distance matrix elements (LDMEs), nonperturbative, extracted from experiment, universal?

Scaling rules: LDMEs scale with relative velocity v ($v^2 \approx 0.2$).

For J/ψ :

scaling	v^3	v^7	v^{11}
n	$^3S_1^{[1]}$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_{0/1/2}^{[8]}$...

- **Double expansion** in v and α_s .
- Leading term in v ($n = ^3S_1^{[1]}$) corresponds to **color-singlet model**.

Global fit at NLO in NRQCD

Fit CO LDMEs to all available world data on J/ψ inclusive production:

type	\sqrt{s}	collider	collaboration	reference
pp	200 GeV	RHIC	PHENIX	PRD82(2010)012001
$p\bar{p}$	1.8 TeV	Tevatron I	CDF	PRL97(1997)572; 578
$p\bar{p}$	1.96 TeV	Tevatron II	CDF	PRD71(2005)032001
pp	7 TeV	LHC	ALICE ATLAS CMS LHCb	NPB(PS)214(2011)56 PoS(ICHEP 2010)013 EPJC71(2011)1575 EPJC71(2011)1645
γp	300 GeV	HERA I	H1, ZEUS	EPJ25(2002)25; 27(2003)173
γp	319 GeV	HERA II	H1	EPJ68(2010)401
$\gamma\gamma$	197 GeV	LEP II	DELPHI	PLB565(2003)76
e^+e^-	10.6 GeV	KEKB	BELLE	PRD79(2009)071101

- Fit values:

$$10^{-2} \text{ GeV}^{3+2L}$$

$$\langle \mathcal{O}(^1S_0^{[8]}) \rangle = 4.97 \pm 0.44$$

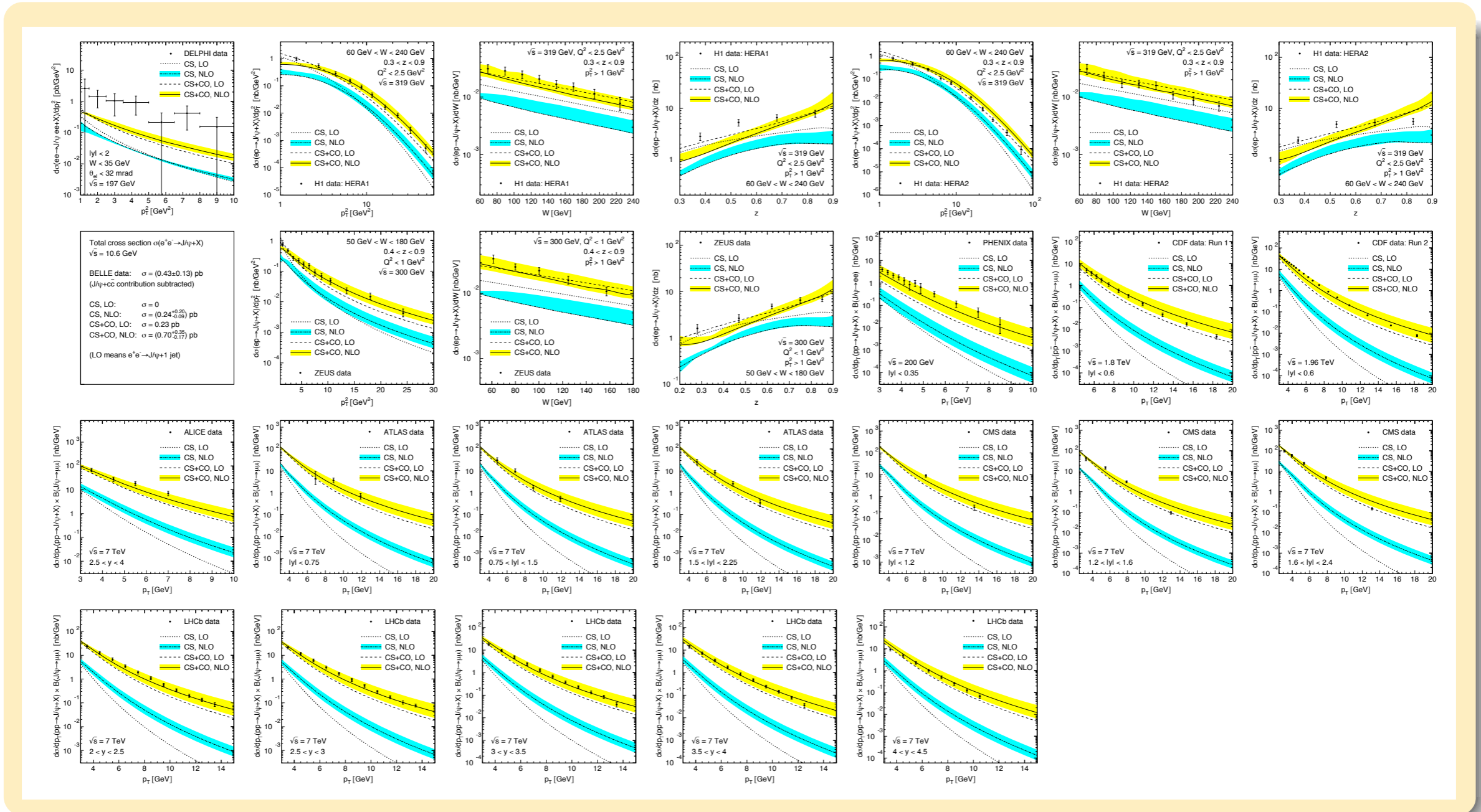
$$\langle \mathcal{O}(^3S_1^{[8]}) \rangle = 0.224 \pm 0.059$$

$$\langle \mathcal{O}(^3P_0^{[8]}) \rangle = -1.61 \pm 0.20$$

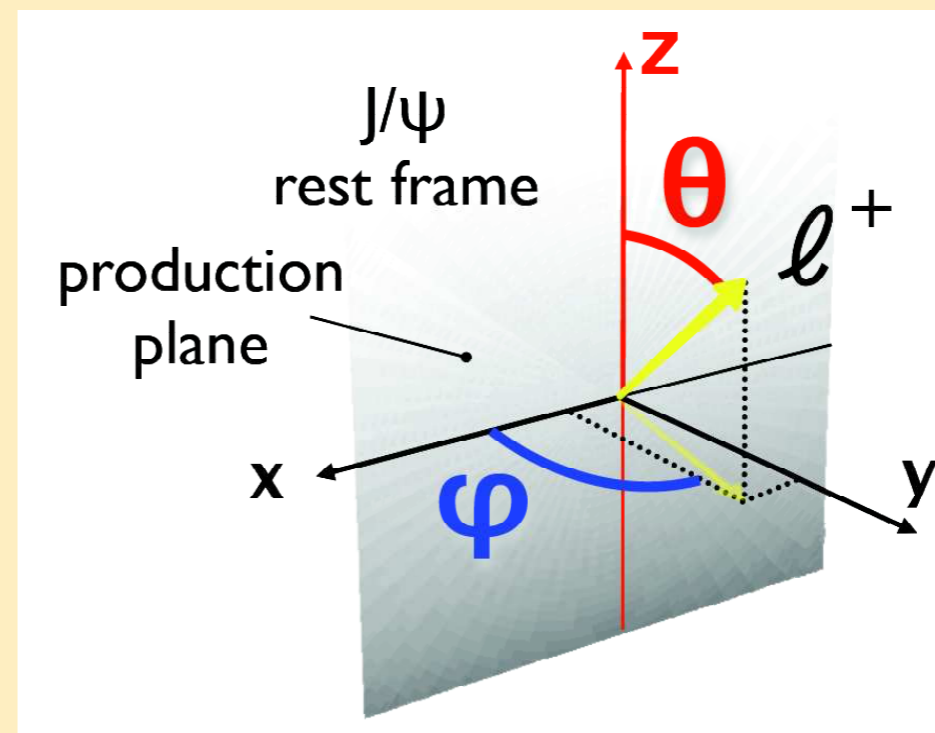
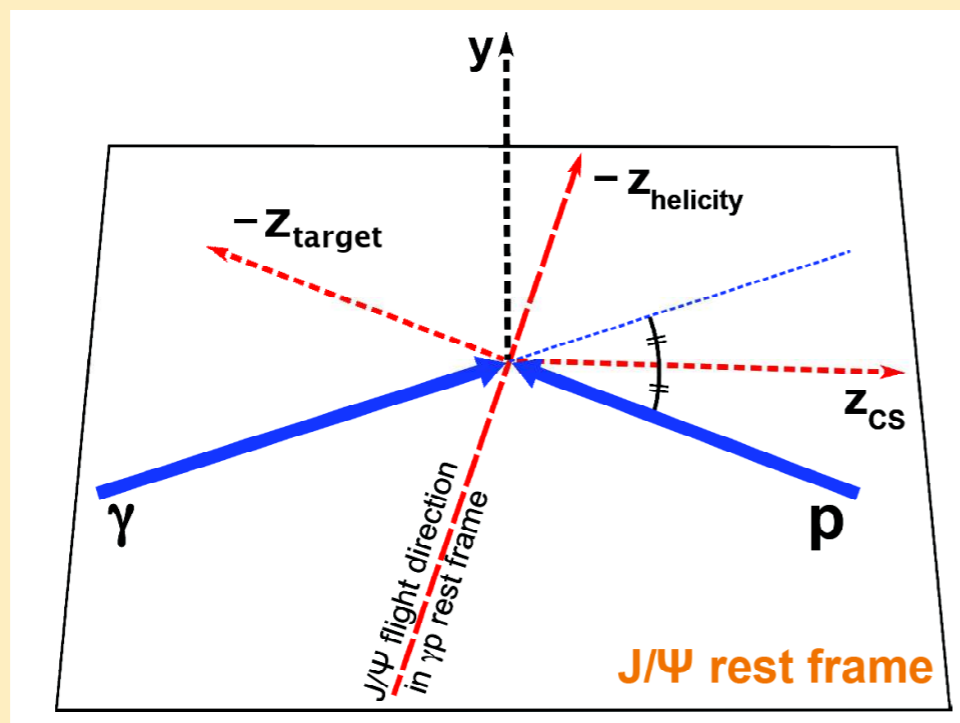
- $\chi^2/\text{d.o.f.} = 857/194 = 4.42$ for default prediction

- $\propto v^4 \langle \mathcal{O}_1(^3S_1) \rangle \rightsquigarrow$ NRQCD velocity scaling rules \checkmark

Comparison with world data



Polarized J/ψ photoproduction



Decay angular distribution:

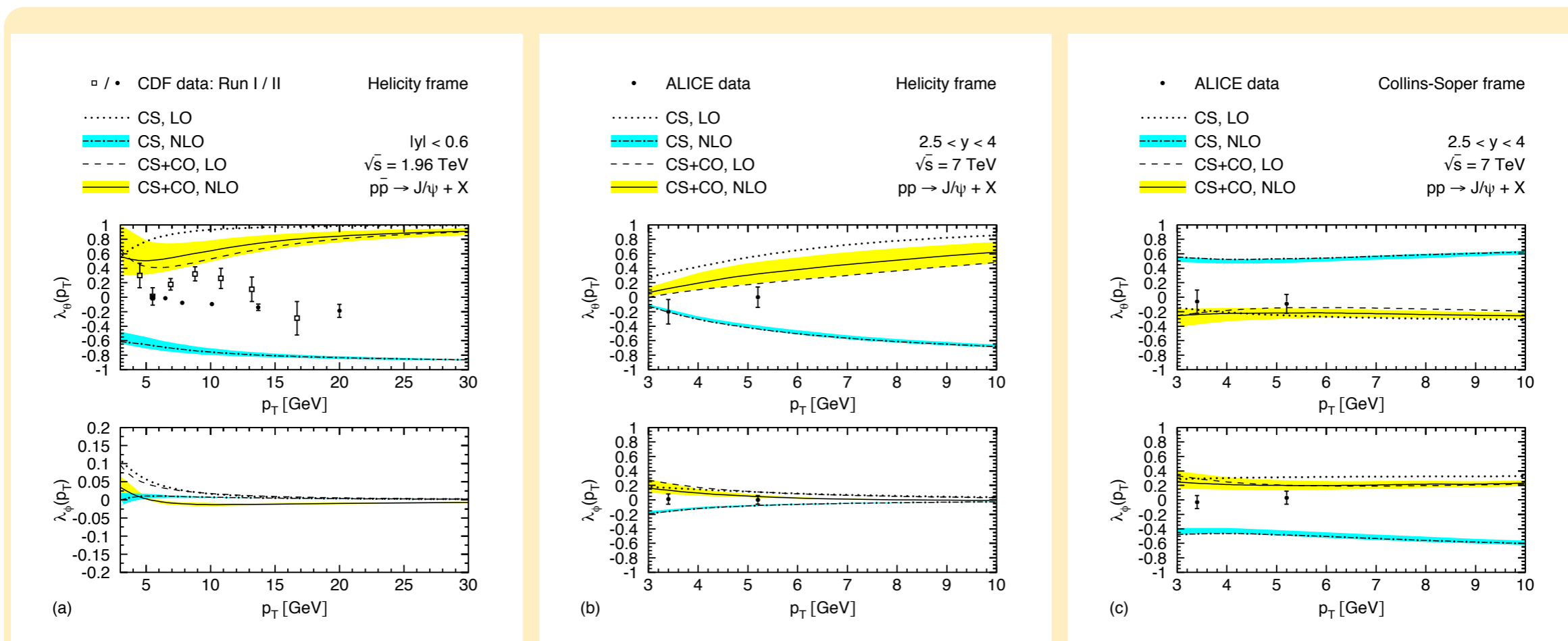
$$\frac{d\Gamma(J/\psi \rightarrow l^+ l^-)}{d\cos\theta d\phi} \propto 1 + \lambda_\theta \cos^2\theta + \lambda_\phi \sin^2\theta \cos(2\phi) + \lambda_{\theta\phi} \sin(2\theta) \cos\phi$$

Polarization observables in spin density matrix formalism:

$$\lambda_\theta = \frac{d\sigma_{11} - d\sigma_{00}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_\phi = \frac{d\sigma_{1,-1}}{d\sigma_{11} + d\sigma_{00}}, \quad \lambda_{\theta\phi} = \frac{\sqrt{2}\text{Re} d\sigma_{10}}{d\sigma_{11} + d\sigma_{00}}$$

$\lambda = 0, +1, -1$: unpolarized, transversely and longitudinally polarized.

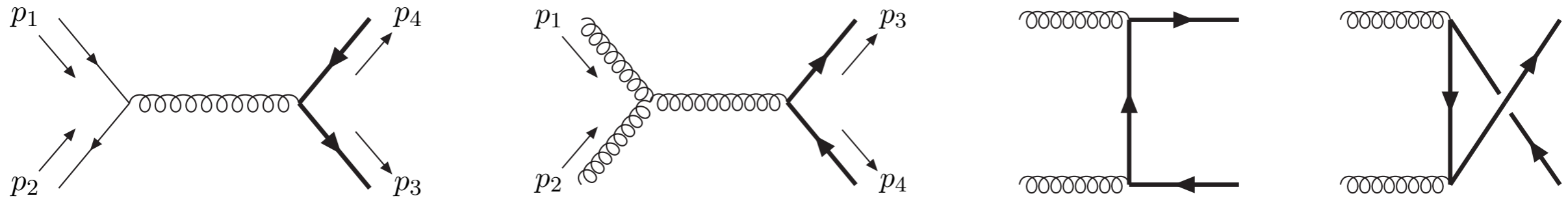
Comparison with CDF and ALICE



- CDF I and II data mutually inconsistent for $p_T < 12$ GeV.
- CDF J/ψ polarization anomaly persists at NLO (10–20 σ).
- 4/8 ALICE points agree w/ NLO NRQCD within errors, others $< 2\sigma$ away.

Top

Top quark pair production



- Two channels at tree-level
- Quark-antiquark annihilation dominant at the Tevatron ($\sim 90\%$)
- Gluon fusion dominant at the LHC ($\sim 75\%$ for 7 TeV)

Top quark pair production

- Observables:
 - Cross section
 - Distributions: t-tbar invariant mass M , p_T , y
 - Asymmetries: A_{FB} , A_C (charge asymmetry)
- Calculations:
 - exact NNLO (talk by [A. Mitov](#))
 - NLO + Resummed: NLO+NNLL ([L. Yang](#), [N. Kidonakis](#))
(Note: different resummations are used)
 - approximate NNLO ([L. Yang](#))

Status of fixed-order calculations

- NLO results known since ~20 years

Nason, Dawson, Ellis ('88-'90); Beenakker, Kujif, van Neerven, Smith, Schuler ('89-'91); Mangano, Nason, Ridolfi ('92); Czakon, Mitov ('08)

- Scale uncertainty ~15%, need to go beyond for LHC!
- Off-shell effects found to be small

Denner, Dittmaier, Kallweit, Pozzorini ('10); Bevilacqua, Czakon, van Hameren, Papadopoulos, Worek ('10)

- NNLO in progress Channels: $q\bar{q}$, gg , qg

- Two-loop virtual is the main obstacle $M_2^{(0)} + M_2^{(1)} + M_2^{(2)}$

Analytic approach: Bonciani, Ferroglia, Gehrmann, Maitre, Studerus, von Manteuffel ('08-'10);
Numeric approach: Czakon et al.

- Virtual+real $M_3^{(0)} + M_3^{(1)}$
Dittmaier, Uwer, Weinzierl ('08)

- New subtraction method for double real $M_4^{(0)}$
Czakon ('10-'11)

- May be available in the near future!

Talk by Alexander Mitov

NNLO result for $qq \rightarrow t\bar{t}$ at Tevatron and LHC

Work with M. Czakon, P. Barnreuther

- ✓ First ever hadron collider calculation at NNLO with more than 2 colored partons.
- ✓ First ever NNLO hadron collider calculation with massive fermions.

Computed partonic reactions. Dominant at Tevatron (~85%)

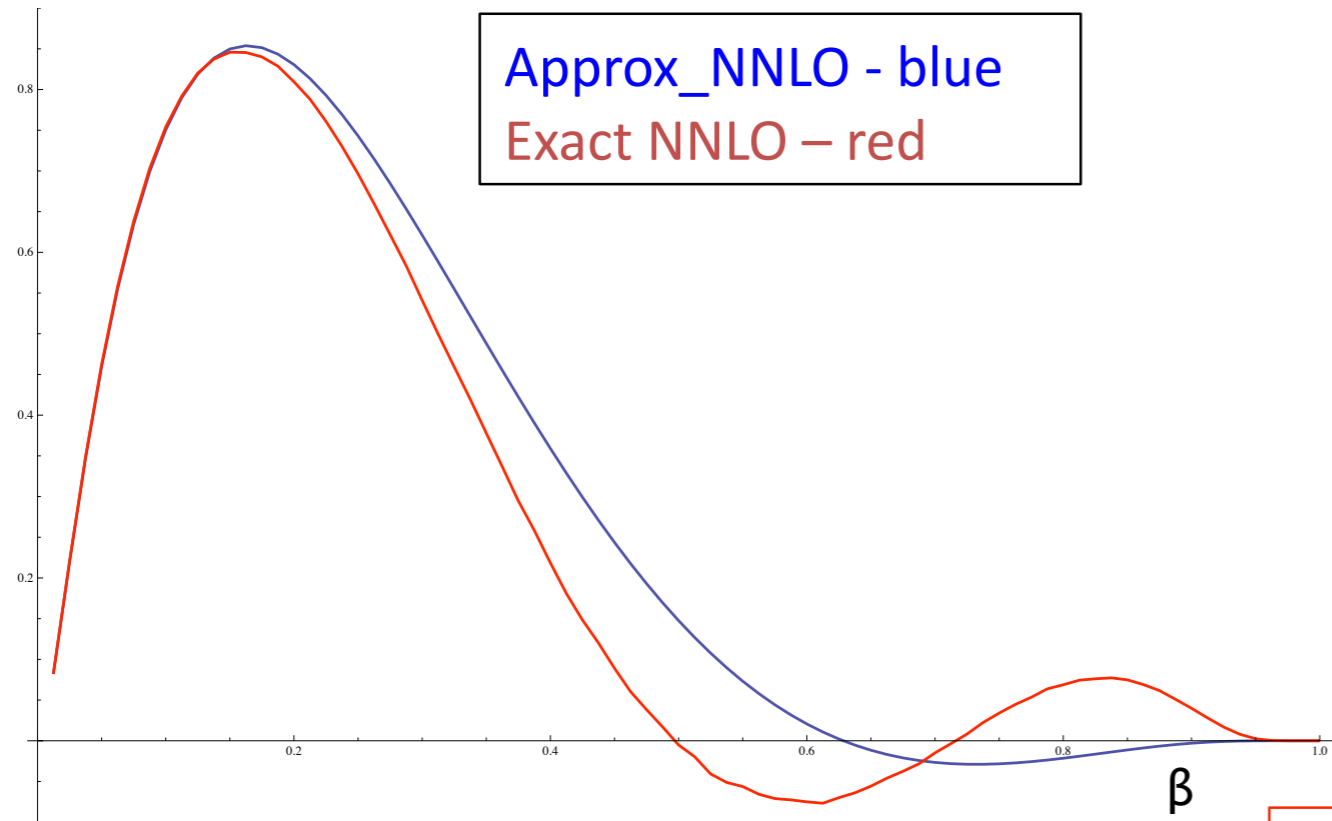
$$\begin{aligned} q\bar{q} &\rightarrow t\bar{t} \\ q\bar{q} &\rightarrow t\bar{t}g \\ q\bar{q} &\rightarrow t\bar{t}gg \\ q\bar{q} &\rightarrow t\bar{t}q'\bar{q}', \quad q \neq q' \end{aligned}$$

$$\begin{aligned} gg &\rightarrow t\bar{t} \\ gg &\rightarrow t\bar{t}g \\ gg &\rightarrow t\bar{t}gg \\ gg &\rightarrow t\bar{t}q\bar{q} \end{aligned}$$

$$\begin{aligned} qg &\rightarrow t\bar{t}q \\ qg &\rightarrow t\bar{t}qg \\ qq' &\rightarrow t\bar{t}qq', \quad q \neq q' \\ q\bar{q} &\rightarrow t\bar{t}q\bar{q} \end{aligned}$$

In progress

Partonic cross-section, convoluted with partonic flux:



Approx_NNLO - blue
Exact NNLO - red

$$\sigma = \frac{\alpha_s^2}{m_t^2} \sum_{ij} \int_0^{\beta_{\max}} \mathcal{L}_{ij}(\beta) \hat{\sigma}(\beta)$$

✓ 50% scales reduction compared to the NLO+NNLL!

Unmatched precision at the Tevatron!

Numerical predictions for the Tevatron (preliminary)

Pure NNLO:
sigma_tot = 7.004 + 2.9 % - 4.4 % [pb].

With resummation NNLO+NNLL:
sigma_tot = 7.048 + 1.9 % - 3.2 % [pb].

Recent results

- ✓ We have also prepared the tools for top physics:

Top++ : a C++ program for the calculation of the total cross-section:

Czakon, Mitov `11

- ✓ Includes:
 - fixed order (NLO and NNLO_approx at present)
 - and resummation (full NNLL already there)
- ✓ It is meant to incorporate the full NNLO once available (**to appear**)
- ✓ Very user friendly.

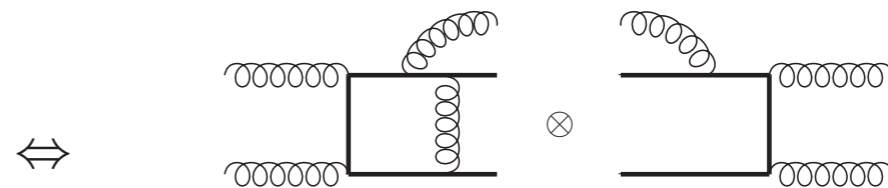
The singular behavior of one-loop massive QCD amplitudes with one external soft gluon

talk by Isabella Bierenbaum, based on work with M. Czakon and A. Mitov

Nucl. Phys. B **856** (2012) 228 [arXiv:1107.4384]

Contributing “virtual + real diagrams” in the framework of the NNLO $t\bar{t}$ calculation:

Integration over the real external gluon generates a divergence when the gluon is soft and/or collinear to the external legs



- Construct a subtraction term in the soft limit for the squared amplitude $|M|^2$
- Following the approach for the massless case by [Catani & Grazzini, \(2000\)](#):

“Factorize” the singularities:

$$M_a^{(1)}(n+1, q) \simeq \underbrace{J_a^{(0)}(q) M^{(1)}(n)}_{\text{factorizable}} + \underbrace{J_a^{(1)}(q) M^{(0)}(n)}_{\text{non-factorizable}}$$

$J_a^{(1)}(q)$ is the *universal* one-loop soft-gluon current in the massive case.

$J_a^{(1)}(q)$ is calculated here for three kinematical cases of one or two massive external fermions.

Threshold enhancement and resummation

- Can improve fixed-order results by adding or resumming *threshold enhanced* terms in higher orders
- Schematically, the threshold enhanced terms looks like (in Laplace or Mellin space)

$$\begin{aligned} d\hat{\sigma} = & 1 + \alpha_s (L^2 + L + 1) \\ & + \alpha_s^2 (L^4 + L^3 + L^2 + L + 1) + \text{power corrections} \\ & + \dots \end{aligned}$$

- Can be resummed to all orders at certain logarithmic accuracy using re-factorization and renormalization-group equations

NLO+NNLL

- Alternatively, can construct an *approximate NNLO* cross section

NNLO_approx

Three types of threshold

- Production threshold (small- β) — relevant for total cross section

$$\beta = \sqrt{1 - \frac{4m_t^2}{\hat{s}}} \rightarrow 0$$

Berger, Contopanagos, Bonciani, Catani, Mangano, Nason, Langenfeld, Moch, Uwer, Beneke, Falgari, Klein, Schwinn, Cacciari, Czakon, Mitov...

- PIM threshold — relevant for invariant mass distribution, charge asymmetry in $t\bar{t}$ frame (and total cross section)

$$z = \frac{M_{t\bar{t}}^2}{\hat{s}} \rightarrow 1$$

Sterman, Kidonakis, Oderda, Vogelsang, Laenen, Moch, Vogt, Almeida...

- 1PI threshold — relevant for transverse momentum and rapidity distribution, charge asymmetry in $p\bar{p}$ frame (and total cross section)

$$s_4 = \hat{s} + \hat{t}_1 + \hat{u}_1 \rightarrow 0$$

Sterman, Oderda, Laenen, Kidonakis, Moch, Vogt...

We work in these two

**Additional differences between
PIM vs PIM_{SCET} and PI vs PI_{SCET}**

Approximate NNLO

- Two-loop anomalous dimension matrices

Ferrogia, Neubert, Pecjak, LLY [arXiv:0907.4791] [arXiv:0908.3676]

- One-loop hard matrix

Ahrens, Ferrogia, Neubert, Pecjak, LLY [arXiv:1003.5827]

- One-loop soft matrix for PIM kinematics



- One-loop soft matrix for 1PI kinematics

Ahrens, Ferrogia, Neubert, Pecjak, LLY [arXiv:1103.0550]

$$d\hat{\sigma}^{(2)} \approx \alpha_s^2 (L^4 + L^3 + L^2 + L + 1)$$

Predict all log terms at NNLO



missing: exact NNLO



Total cross section

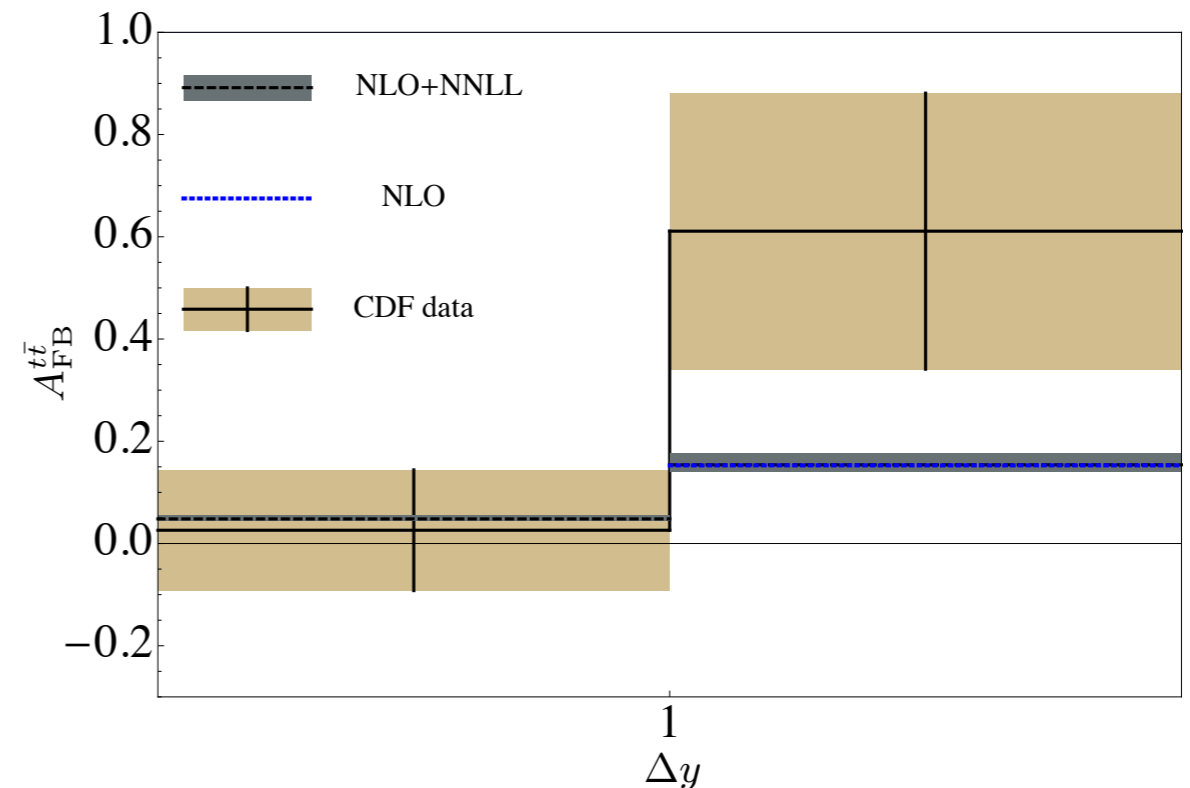
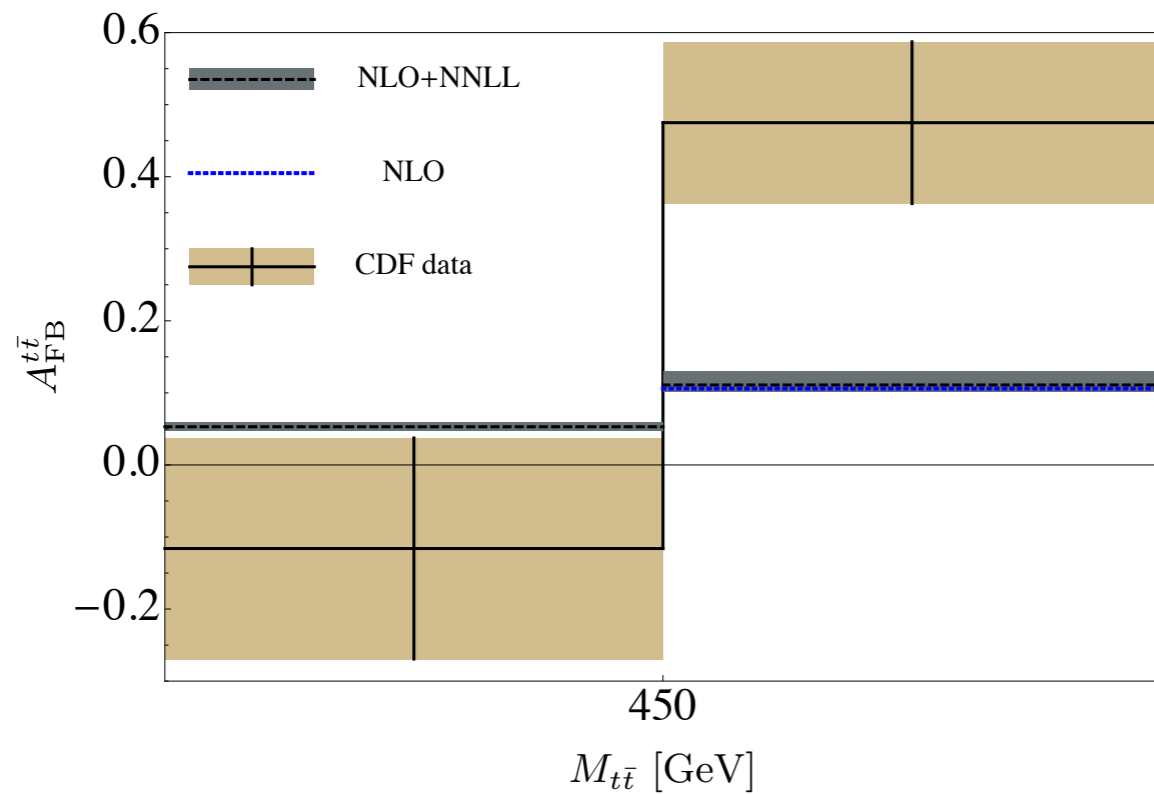
Ahrens, Neubert, Pecjak, Ferroglia, LLY [arXiv:1105.5824]

- Can integrate both PIM and 1PI distributions to get the total cross section
- We find nice agreement between the two kinematics — use the difference as an additional uncertainty
- Computer code available (parallel enabled):
<http://www.physik.uzh.ch/~llyang/TopNNLO.tar.gz>

$m_t = 173.1$ GeV	Tevatron	LHC7	LHC8
NLO	$6.72^{+0.41+0.47}_{-0.76-0.45}$	159^{+20+14}_{-21-13}	228^{+28+19}_{-30-17}
NNLO approx.	$6.63^{+0.07+0.63}_{-0.41-0.48}$	155^{+8+14}_{-9-14}	221^{+12+19}_{-12-19}

Charge asymmetry — $M_{t\bar{t}}$ and y dependence

Ahrens, Ferroglia, Neubert, Pecjak, LLY [arXiv:1106.6051]



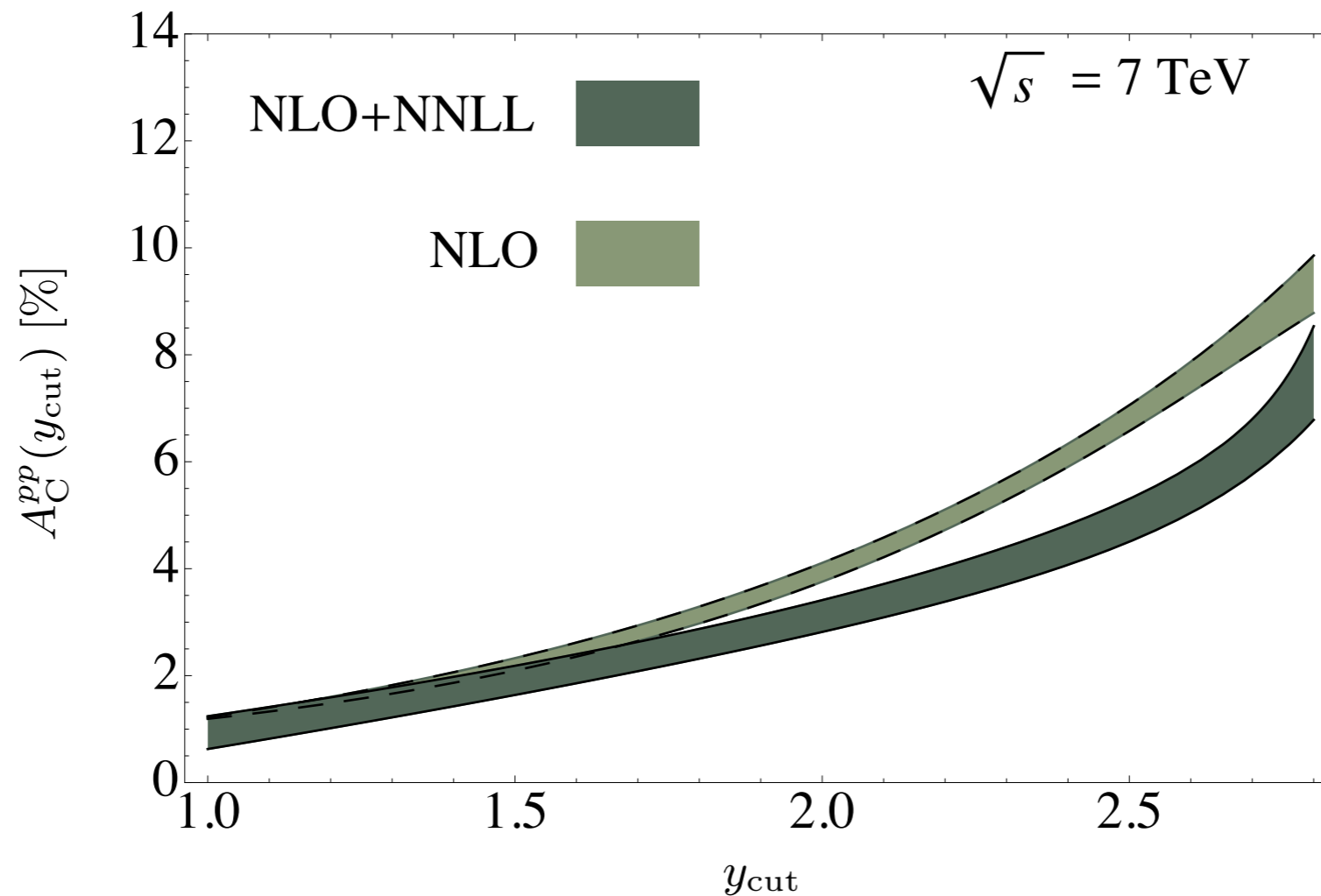
- Higher order predictions consistent with NLO

Of course, exact NNLO can change the picture!

- Discrepancies at high invariant mass and rapidity not resolved

Charge asymmetry at the LHC

Ahrens, Ferroglia, Neubert, Pecjak, LLY [arXiv:1106.6051]



- Increase with higher rapidity cut — but less statistics
- NLO prediction depends a lot on whether or not to expand the ratio in α_s

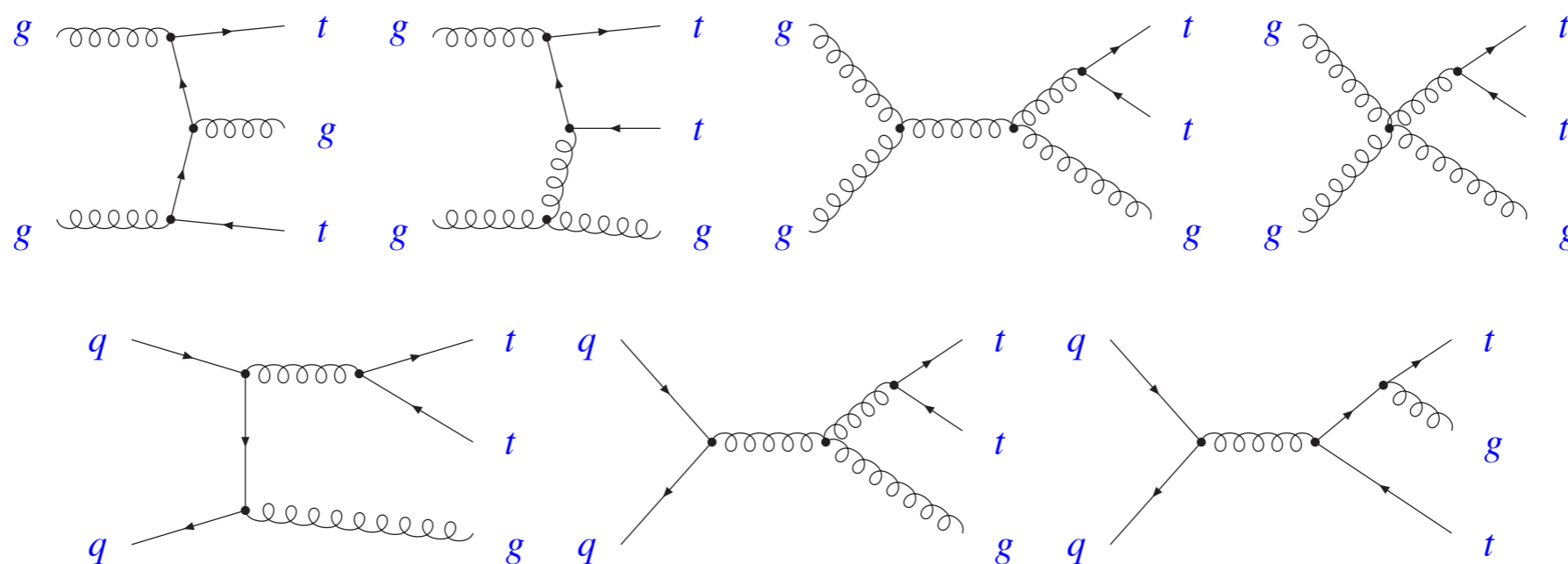
Single top

- Large number of results/figures for LHC7, LHC8, LHC14 and Tevatron
- t-channel, Wt production, s-channel
- cross section vs m_t
- p_T -distribution
- see slides for details

Top-quark pairs with one jet

Production of $t\bar{t}$ +jet at fixed order

- LHC: large rates for production of $t\bar{t}$ -pairs with additional jets
- Scale dependence at LO large



- Feynman diagrams (sample) for $t\bar{t}$ +jet production at LO

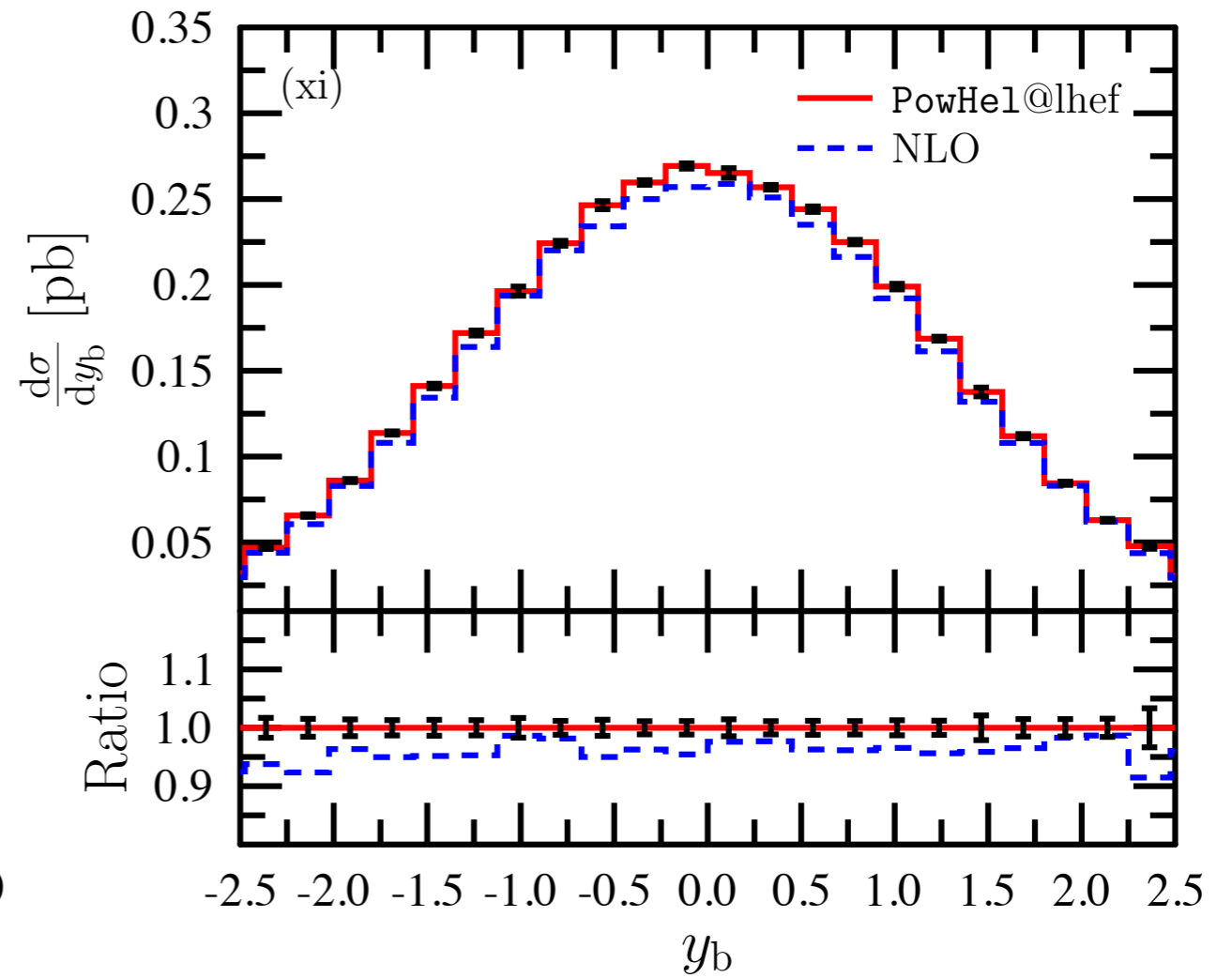
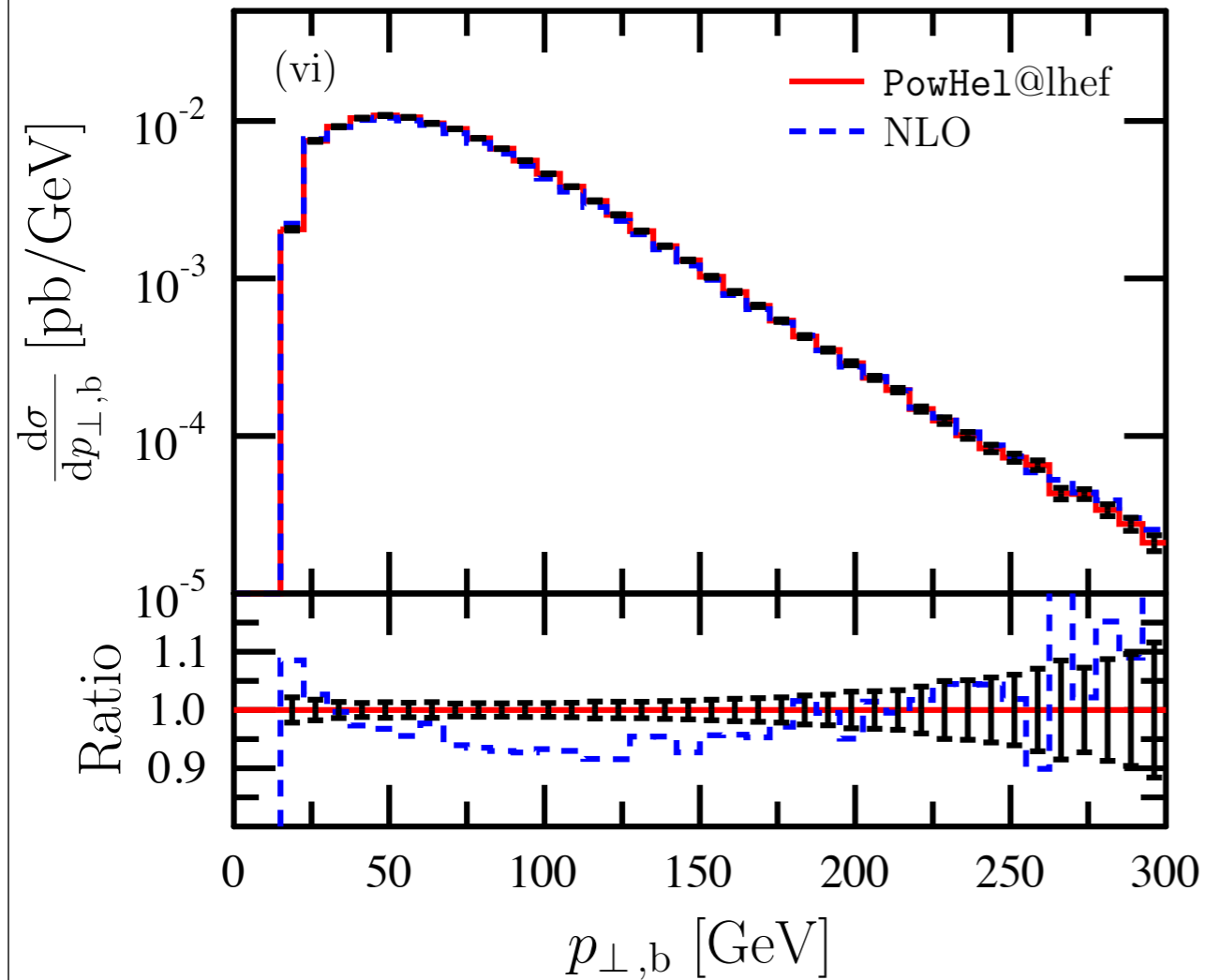
t-tbar + j

- NLO corrections calculated.
Considerably reduced scale dependence
- Implemented in POWHEGBOX
 - NLO + Parton Shower. Public release soon
 - Important for A_{FB} and A_C in t-tbar+jet samples
 - Top quark decay included
 - generate events with stable t-tbar with POWHEG
 - generate decay products using ME for full production and decay
 - reshuffle momenta of t-tbar decay products
 - obtain off-shell t, tbar, W
- New observables:
 - independent measurement of m_t
 - spin-correlations

**t-tbar + j, t-tbar + Z, t-tbar + H/A, W⁺W⁻b-bbar
in POWHEL**

- POWHEL = POWHEG-BOX + HELAC-ILOOP
(NLO + Parton Shower)
- New: HELAC-ILOOP@dd
(more than double precision)
- New: Decay with DECAYER
 - Post-event generation run
 - Spin correlations
 - CPU efficient

$W^+ W^- b \bar{b}$



Transverse momentum and rapidity distribution for the b
at 7TeV LHC

based on the full NLO calculation by
Bevilacqua in [arXiv:1012:4230](https://arxiv.org/abs/1012.4230)