

# Nuclear PDFs

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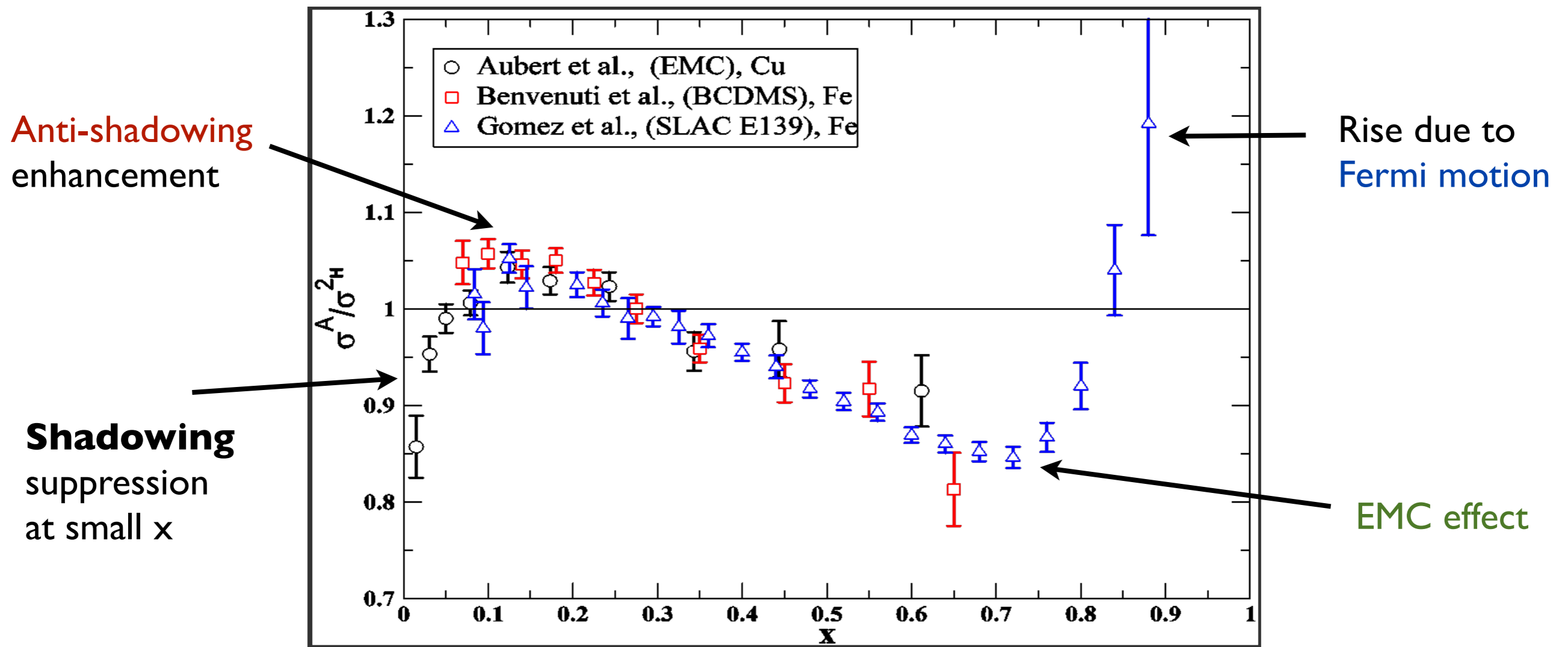
# Outline

- Introduction
- Brief review of available nuclear PDFs
- Vector boson production and the strange PDF
- Wishlist and Conclusions

# Introduction

# Nuclear modifications of DIS structure functions

$$F_2^A(x) \neq ZF_2^p(x) + NF_2^n(x)$$



Can we translate these modifications into **universal nuclear PDFs**?

# Nuclear PDFs

- There are at least two motivations for NPDFs:
  1. They encode **information on the partonic structure** of nuclei
  2. They are **crucial tools** for the description of pA and AA collisions at RHIC/LHC and lepton-A DIS
- Predictions for observables have to include **reliable estimates of the uncertainties** due to the NPDFs
- So far NPDFs are determined by performing **global analyses of data** similar to global analyses of proton PDFs

# Theoretical Framework

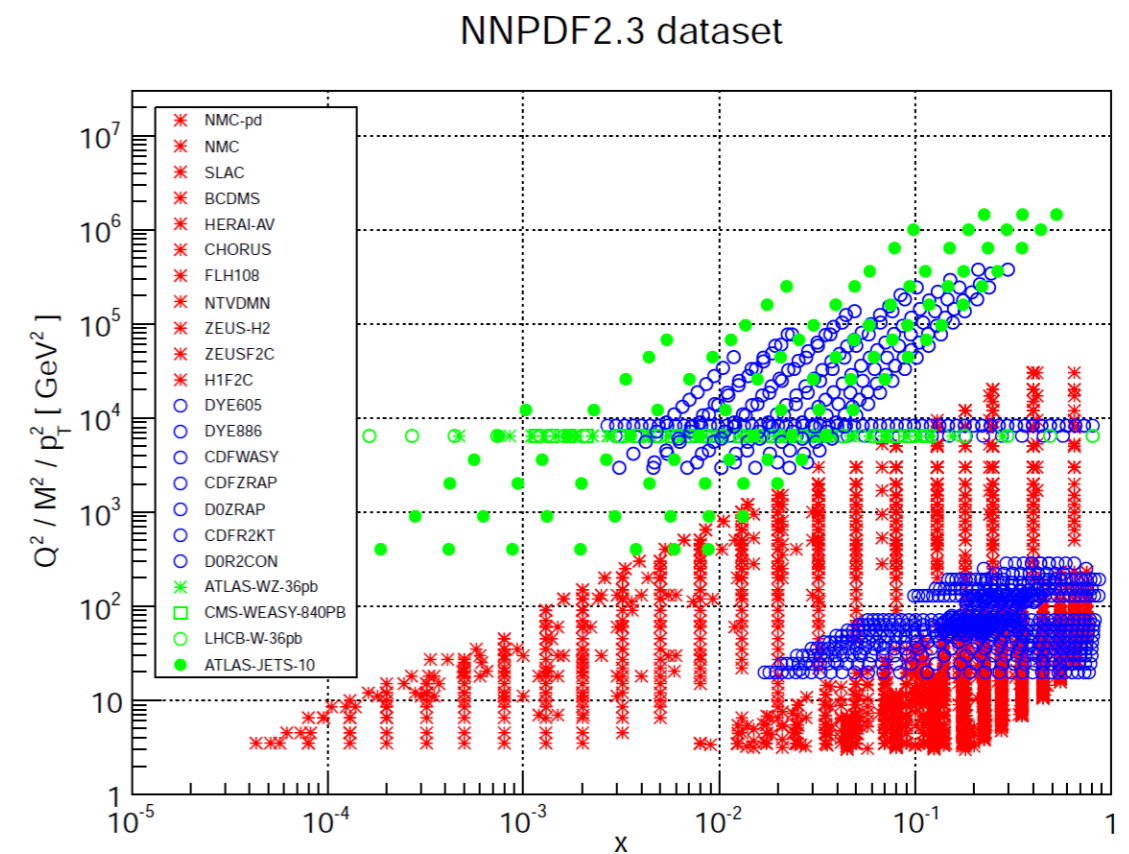
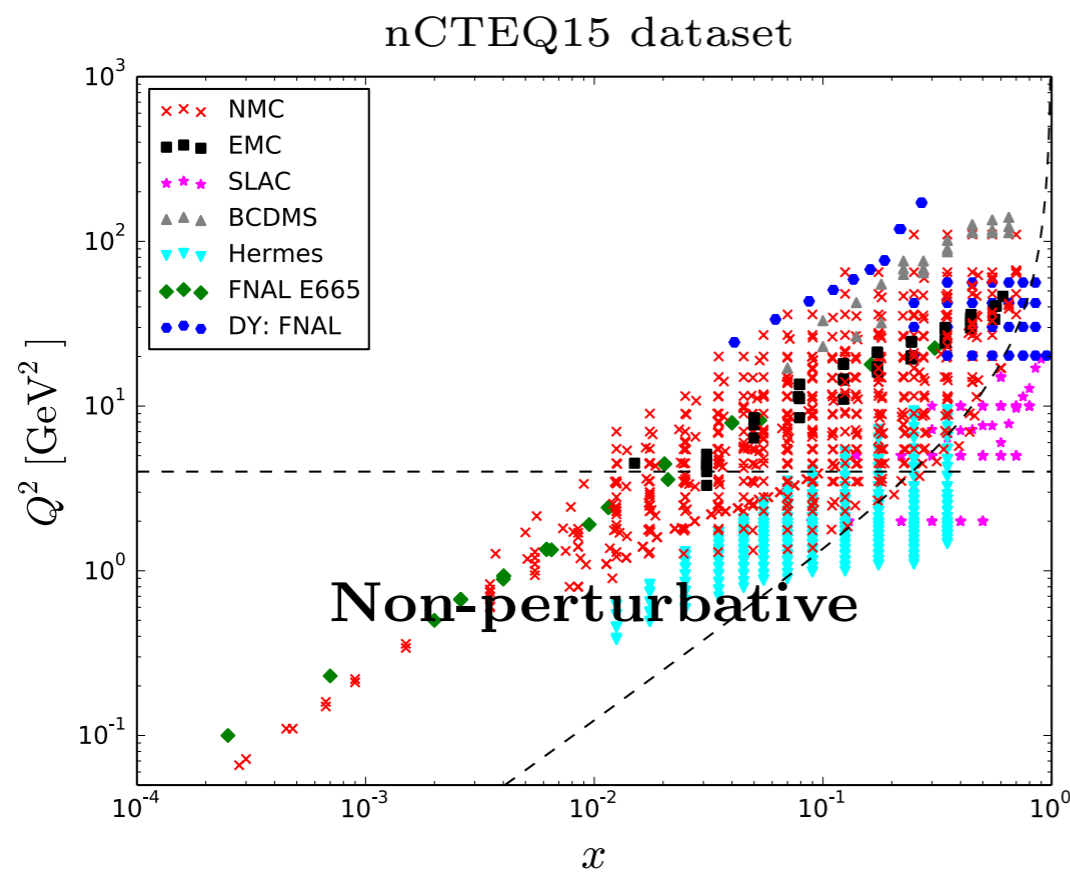
- Factorization theorems
  - provide (field theoretical) **definitions of universal PDFs**
  - make the formalism **predictive**
  - make a statement about the **error**
- **PDFs** and predictions for **observables+uncertainties** **refer to this standard pQCD framework**
- There might be breaking of QCD factorization, deviations from **DGLAP** evolution — in particular in a nuclear environment

**Still need solid understanding of standard framework to establish deviations!**

In the nuclear case, consider factorization as a **working assumption** to be tested phenomenologically

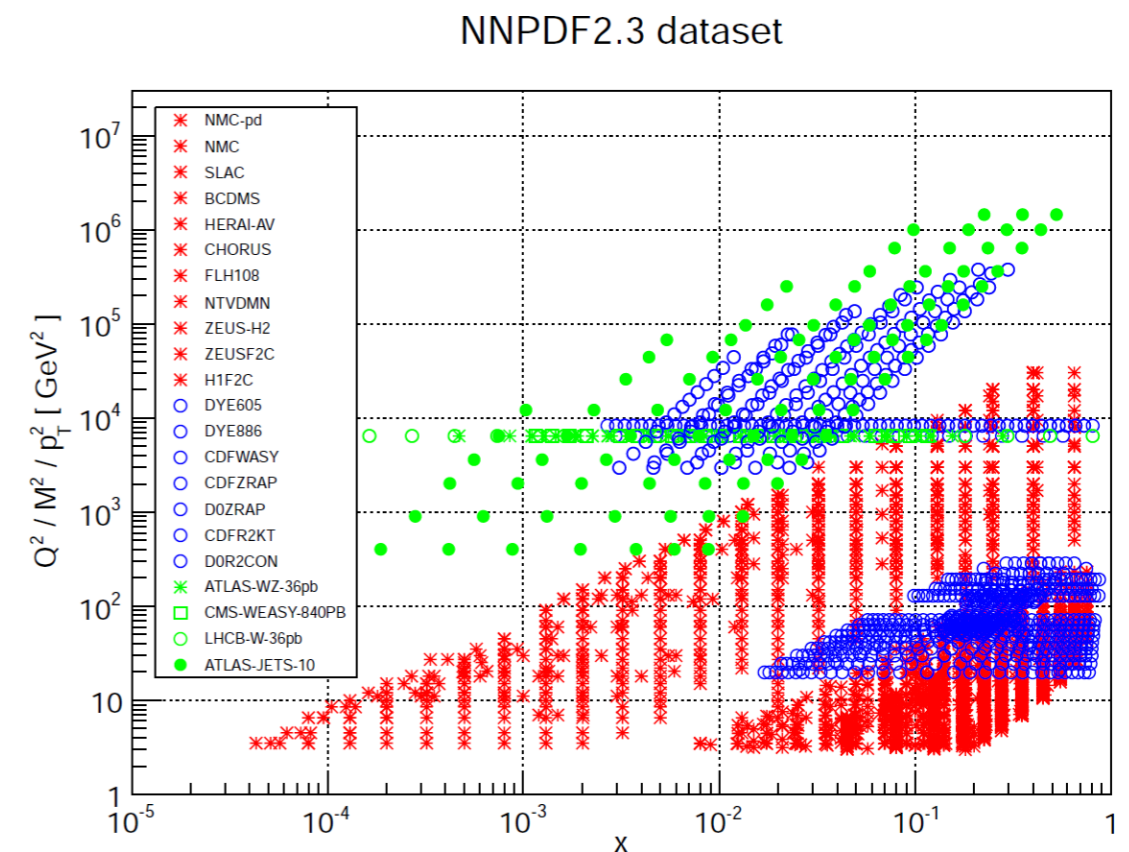
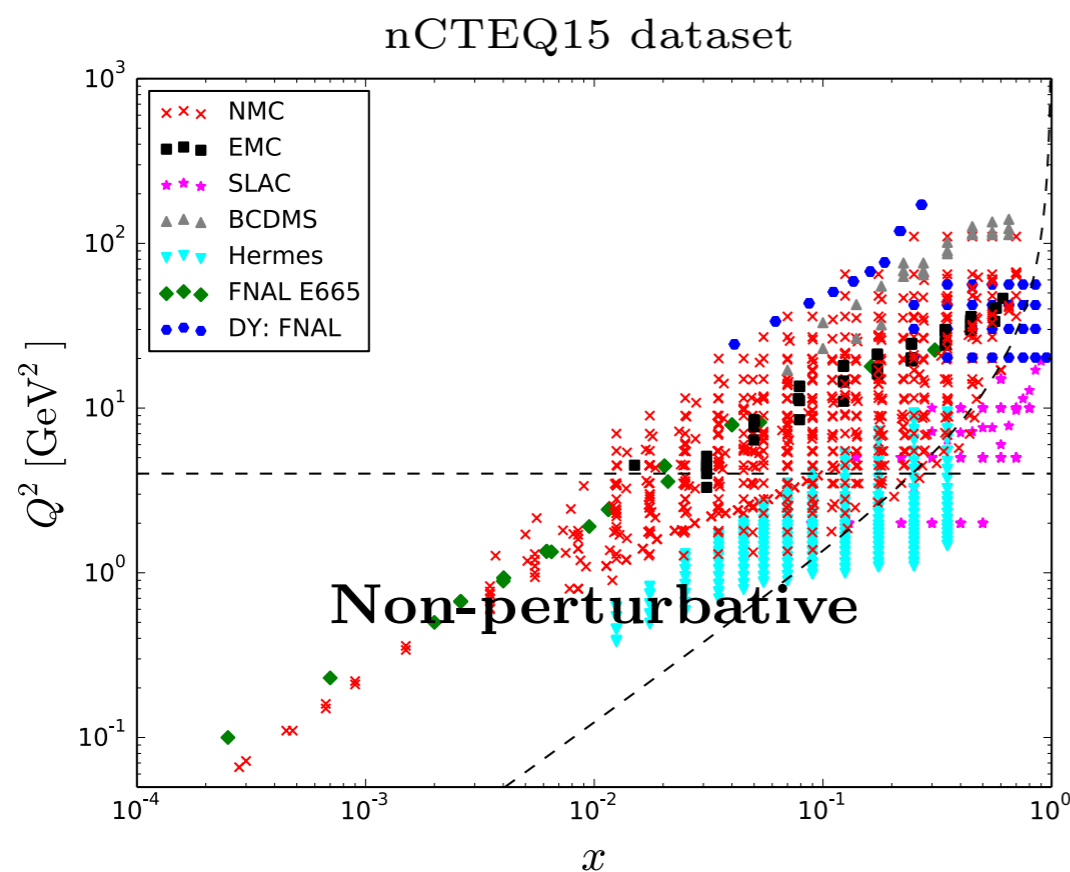
# Main differences with free-proton PDFs

- Theoretical status of factorization
- Parametrization: more parameters to model  $A$ -dependence
- Less data constraints, much(!) smaller kinematic coverage



# Main differences with free-proton PDFs

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- Less data constraints → more **assumptions** about input PDFs
- Assumptions “hide” uncertainties!



# Brief review of available nuclear PDFs

# Available nuclear PDFs (NLO)

- **EPPS'16 (supersedes EPS'09)**

Eskola, Paakkinen, Paukkunen, Salgado, arXiv:1612.0574

**NEW**

- **nCTEQ'15**

nCTEQ collaboration, PRD93(2016)085037, arXiv:1509.00792

- **DSSZ'11**

de Florian, Sassot, Stratmann, Zurita, PRD85(2012)074028, arXiv:1509.00792

- **HKN'07**

Hirai, Kumano, Nagai, PRC76(2007)065207, arXiv:0709.3038

- **AT'12**

Atashbar Tehrani, PRC86(2012)064301

# Available nuclear PDFs (NNLO)

- KA'15

Khanpour, Atashbar Tehrani, PRD93(2016)014026, arXiv:1601.00939

# Main differences

- **Used data sets**

- **charged lepton-nucleus DIS, pA DY**: All groups (but **different cuts!**)  
(EPPS'16 uses also  $\pi$ -A DY data)
- **RHIC single pion production**: EPPS'16, nCTEQ'15, DSSZ'11  
(EPPS now with weight = 1; DSSZ includes nuclear corrections to FFs)
- **neutrino-Pb DIS** (CHORUS): EPPS'16
- **LHC data** (dijet production, W/Z production): EPPS'16

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- **Parametrization**

- Multiplicative nuclear correction factors: EPPS'16, DSSZ'11, HKN'07, AT'12, KA'15  
(requires proton baseline, parametrization can be quite complicated)
- Native nuclear PDFs (same treatment as proton PDFs): nCTEQ'16

# Parametrization

- **Multiplicative nuclear correction factors**

$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A) f_i^{\text{free proton}}(x_N, \mu_0)$$

- **HKN**: Hirai, Kumano, Nagai  
[PRC 76, 065207 (2007), arXiv:0709.3038]
- **EPS**: Eskola, Paukkunen, Salgado  
[JHEP 04 (2009) 065, arXiv:0902.4154]
- **DSSZ**: de Florian, Sassot, Stratmann, Zurita  
[PRD 85, 074028 (2012), arXiv:1112.6324]

- **Native nuclear PDFs**

- nCTEQ [PRD 93, 085037 (2016), arXiv:1509.00792]

$$f_i^{p/A}(x_N, \mu_0) = f_i(x_N, A, \mu_0)$$

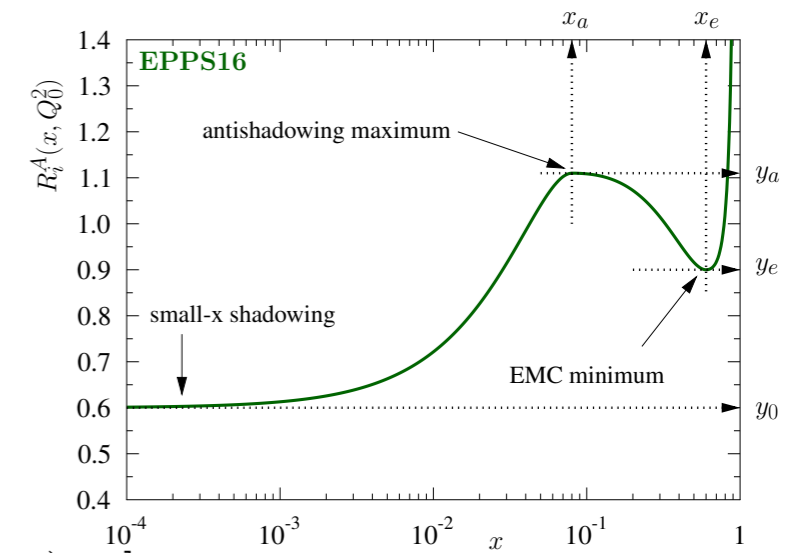
$$f_i(x_N, A = 1, \mu_0) \equiv f_i^{\text{free proton}}(x_N, \mu_0)$$

# EPPS'16 framework

- NLO PDFs with errors (Hessian method,  $\Delta\chi^2 = 52$ )
- Parametrization ( $x_N < 1$ ,  $Q_0 = 1.3$  GeV,  $i = u_v, d_v, \text{ubar}, \text{dbar}, s, g$ )

$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A, Z) f_i(x_N, \mu_0),$$

$$R_i(x, A, Z) = \begin{cases} a_0 + (a_1 + a_2 x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x)(1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$

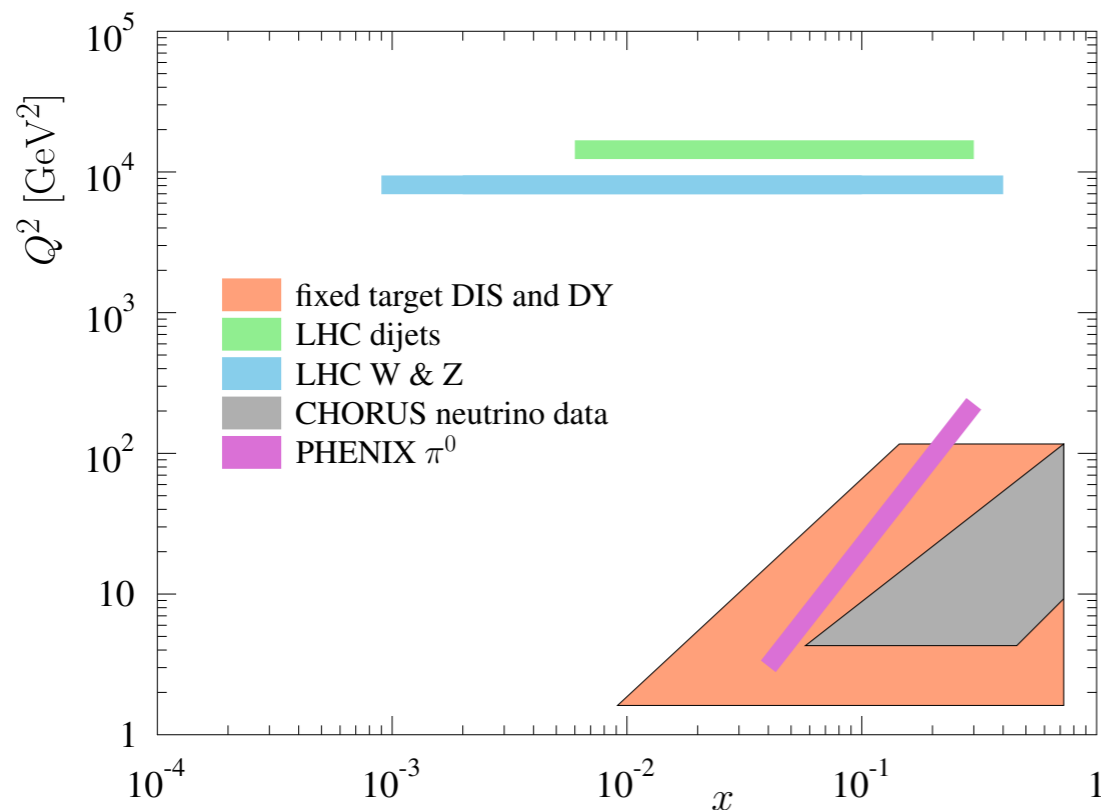


A-dependence of fit parameters:  $y_i(A) = y_i(A_{\text{ref}}) \left( \frac{A}{A_{\text{ref}}} \right)^{\gamma_i [y_i(A_{\text{ref}}) - 1]}$

- CT14NLO free proton baseline, D ( $A=2$ ) taken as free
- Data: IA DIS, DY, nu-A DIS,  $\pi^0$ @RHIC, LHC:dijets, W/Z

# EPPS'16 framework: Data

- DIS cut:  $Q > 1.3 \text{ GeV}$
- No cut on  $W$
- Underlying assumption: structure function ratios less sensitive to higher twist and TMC



**Fig. 2** The approximate regions in the  $(x, Q^2)$  plane at which different data in the EPPS16 fit probe the nuclear PDFs.

Experiment	Observable	Collisions	Data points	$\chi^2$
SLAC E139	DIS	$e^- \text{He}(4), e^- \text{D}$	21	12.2
CERN NMC 95, re.	DIS	$\mu^- \text{He}(4), \mu^- \text{D}$	16	18.0
CERN NMC 95	DIS	$\mu^- \text{Li}(6), \mu^- \text{D}$	15	18.4
CERN NMC 95, $Q^2$ dep.	DIS	$\mu^- \text{Li}(6), \mu^- \text{D}$	153	161.2
SLAC E139	DIS	$e^- \text{Be}(9), e^- \text{D}$	20	12.9
CERN NMC 96	DIS	$\mu^- \text{Be}(9), \mu^- \text{C}$	15	4.4
SLAC E139	DIS	$e^- \text{C}(12), e^- \text{D}$	7	6.4
CERN NMC 95	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	15	9.0
CERN NMC 95, $Q^2$ dep.	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	165	133.6
CERN NMC 95, re.	DIS	$\mu^- \text{C}(12), \mu^- \text{D}$	16	16.7
CERN NMC 95, re.	DIS	$\mu^- \text{C}(12), \mu^- \text{Li}(6)$	20	27.9
FNAL E772	DY	$p\text{C}(12), p\text{D}$	9	11.3
SLAC E139	DIS	$e^- \text{Al}(27), e^- \text{D}$	20	13.7
CERN NMC 96	DIS	$\mu^- \text{Al}(27), \mu^- \text{C}(12)$	15	5.6
SLAC E139	DIS	$e^- \text{Ca}(40), e^- \text{D}$	7	4.8
FNAL E772	DY	$p\text{Ca}(40), p\text{D}$	9	3.33
CERN NMC 95, re.	DIS	$\mu^- \text{Ca}(40), \mu^- \text{D}$	15	27.6
CERN NMC 95, re.	DIS	$\mu^- \text{Ca}(40), \mu^- \text{Li}(6)$	20	19.5
CERN NMC 96	DIS	$\mu^- \text{Ca}(40), \mu^- \text{C}(12)$	15	6.4
SLAC E139	DIS	$e^- \text{Fe}(56), e^- \text{D}$	26	22.6
FNAL E772	DY	$e^- \text{Fe}(56), e^- \text{D}$	9	3.0
CERN NMC 96	DIS	$\mu^- \text{Fe}(56), \mu^- \text{C}(12)$	15	10.8
FNAL E866	DY	$p\text{Fe}(56), p\text{Be}(9)$	28	20.1
CERN EMC	DIS	$\mu^- \text{Cu}(64), \mu^- \text{D}$	19	15.4
SLAC E139	DIS	$e^- \text{Ag}(108), e^- \text{D}$	7	8.0
CERN NMC 96	DIS	$\mu^- \text{Sn}(117), \mu^- \text{C}(12)$	15	12.5
CERN NMC 96, $Q^2$ dep.	DIS	$\mu^- \text{Sn}(117), \mu^- \text{C}(12)$	144	87.6
FNAL E772	DY	$p\text{W}(184), p\text{D}$	9	7.2
FNAL E866	DY	$p\text{W}(184), p\text{Be}(9)$	28	26.1
CERN NA10*	DY	$\pi^- \text{W}(184), \pi^- \text{D}$	10	11.6
FNAL E615*	DY	$\pi^+ \text{W}(184), \pi^- \text{W}(184)$	11	10.2
CERN NA3*	DY	$\pi^- \text{Pt}(195), \pi^- \text{H}$	7	4.6
SLAC E139	DIS	$e^- \text{Au}(197), e^- \text{D}$	21	8.4
RHIC PHENIX	$\pi^0$	$d\text{Au}(197), pp$	20	6.9
CERN NMC 96	DIS	$\mu^- \text{Pb}(207), \mu^- \text{C}(12)$	15	4.1
CERN CMS*	$W^\pm$	$p\text{Pb}(208)$	10	8.8
CERN CMS*	Z	$p\text{Pb}(208)$	6	5.8
CERN ATLAS*	Z	$p\text{Pb}(208)$	7	9.6
CERN CMS*	dijet	$p\text{Pb}(208)$	7	5.5
CERN CHORUS*	DIS	$\nu\text{Pb}(208), \bar{\nu}\text{Pb}(208)$	824	998.6
Total			1811	1789



# EPPS'16 framework: Results

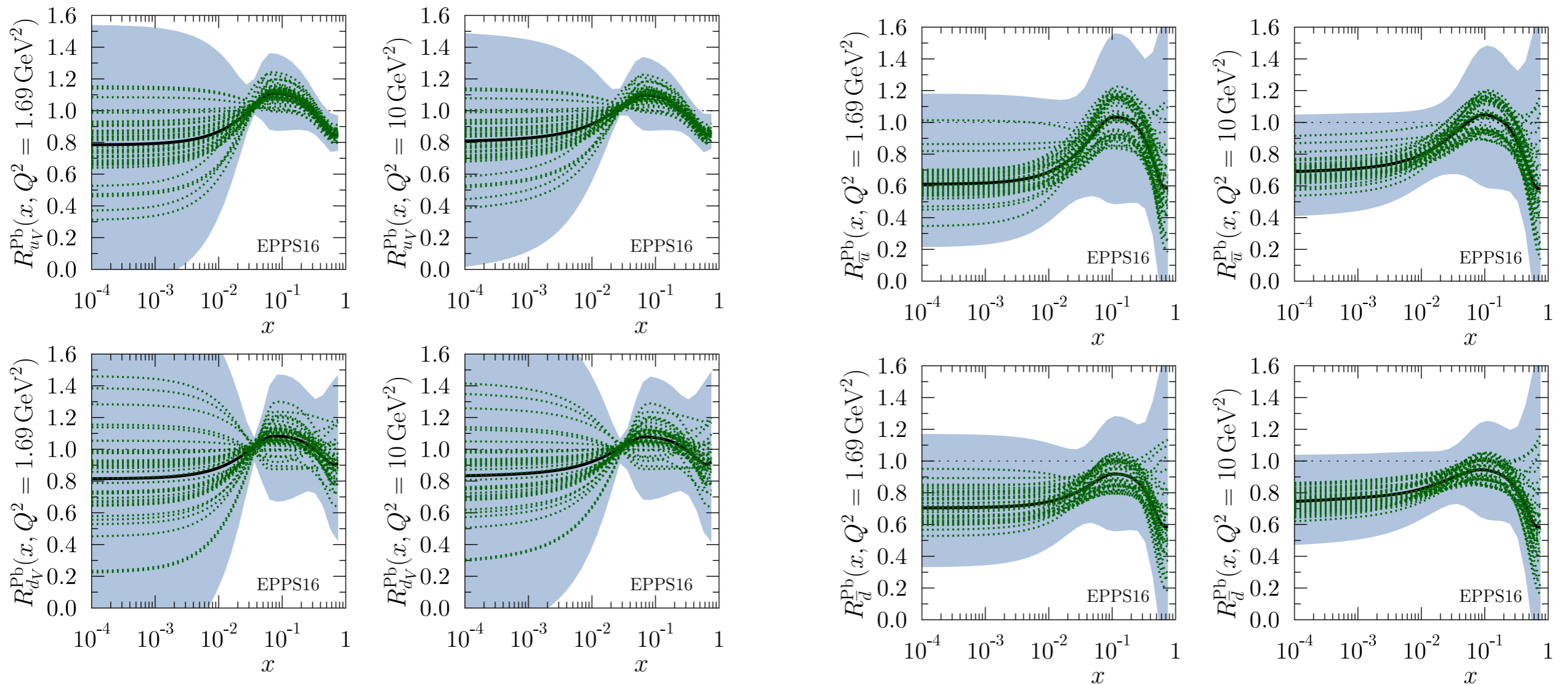
**Table 3** List of parameters defining the central set of EPPS16 at the initial scale  $Q_0^2 = 1.69 \text{ GeV}^2$ . The numbers in bold indicate the 20 parameters that were free in the fit.

Parameter	$u_V$	$d_V$	$\bar{u}$
$y_0(A_{\text{ref}})$	sum rule	sum rule	<b>0.844</b>
$\gamma_{y_0}$	sum rule	sum rule	<b>0.731</b>
$x_a$	<b>0.0717</b>	as $u_V$	<b>0.104</b>
$x_e$	<b>0.693</b>	as $u_V$	as $u_V$
$y_a(A_{\text{ref}})$	<b>1.06</b>	<b>1.05</b>	<b>1.03</b>
$\gamma_{y_a}$	<b>0.278</b>	as $u_V$	0, fixed
$y_e(A_{\text{ref}})$	<b>0.908</b>	<b>0.943</b>	<b>0.725</b>
$\gamma_{y_e}$	<b>0.288</b>	as $u_V$	as $u_V$
$\beta$	1.3, fixed	1.3, fixed	1.3, fixed

Parameter	$\bar{d}$	$s$	$g$
$y_0(A_{\text{ref}})$	<b>0.889</b>	<b>0.723</b>	sum rule
$\gamma_{y_0}$	as $\bar{u}$	as $\bar{u}$	sum rule
$x_a$	as $\bar{u}$	as $\bar{u}$	<b>0.0820</b>
$x_e$	as $u_V$	as $u_V$	as $u_V$
$y_a(A_{\text{ref}})$	<b>0.919</b>	<b>1.24</b>	<b>1.12</b>
$\gamma_{y_a}$	0, fixed	0, fixed	as $u_V$
$y_e(A_{\text{ref}})$	as $\bar{u}$	as $\bar{u}$	<b>0.874</b>
$\gamma_{y_e}$	as $u_V$	as $u_V$	as $u_V$
$\beta$	1.3, fixed	1.3, fixed	1.3, fixed

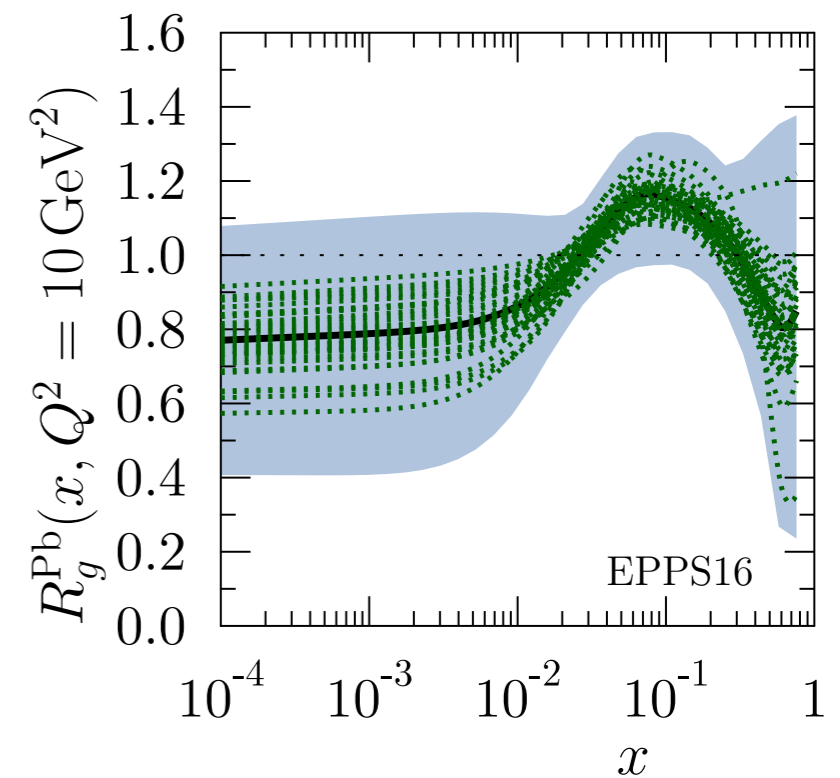
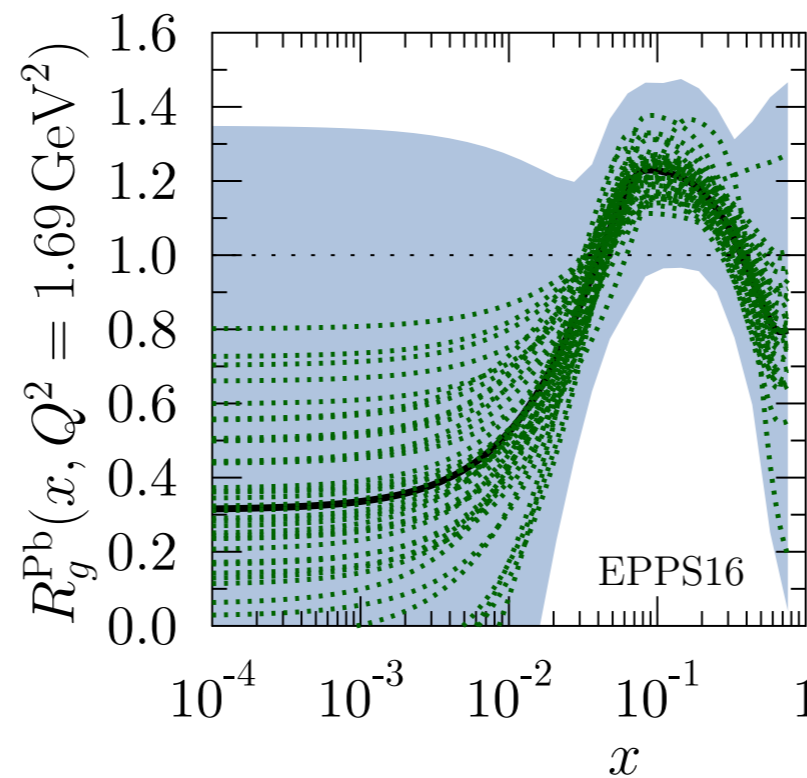
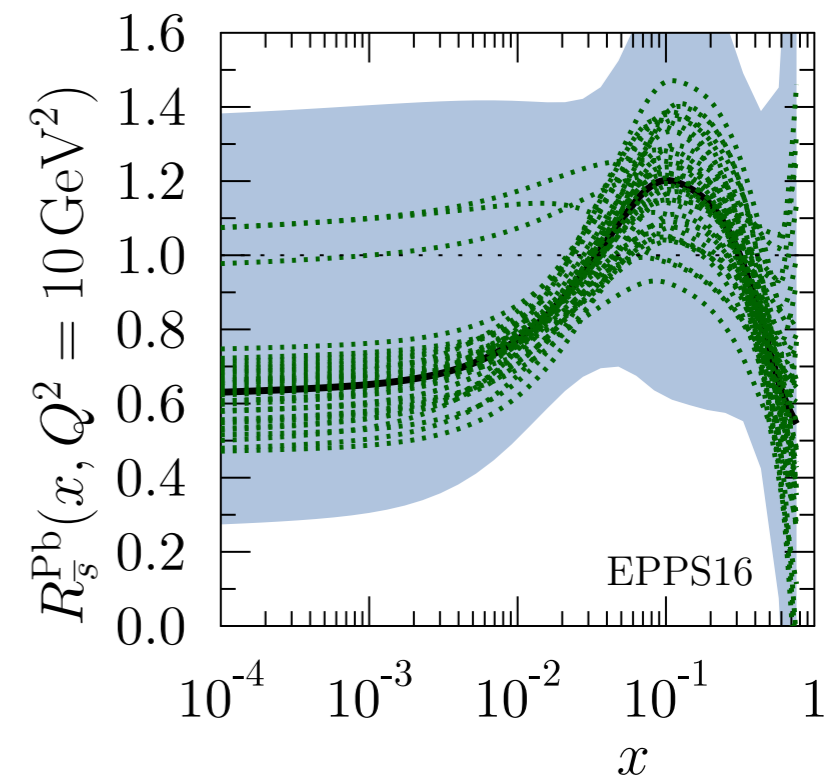
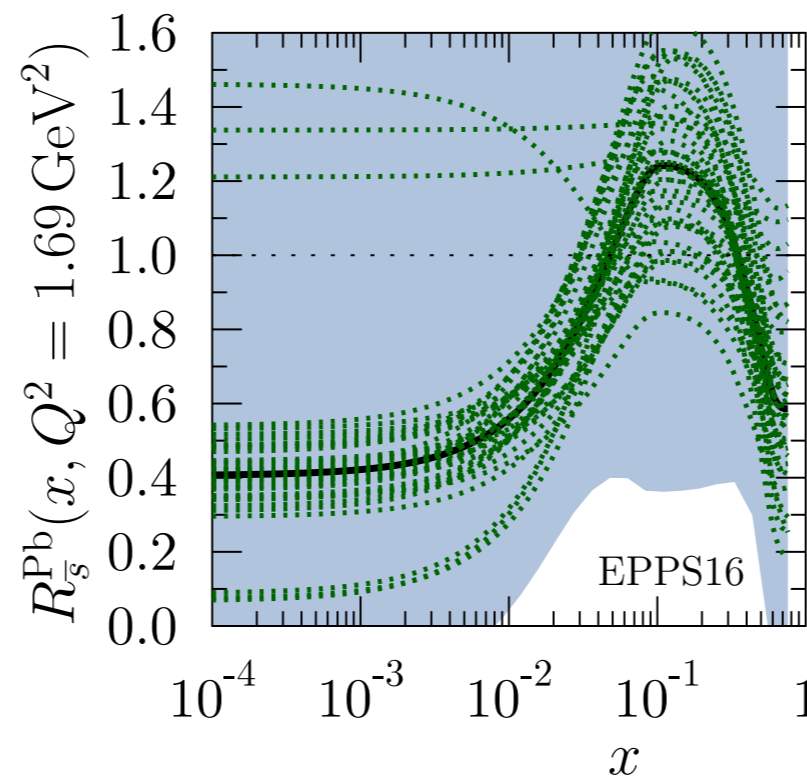
# EPPS'16 framework: Results



- Considerably larger uncertainties than EPS'09 despite more data (more flexible param., larger tolerance). Main impact from CHORUS and CMS dijet data.
- No notable tensions with previous data sets. **Supports validity of theoretical framework!**
- Still some parametrization bias (shape of PDFs), still quite a number of assumptions on parametrization
- Some aggressive choices (low DIS cuts,  $\pi$ -A DY data, RHIC  $\pi^0$  data)

# EPPS'16 framework: Results

- Large uncertainties for nuclear gluon distribution
- Nuclear strange PDF poorly constrained
- Clearly more LHC pPb data required
  - from LHC5
  - from LHC8 (much higher statistics)



- Functional form of the **bound proton PDF** same as for the free proton (CTEQ6M,  $x$  restricted to  $0 < x < 1$ )

$$x f_i^{p/A}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}, \quad i = u_v, d_v, g, \dots$$

$$\bar{d}(x, Q_0)/\bar{u}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} + (1 + c_3 x)(1-x)^{c_4}$$

- $A$ -dependent fit parameters (reduces to free proton for  $A = 1$ )

$$c_k \rightarrow c_k(A) \equiv c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}}), \quad k = \{1, \dots, 5\}$$

- PDFs for nucleus ( $A, Z$ )

$$f_i^{(A,Z)}(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{A-Z}{A} f_i^{n/A}(x, Q)$$

(bound neutron PDF  $f_i^{n/A}$  by isospin symmetry)

# nCTEQ'15 framework: Data sets

- NC DIS & DY

**CERN BCDMS & EMC & NMC**

$N = (\text{D, Al, Be, C, Ca, Cu, Fe, Li, Pb, Sn, W})$

**FNAL E-665**

$N = (\text{D, C, Ca, Pb, Xe})$

**DESY Hermes**

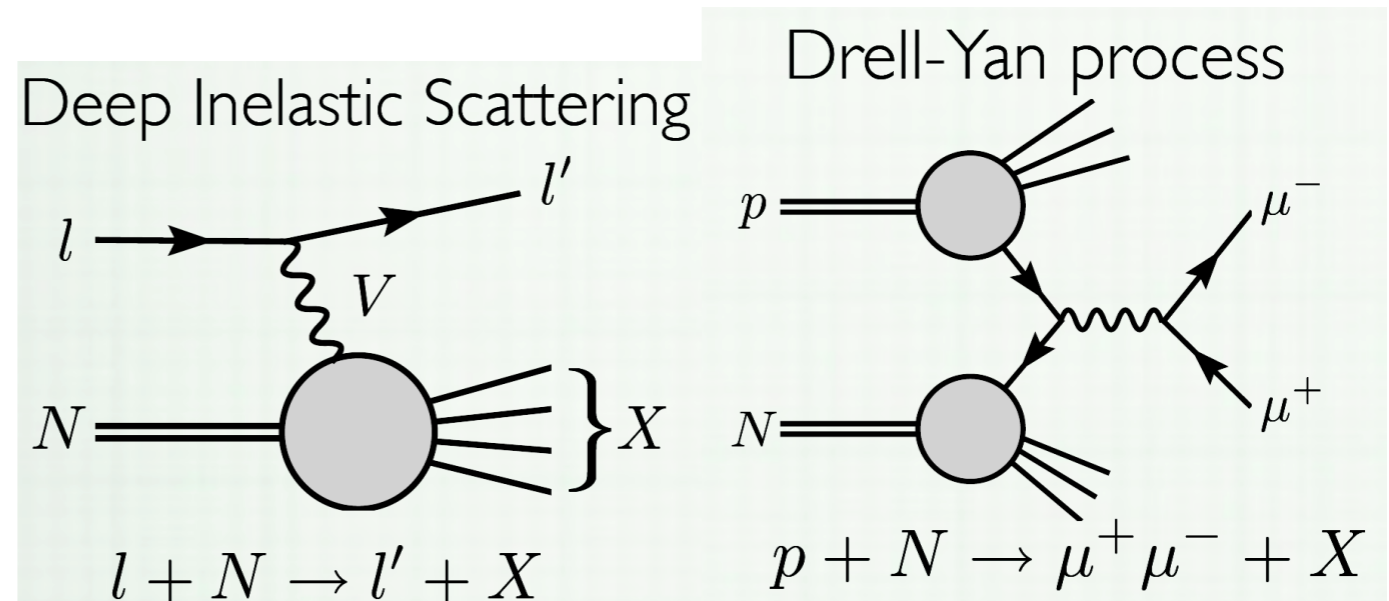
$N = (\text{D, He, N, Kr})$

**SLAC E-139 & E-049**

$N = (\text{D, Ag, Al, Au, Be, C, Ca, Fe, He})$

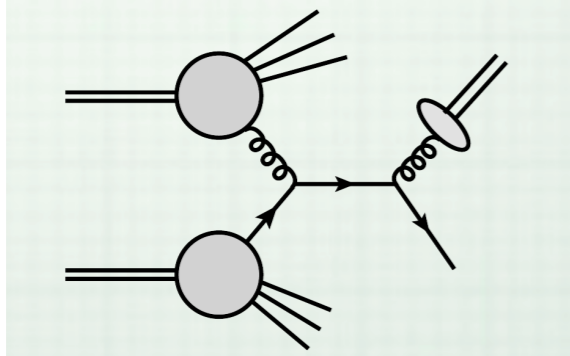
**FNAL E-772 & E-886**

$N = (\text{D, C, Ca, Fe, W})$



- Single pion production (new)

*Single pion production*

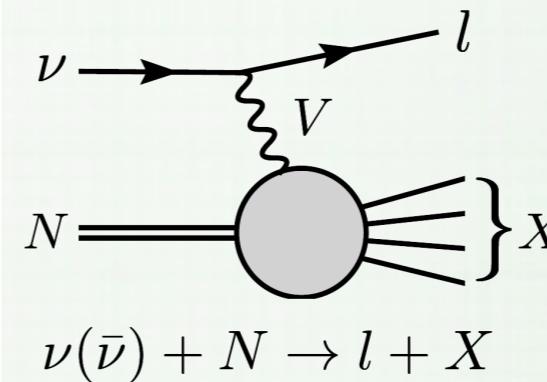


**RHIC - PHENIX & STAR**

$N = \text{Au}$

- Neutrino (to be included later)

Deep Inelastic Scattering



**CHORUS CCFR & NuTeV**

$N = \text{Pb } N = \text{Fe}$

## Fit properties:

- fit @NLO
- $Q_0 = 1.3\text{GeV}$
- using ACOT heavy quark scheme
- kinematic cuts:  
 $Q > 2\text{GeV}$ ,  $W > 3.5\text{GeV}$   
 $p_T > 1.7\text{ GeV}$
- 708 (DIS & DY) + 32 (single  $\pi^0$ )  
= 740 data points after cuts
- 16+2 free parameters
  - 7 gluon
  - 7 valence
  - 2 sea
  - 2 pion data normalizations
- $\chi^2 = 587$ , giving  $\chi^2/\text{dof} = 0.81$

## Error analysis:

- use Hessian method

$$\chi^2 = \chi_0^2 + \frac{1}{2} H_{ij} (a_i - a_i^0) (a_j - a_j^0)$$

$$H_{ij} = \frac{\partial^2 \chi^2}{\partial a_i \partial a_j}$$

- tolerance  $\Delta\chi^2 = 35$  (every nuclear target within 90% C.L.)
- eigenvalues span 10 orders of magnitude  $\rightarrow$  require numerical precision
- use noise reducing derivatives

Fit properties

- fit @M
- $Q_0 =$
- using
- kinem
- $Q > 2$
- $p_T >$
- 708 (1
- = 740
- 16+2
- 
- 
- 
- $\chi^2 =$

## Kinematic cuts

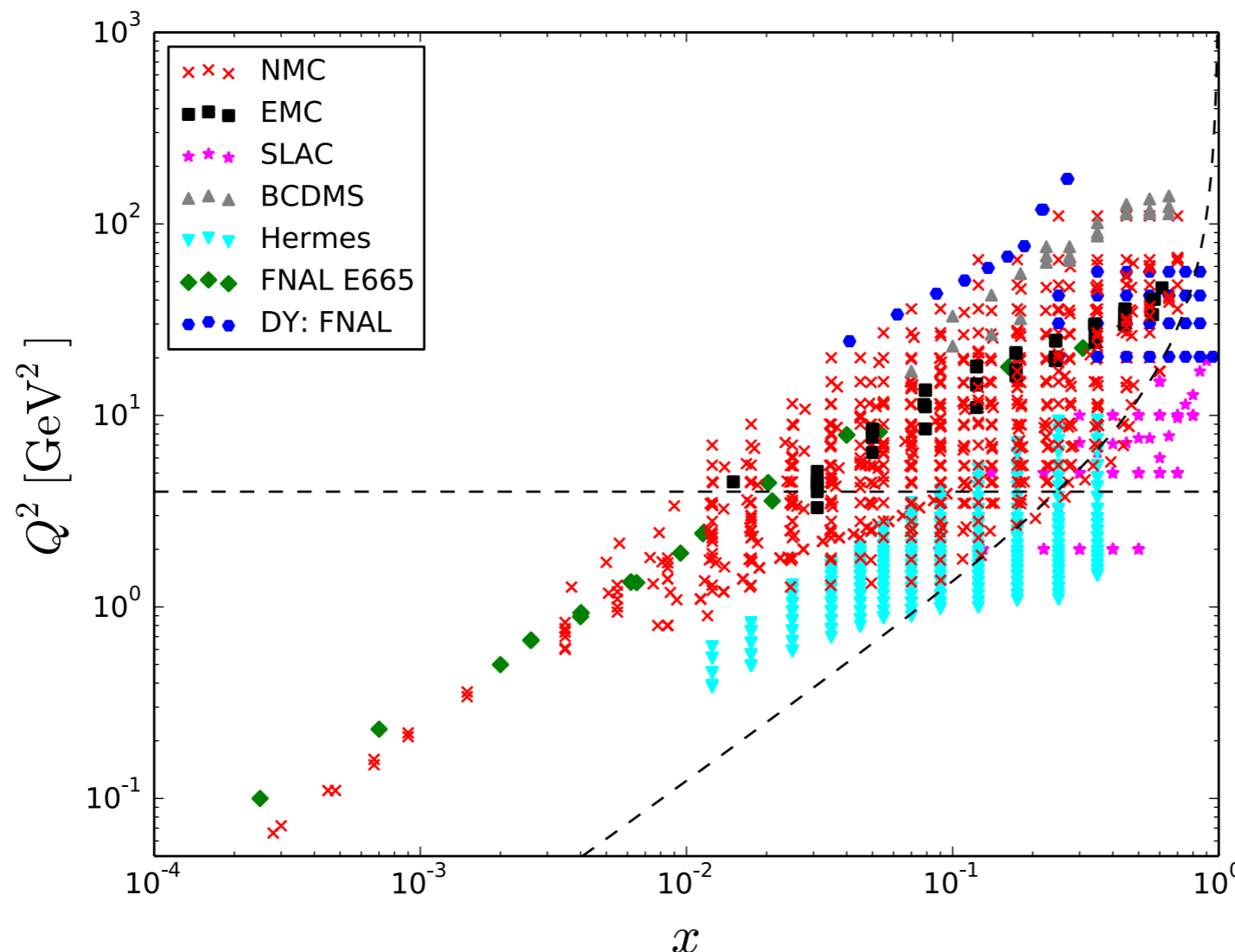
nCTEQ:

$$\begin{cases} Q > 2 \text{ GeV} \\ W > 3.5 \text{ GeV} \end{cases}$$

EPS:  $Q > 1.3 \text{ GeV}$

HKN:  $Q > 1 \text{ GeV}$

DSSZ:  $Q > 1 \text{ GeV}$



$\Delta\chi^2 = 35$  (every  
target within 90% C.L.)

es span 10 orders of  
le  $\rightarrow$  require numerical

**nCTEQ: 740** data points  
reducing derivatives  
**EPS09: 929** data points

Fit properties:

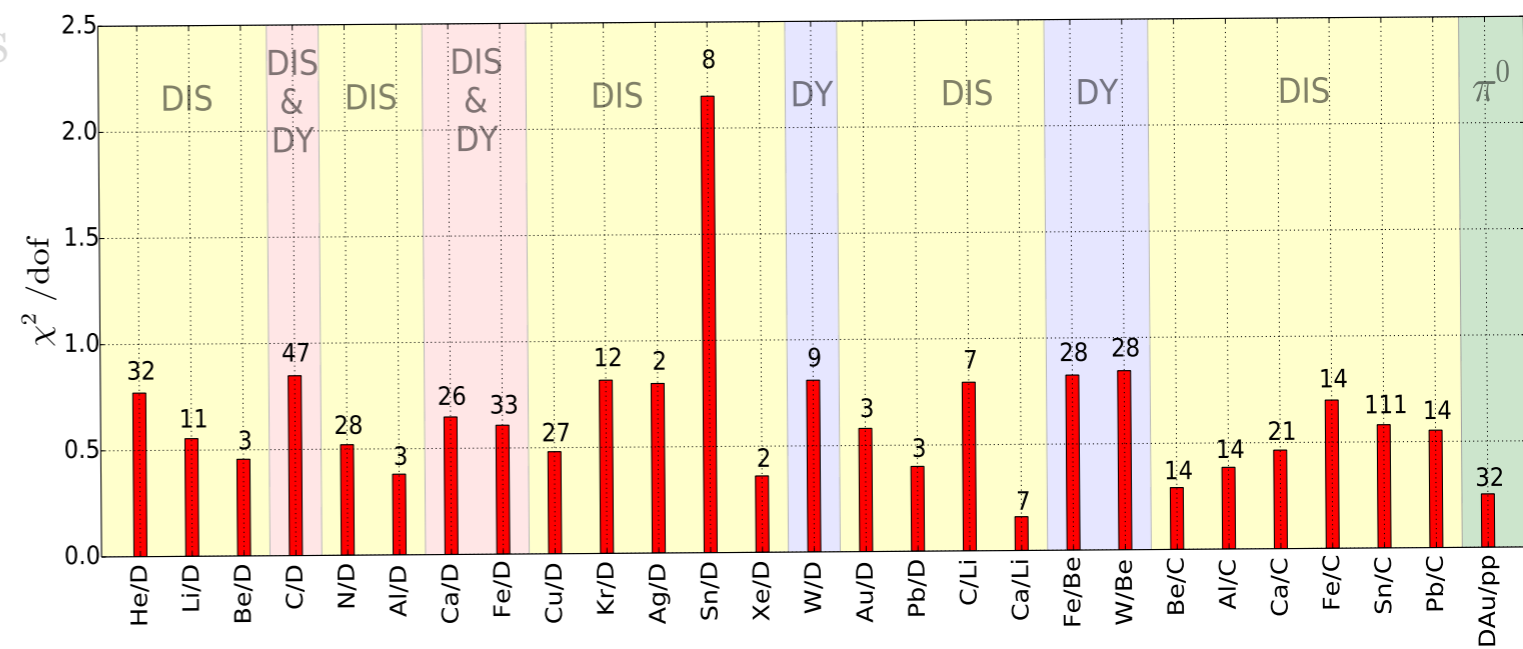
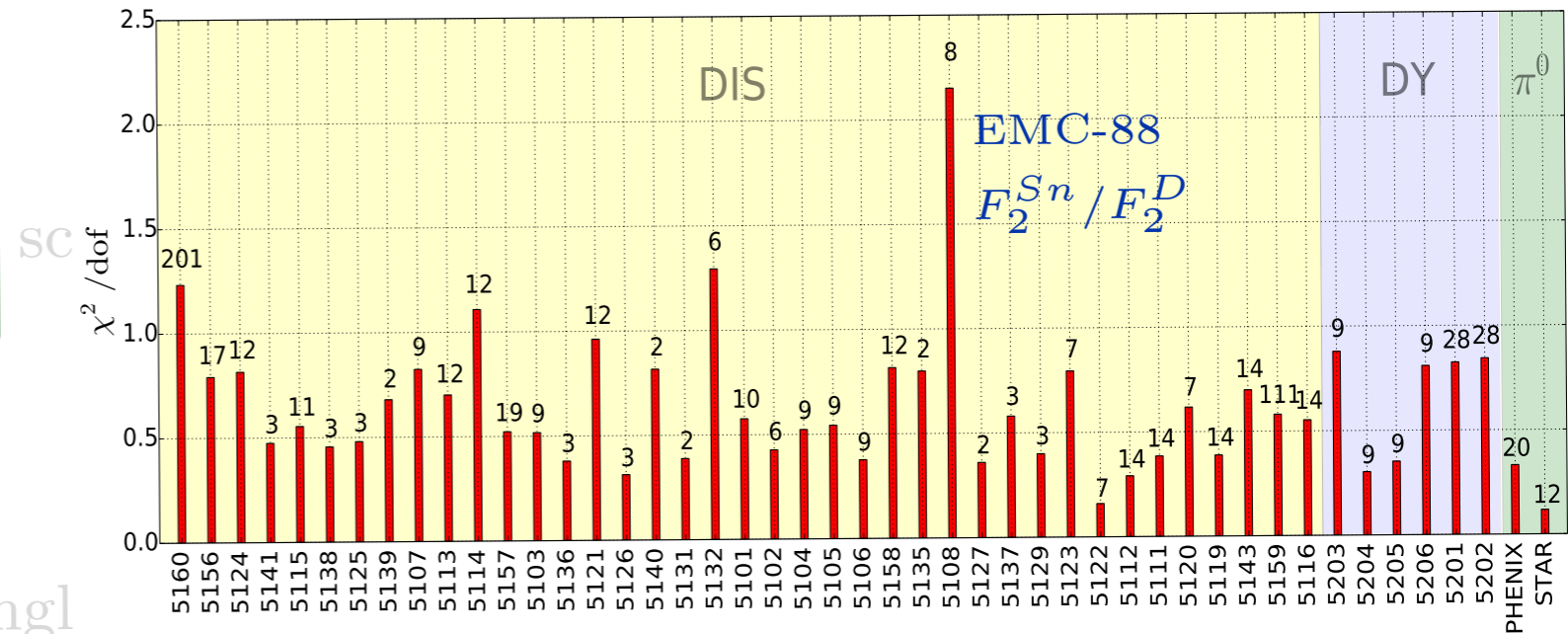
Error analysis:

## Fit quality

- $\chi^2/dof = 0.81$

$Q > 2\text{GeV}, W > 3.5\text{GeV}$   
 $p_T > 1.7\text{ GeV}$

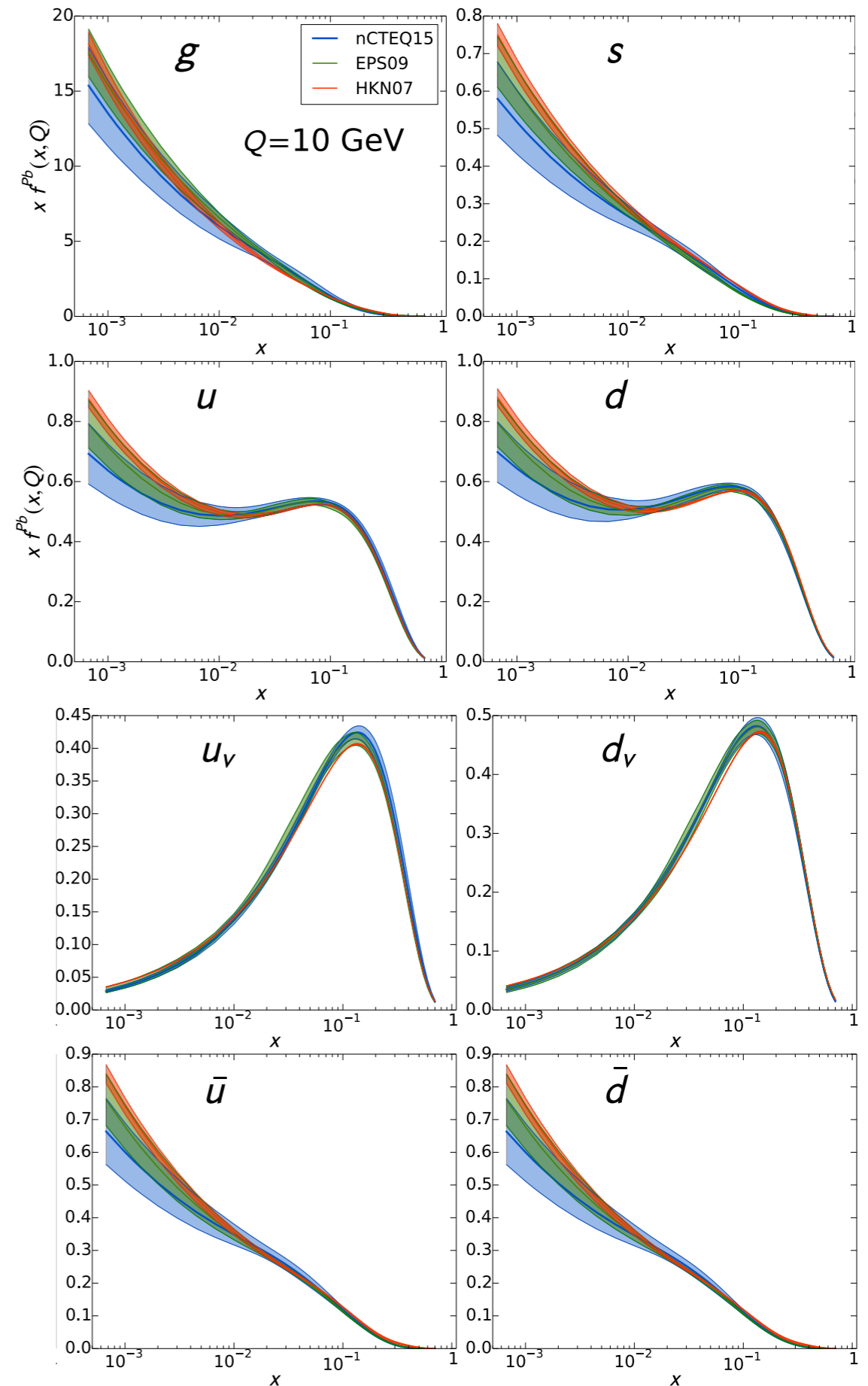
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- 16+2 free parameters
  - 7 gluon
  - 7 valence
  - 2 sea
  - 2 pion data normalizations
- $\chi^2 = 587$ , giving  $\chi^2/dof = 0.81$





# nCTEQ results

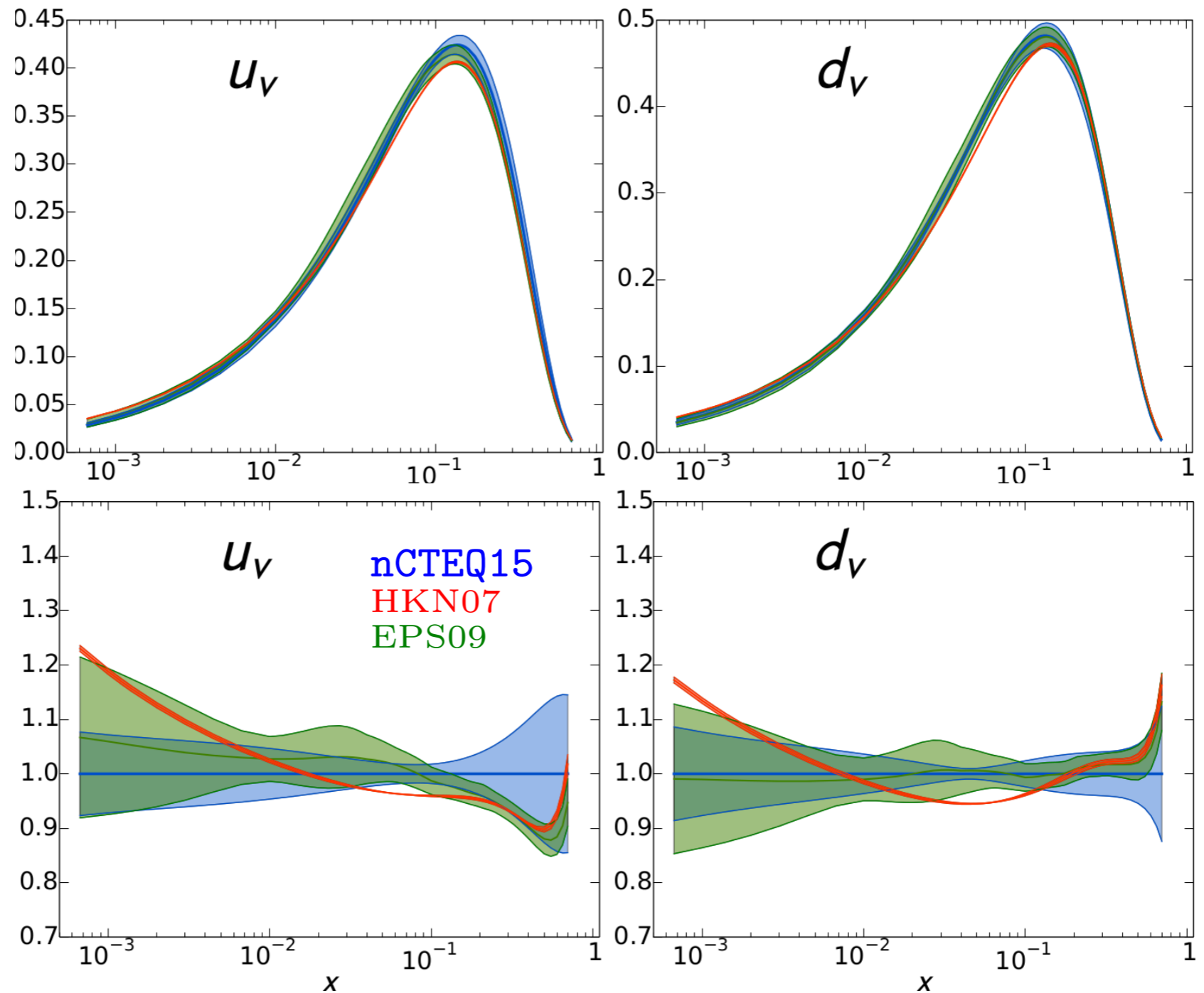
- First global analysis with Hessian error PDFs: [PRD93(2016)085037]
- Figure: PDFs inside lead at  $Q=10$  GeV vs  $x$
- nCTEQ features larger uncertainties than previous nPDFs
- better agreement between different groups



# Valence distributions

Full lead nucleus distribution:

$$f^{Pb} = \frac{82}{208} f^{p/Pb} + \frac{208 - 82}{208} f^{n/Pb}$$



# DSSZ'11 framework

- ▶ NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ( $Q_0=1\text{GeV}$ )

$$f_i^{p/A}(x_N, Q_0) = R_i^A(x_N, Q_0) f_i^p(x_N, Q_0), \quad i = \text{valence, sea, } g$$

$$R_v^A(x, Q_0) = \epsilon_1 x^{\alpha_1} (1-x)^{\beta_1} \left[ 1 + \epsilon_2 (1-x)^{\beta_2} \right] \left[ 1 + a_v (1-x)^{\beta_3} \right]$$

$$R_s^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_s}{\epsilon_1} \frac{1 + a_s x^{\alpha_s}}{1 + a_s}$$

$$R_g^A(x, Q_0) = R_v^A(x, Q_0) \frac{\epsilon_g}{\epsilon_1} \frac{1 + a_g x^{\alpha_g}}{1 + a_g}$$

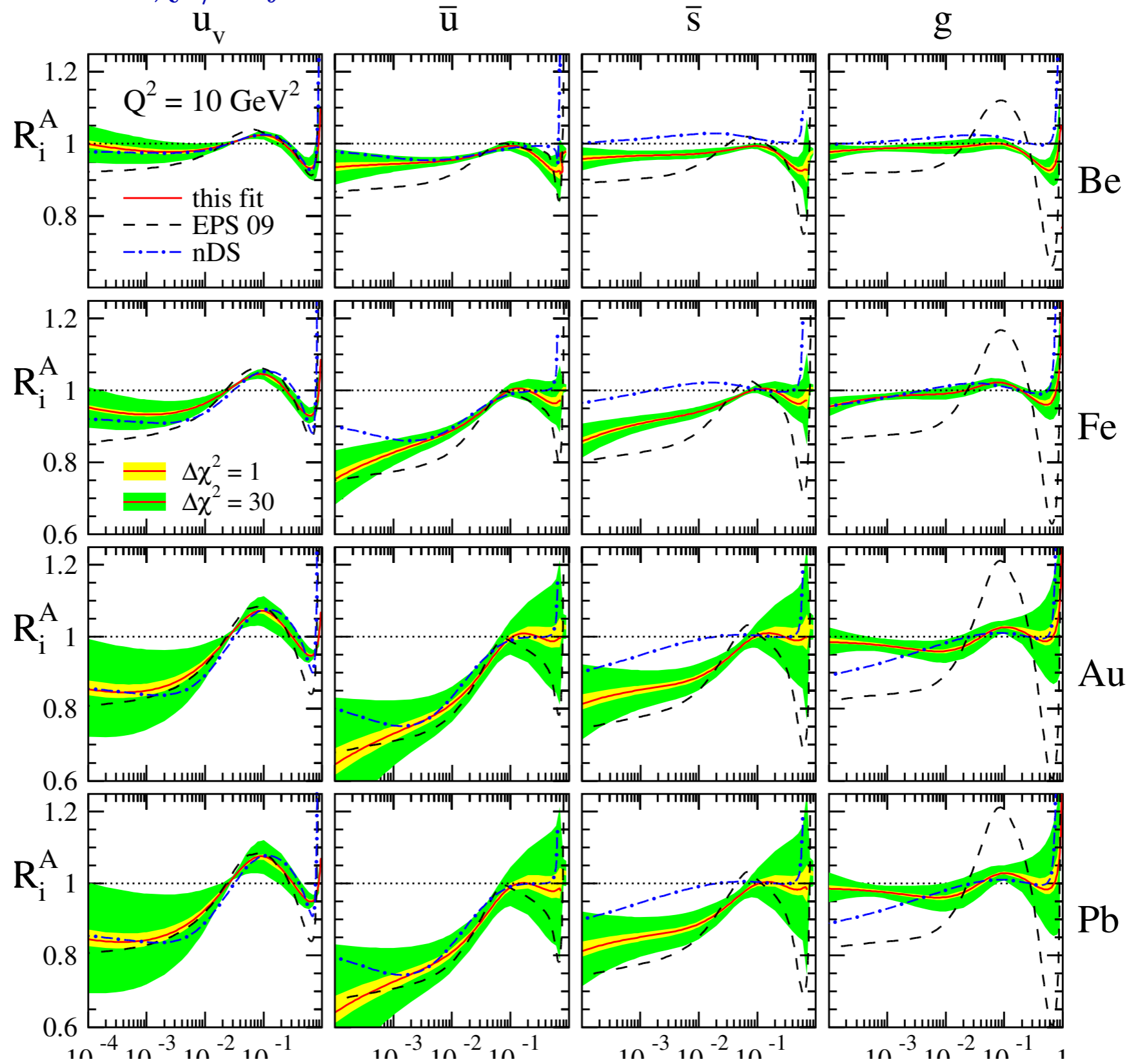
A-dependence of fitting parameters ( $\xi = \alpha_v, \alpha_s, \dots$ )

$$\xi = \gamma_\xi + \lambda_\xi A^{\delta_\xi}$$

- ▶ MSTW 2008 free proton baseline
- ▶ Neglects  $x_N > 1$
- ▶ Data: DIS, DY,  $\pi^{0\pm}$  @ RHIC, Neutrino DIS

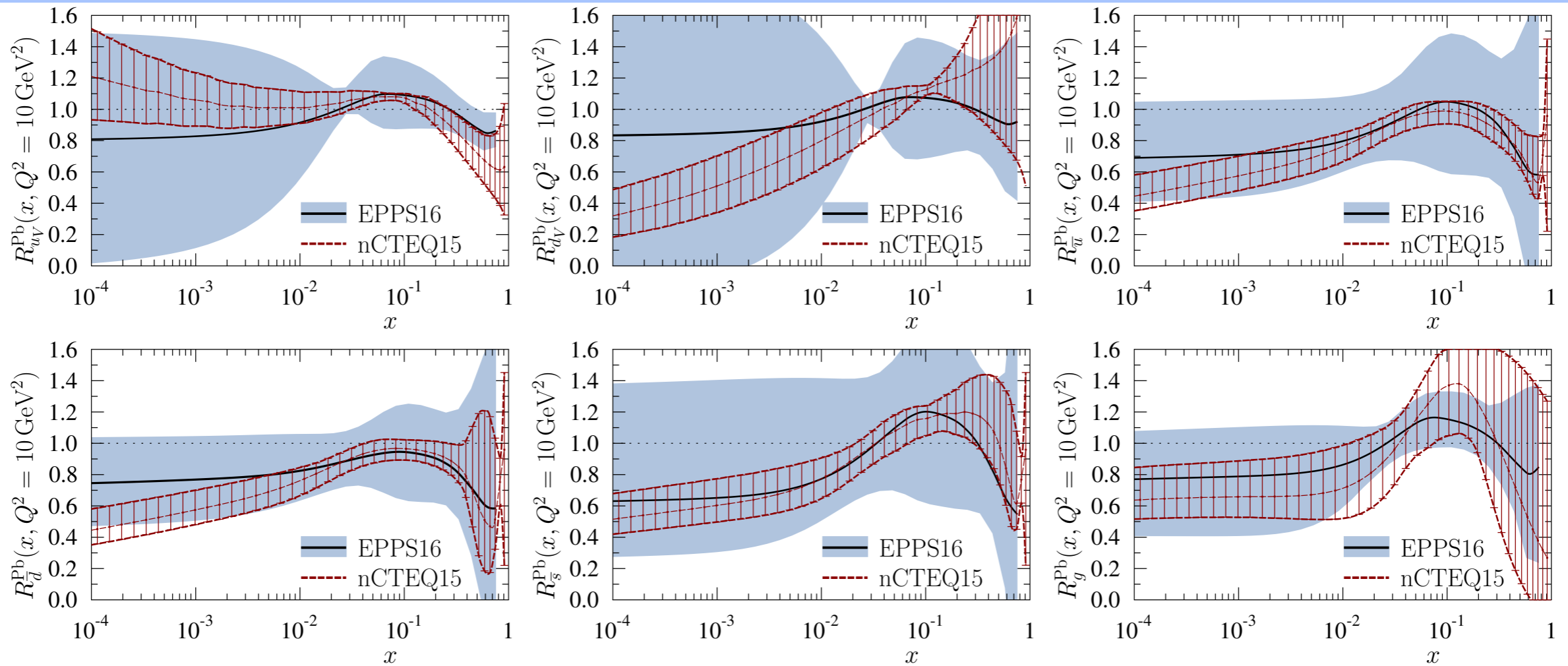
# DSSZ'11 framework

► NLO fit:  $\chi^2/dof = 0.99$



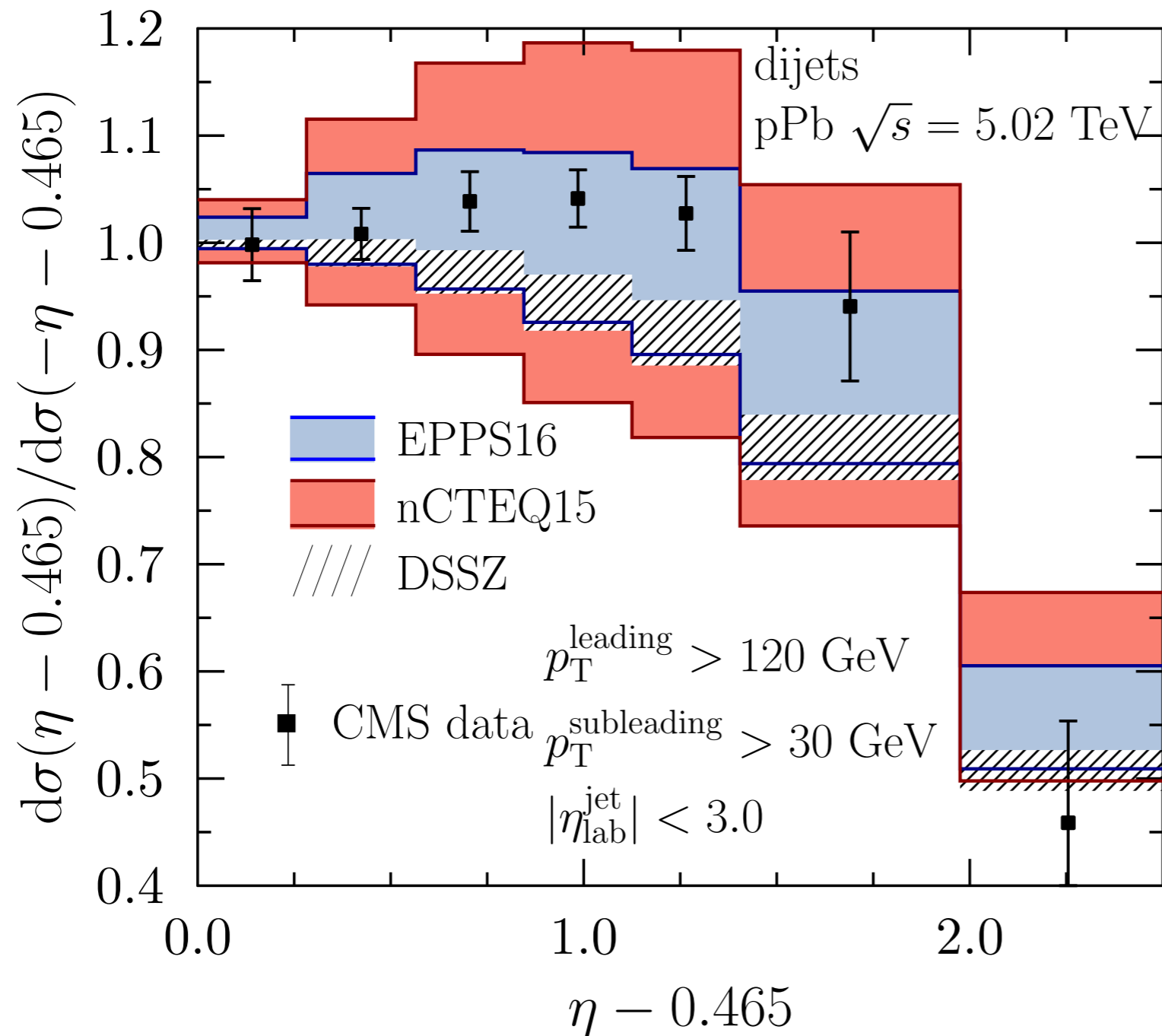
**Some comparisons  
(taken from EPPS'16 paper)**

# EPPS'16 vs nCTEQ'15 @ $Q^2=10 \text{ GeV}^2$



- Generally good agreement for  $x > 0.01$  (nCTEQ has no data constraints for  $x < 0.01$ )  
 $\Delta\chi^2 = 35$  (nCTEQ'15),  $\Delta\chi^2 = 52$  (EPPS'16)
- Valence bands at large- $x$  partly differ (valence at small- $x < 10^{-2}$  irrelevant);  
 influence from CHORUS data?
- EPPS'16 bands for light sea more realistic; nCTEQ'15 has fewer fit parameters for sea
- Still quite some parametrization bias even for EPPS'16

# Comparison with dijet data



- nCTEQ'15 in agreement with CMS data; including CMS dijet data in global analysis will help
- DSSZ gluon needs to be revised since not enough shadowed **OR** energy loss effects need to be included?

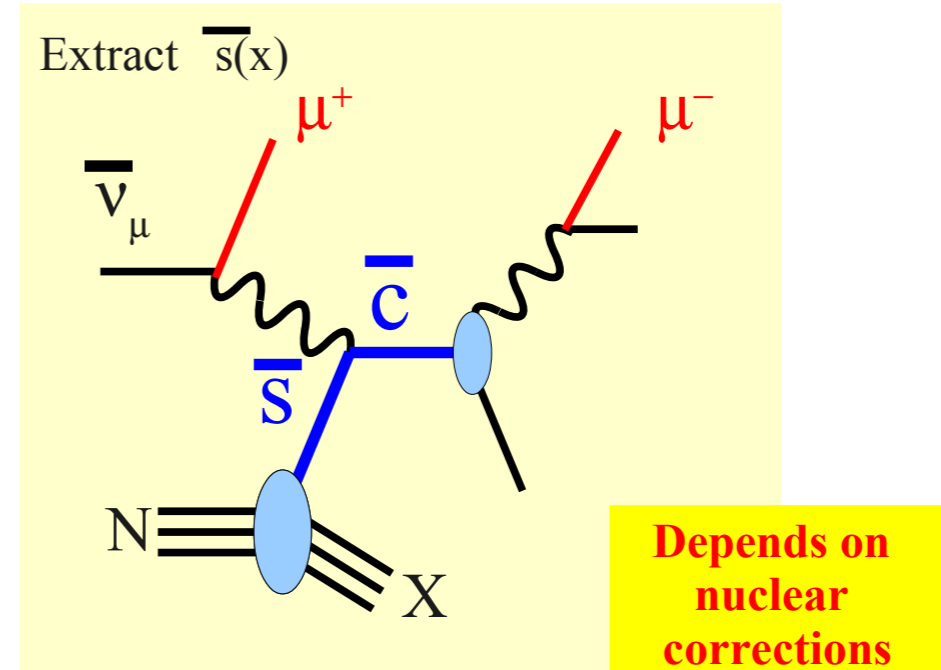
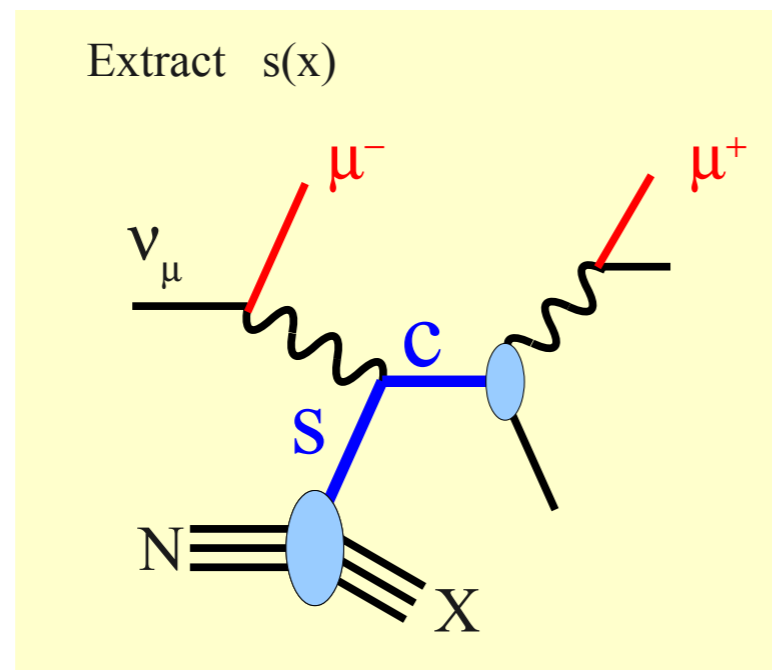
# Vector boson production and the strange PDF

see [arXiv:1203.1290](#) for a discussion of experimental constraints on the strange PDF



# Strange PDF: experimental constraints

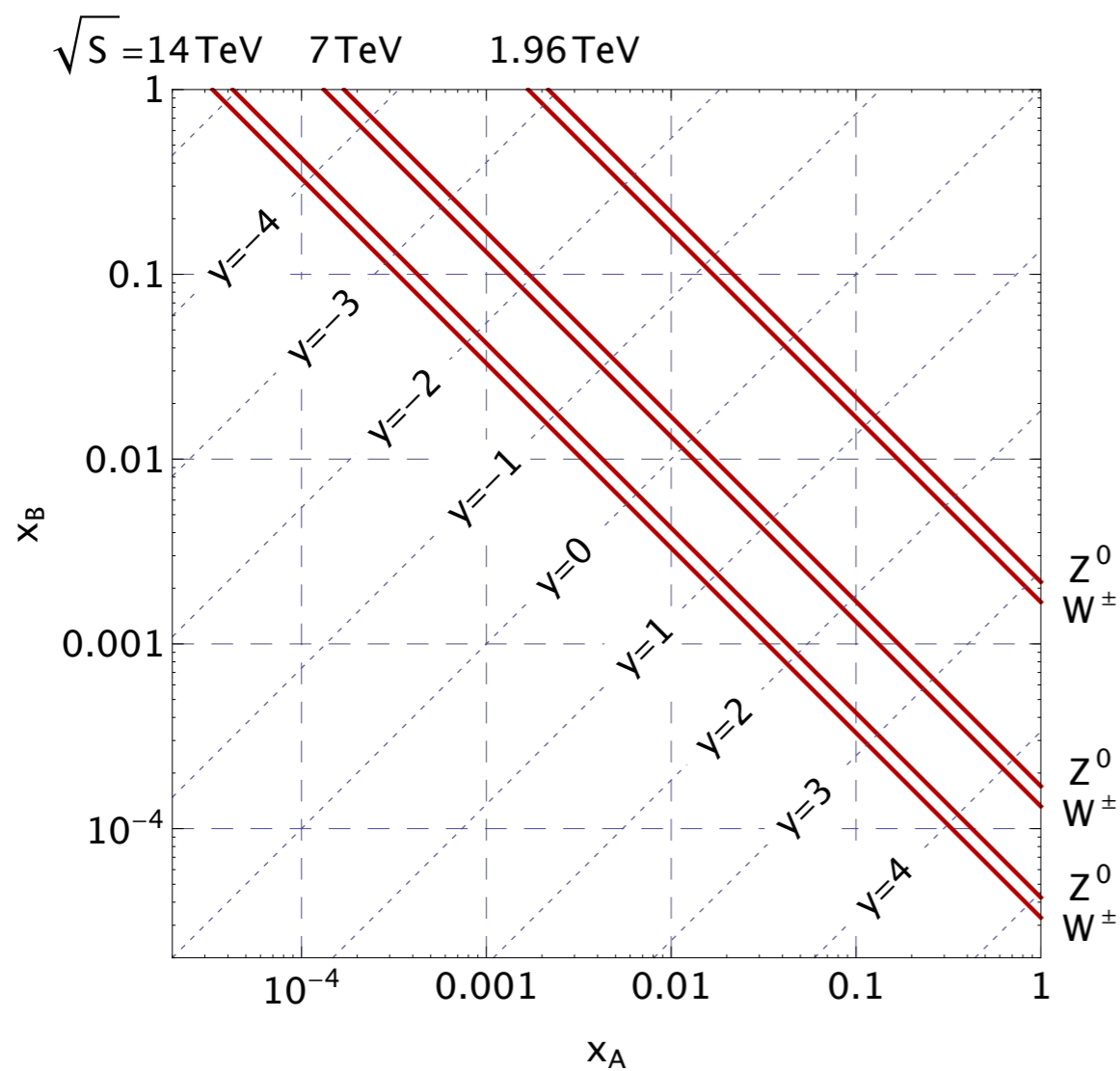
Opposite sign dimuon production in neutrino DIS:  $\nu N \rightarrow \mu^+ \mu^- X$



- High-statistics data from CCFR and NuTeV: **Main source** of information!
- $x \sim [0.01, 0.4]$
- $\nu\text{Fe}$  DIS: need **nuclear corrections!** Problem: Final State Interactions (FSI)
- CHORUS ( $\nu\text{Pb}$ ): compatible with NuTeV, could be included
- NOMAD ( $\nu\text{Fe}$ ): data not yet published, in principle very interesting

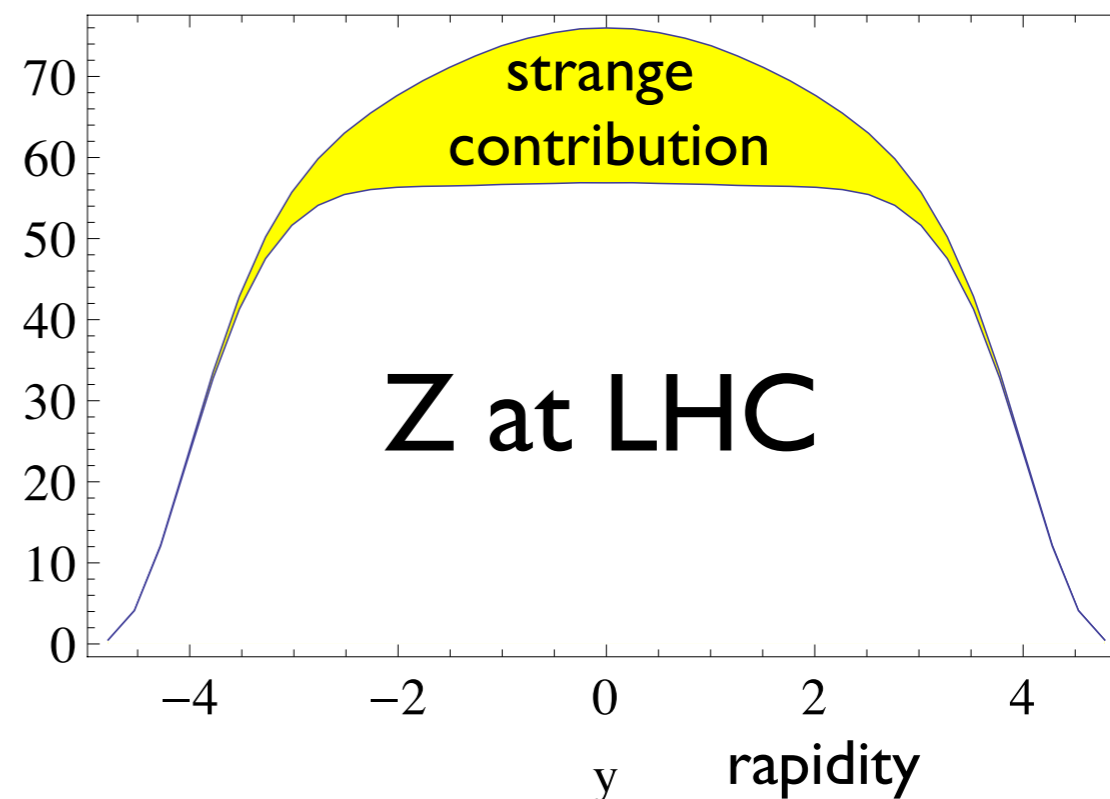
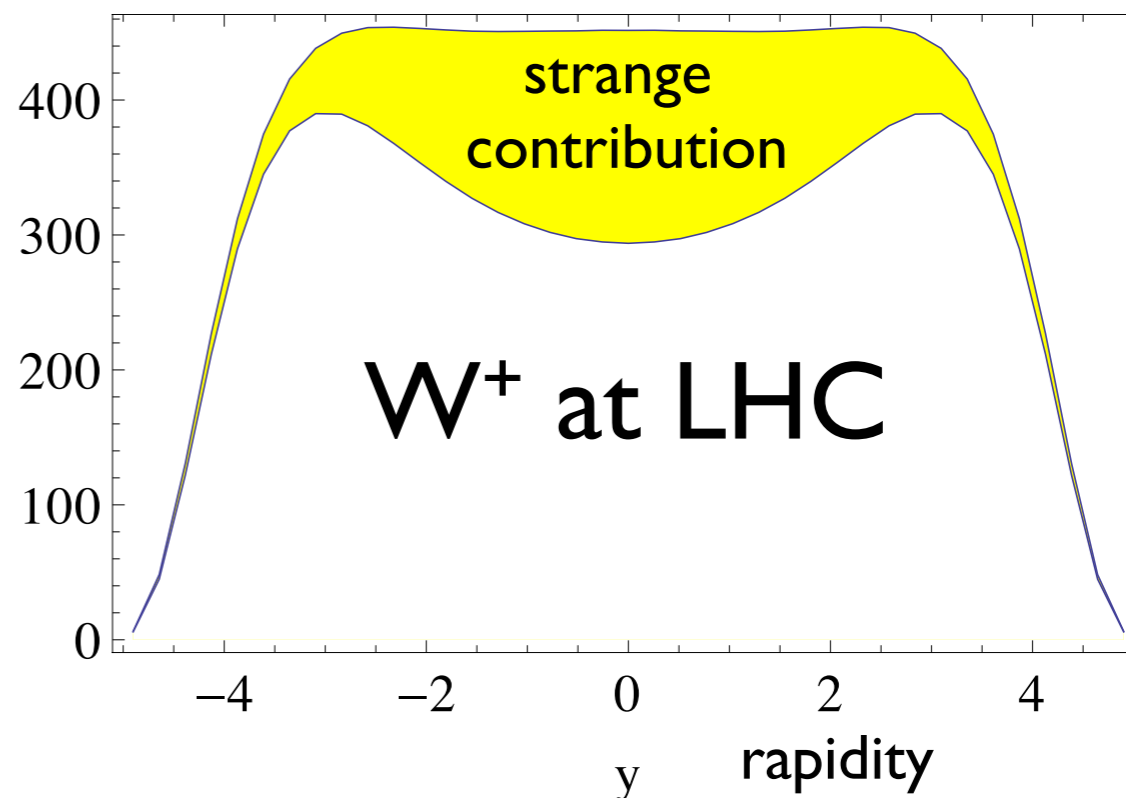
# Drell-Yan production of W/Z at the LHC

Kinematic plane



Uncertainty of strange-PDF will feed into benchmark process

$d^2\sigma/dM/dy$  [pb/GeV]



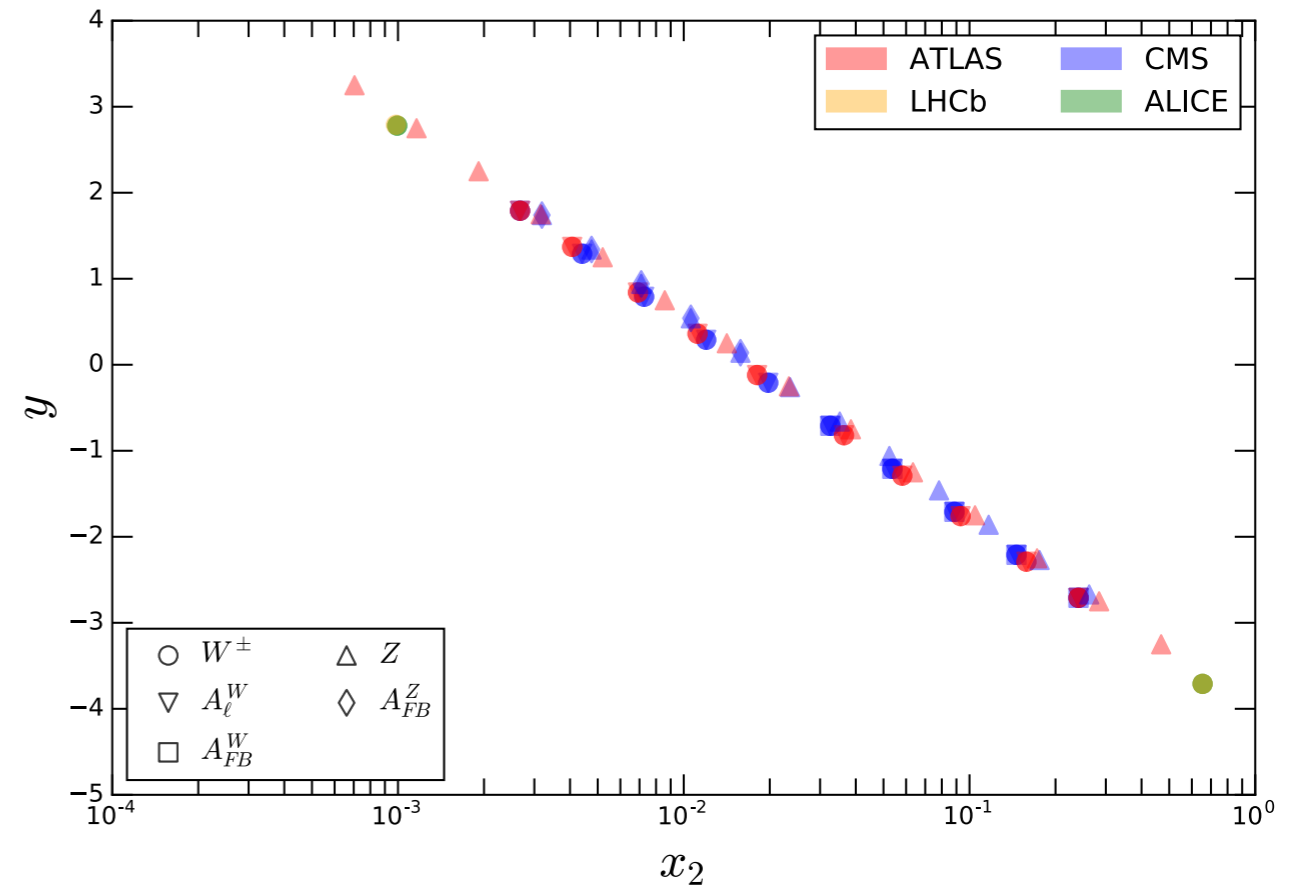
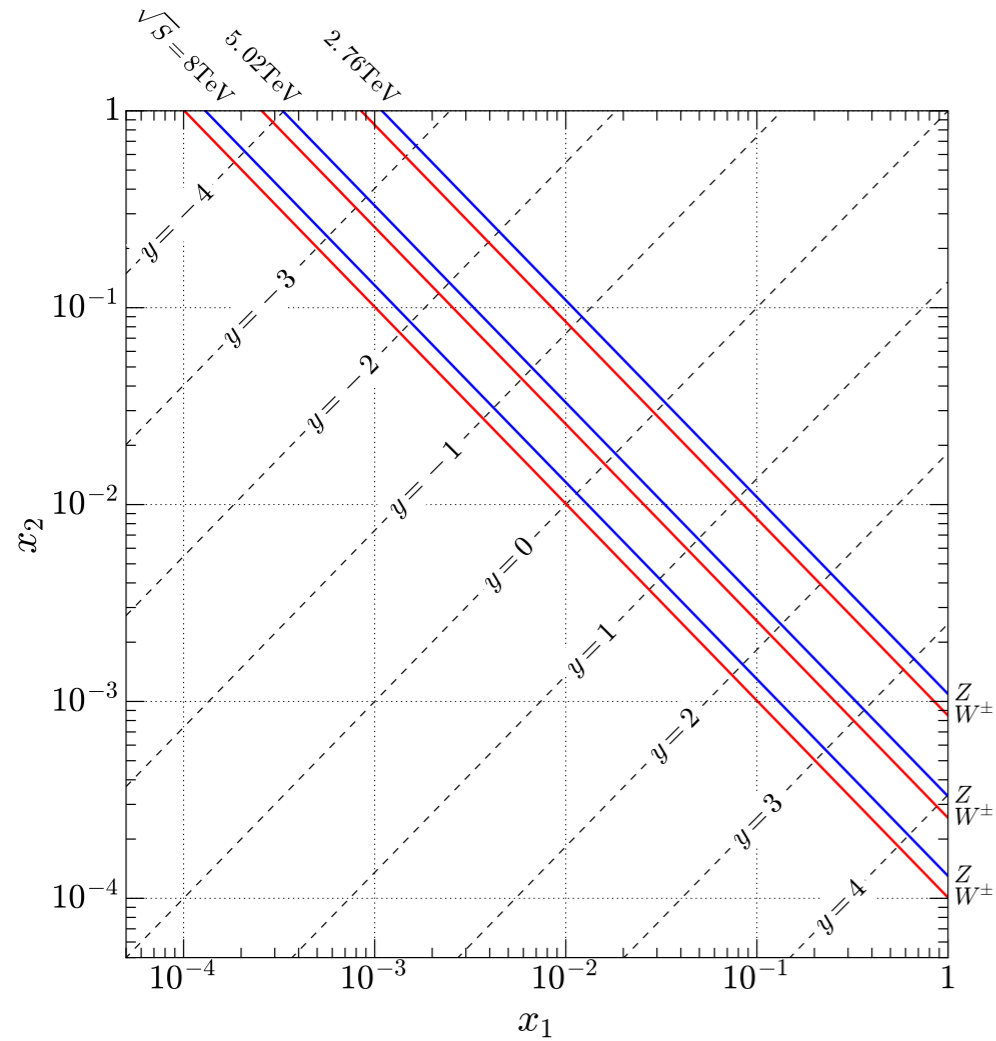
# nCTEQ study of W,Z production at LHC

arXiv:1610.02925

		Observable	Cuts (GeV)	Figure
pPb	ATLAS	$d\sigma(Z \rightarrow \ell^+ \ell^-)/dy_Z$ [2]	$ y_Z^{\text{CM}}  < 3.5; 60 < m_{\ell^+ \ell^-} < 120$	Fig. 3
		$d\sigma(W^+ \rightarrow \ell^+ \nu)/dy_{\ell^+}$ [6]	$p_T^{\ell^\pm} > 25; m_T^{\ell^\pm} > 40;  \eta_{lab}^{\ell^\pm}  < 2.4$	Fig. 7a
		$d\sigma(W^- \rightarrow \ell^- \bar{\nu})/dy_{\ell^-}$ [6]	$p_T^{\ell^\pm} > 25; m_T^{\ell^\pm} > 40;  \eta_{lab}^{\ell^\pm}  < 2.4$	Fig. 7b
	CMS	$d\sigma(Z \rightarrow \ell^+ \ell^-)/dy_Z$ [3]	$ \eta_{lab}^{\ell^\pm}  < 2.4; 60 < m_{\ell^+ \ell^-} < 120; p_T^{\ell^+ (\ell^-)} > 20$	Fig. 4
		$d\sigma(W^+ \rightarrow \ell^+ \nu)/dy_{\ell^+}$ [5]	$p_T^{\ell^\pm} > 25;  \eta_{lab}^{\ell^\pm}  < 2.4$	Fig. 6a
		$d\sigma(W^- \rightarrow \ell^- \bar{\nu})/dy_{\ell^-}$ [5]	$p_T^{\ell^\pm} > 25;  \eta_{lab}^{\ell^\pm}  < 2.4$	Fig. 6b
	LHCb	$\sigma(Z \rightarrow \ell^+ \ell^-)$ [4]	$60 < m_{\ell^+ \ell^-} < 120; p_T^{\ell^+ (\ell^-)} > 20; 2.0 < \eta^{\ell^\pm} < 4.5; -4.5 < \eta_{\ell^\pm} < -2.0$	Fig. 5
	ALICE	$\sigma(W^+ \rightarrow \ell^+ \nu)$ [7]	$p_T^{\ell^\pm} > 10; 2.03 < \eta_{lab}^{\ell^\pm} < 3.53; -4.46 < \eta_{lab}^{\ell^\pm} < -2.96$	Fig. 8a
$\sigma(W^- \rightarrow \ell^- \bar{\nu})$ [7]		$p_T^{\ell^\pm} > 10; 2.03 < \eta_{lab}^{\ell^\pm} < 3.53; -4.46 < \eta_{lab}^{\ell^\pm} < -2.96$	Fig. 8b	
PbPb	ATLAS	$1/\sigma_{tot} d\sigma/dy_Z$ [8]	$66 < m_{\ell^+ \ell^-} < 116;  y_Z  < 2.5$	Fig. 9a
		$A_\ell$ [10]	$p_T^\ell < 25;  \eta_{lab}^\ell  < 2.5; m_T > 40; p_T^{miss} < 25$	Fig. 10a
	CMS	$1/\sigma_{tot} d\sigma/dy_Z$ [9]	$60 < m_{\ell^+ \ell^-} < 120;  y_Z  < 2.0$	Fig. 9b
		$A_\ell$ [11]	$p_T^\ell < 25;  \eta_{lab}^\ell  < 2.1; m_T > 40$	Fig. 10b

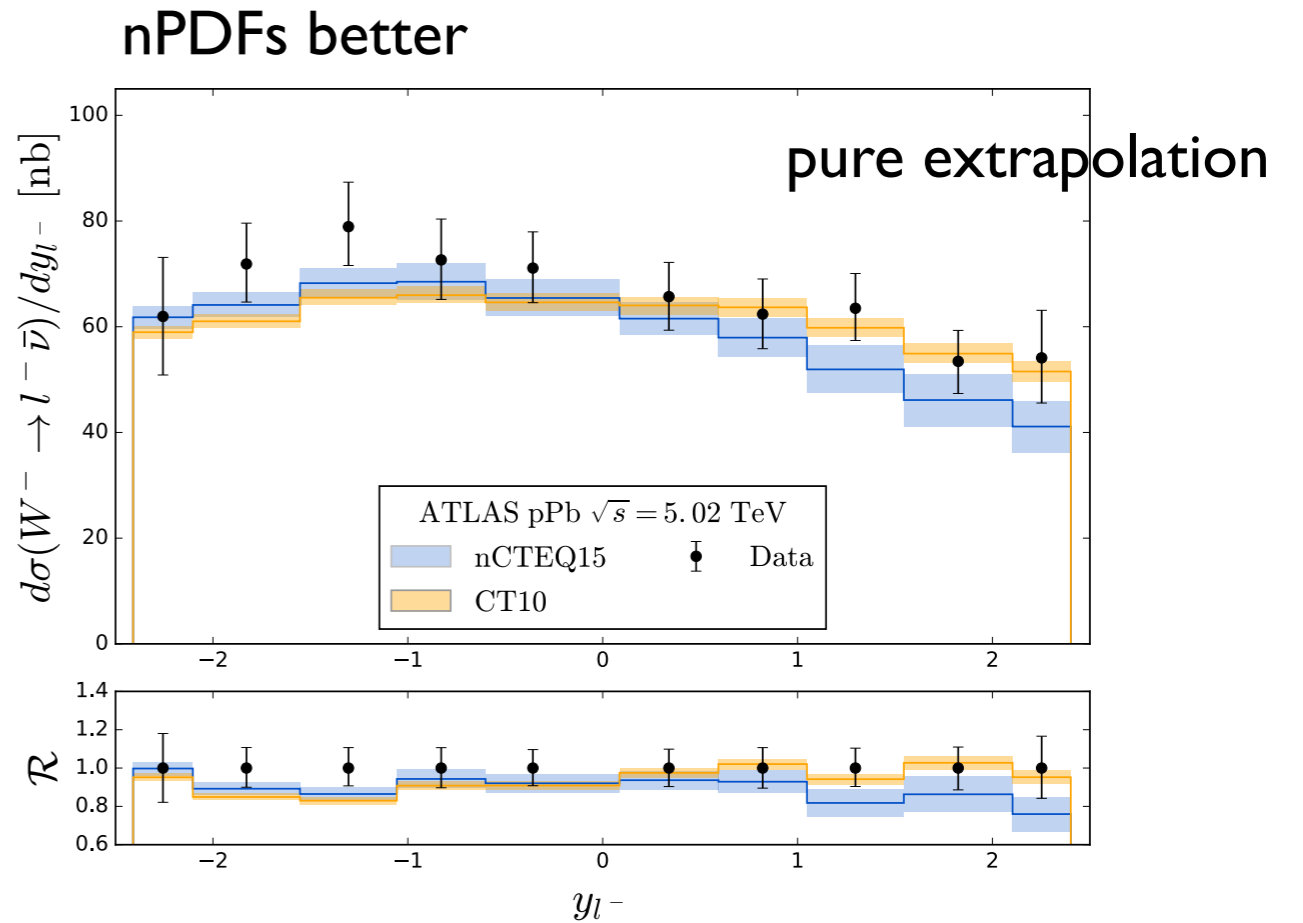
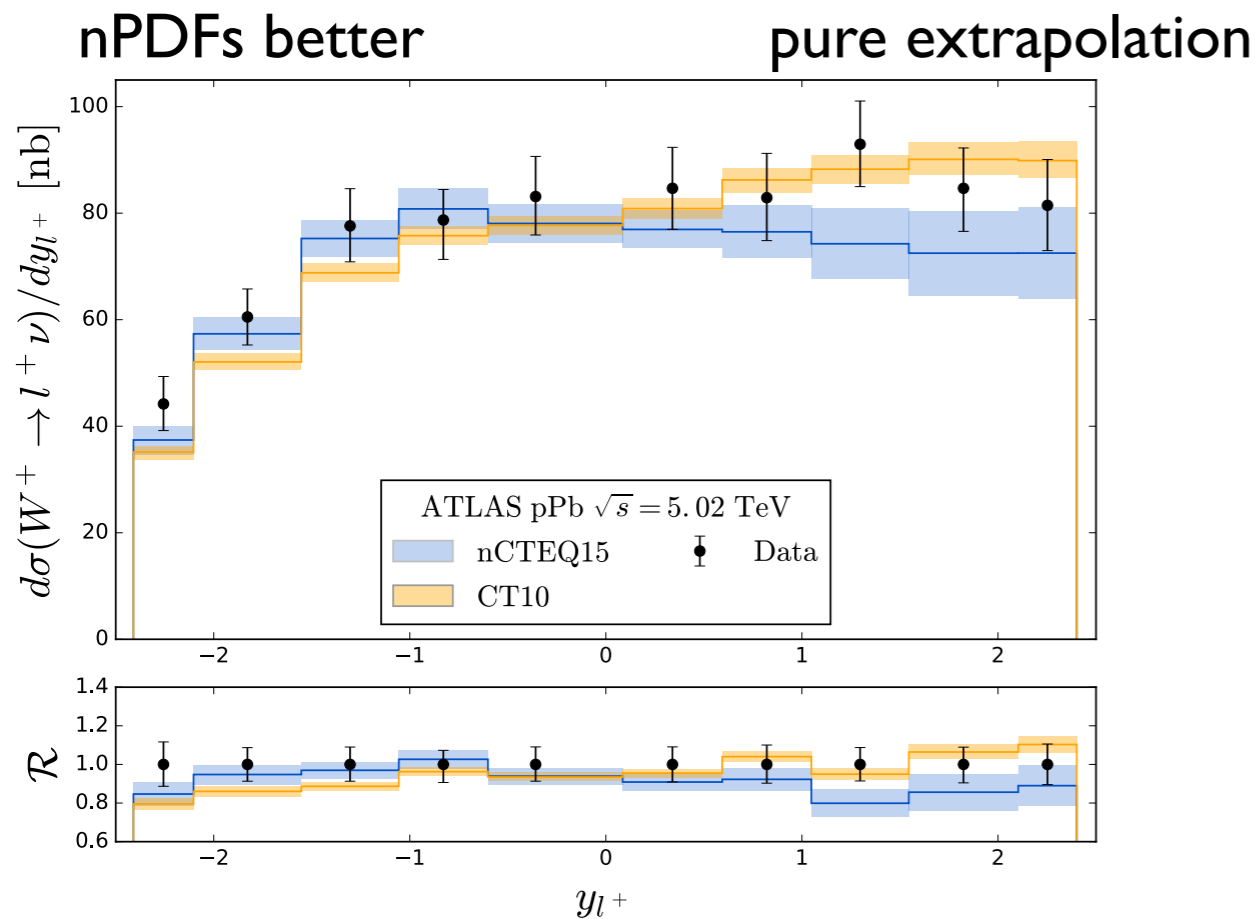
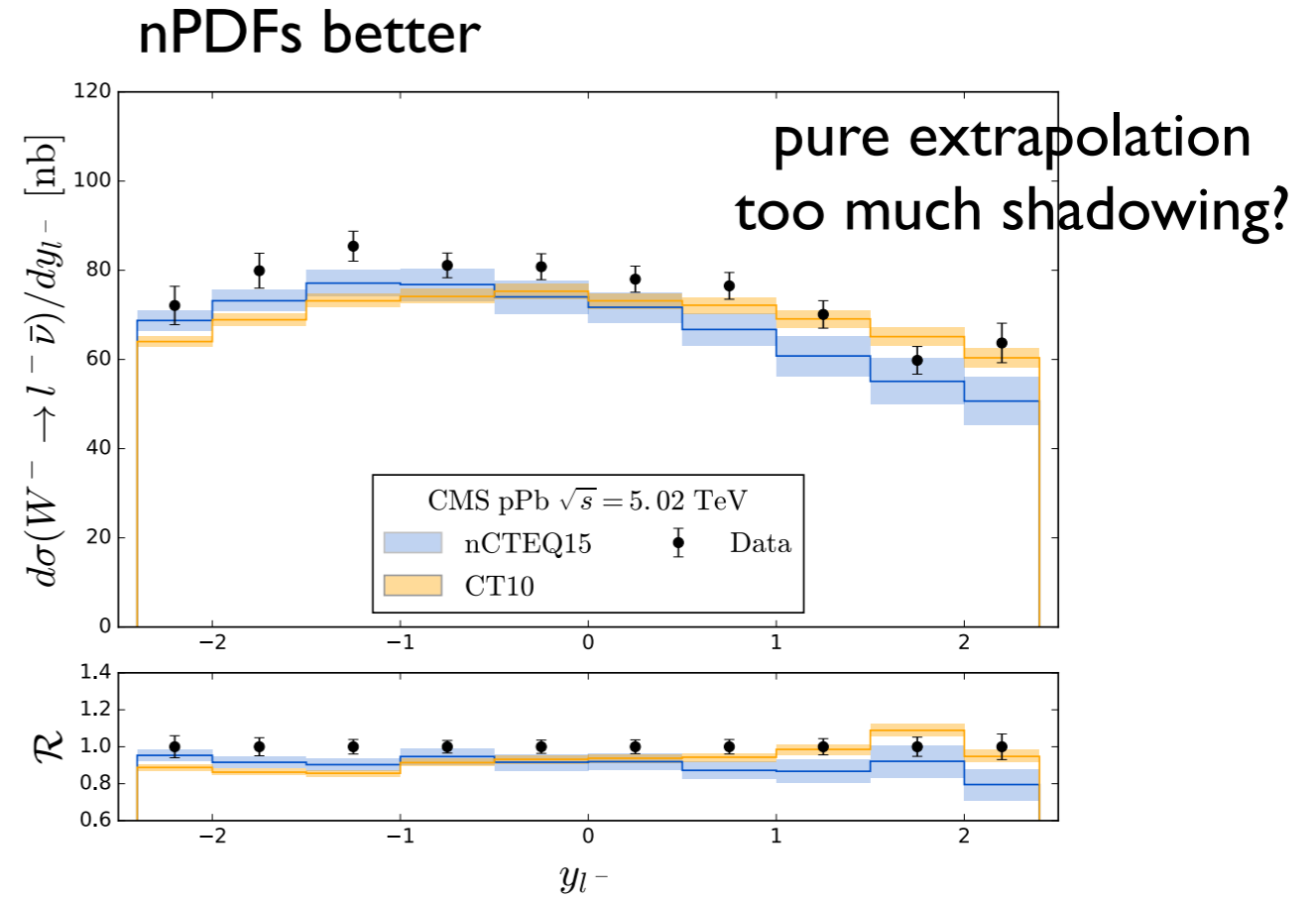
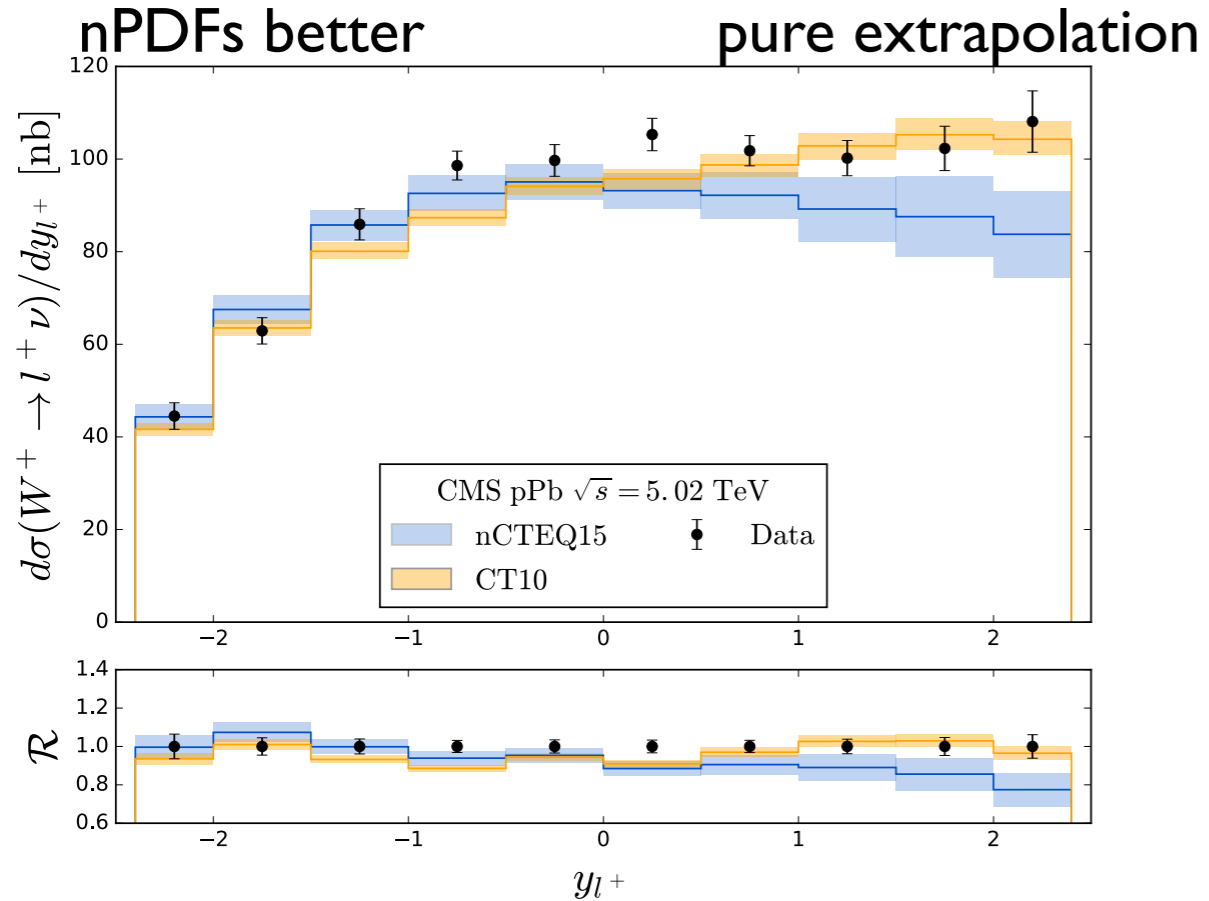
Table I: LHC data sets considered in this analysis.

# nCTEQ study of W,Z production at LHC

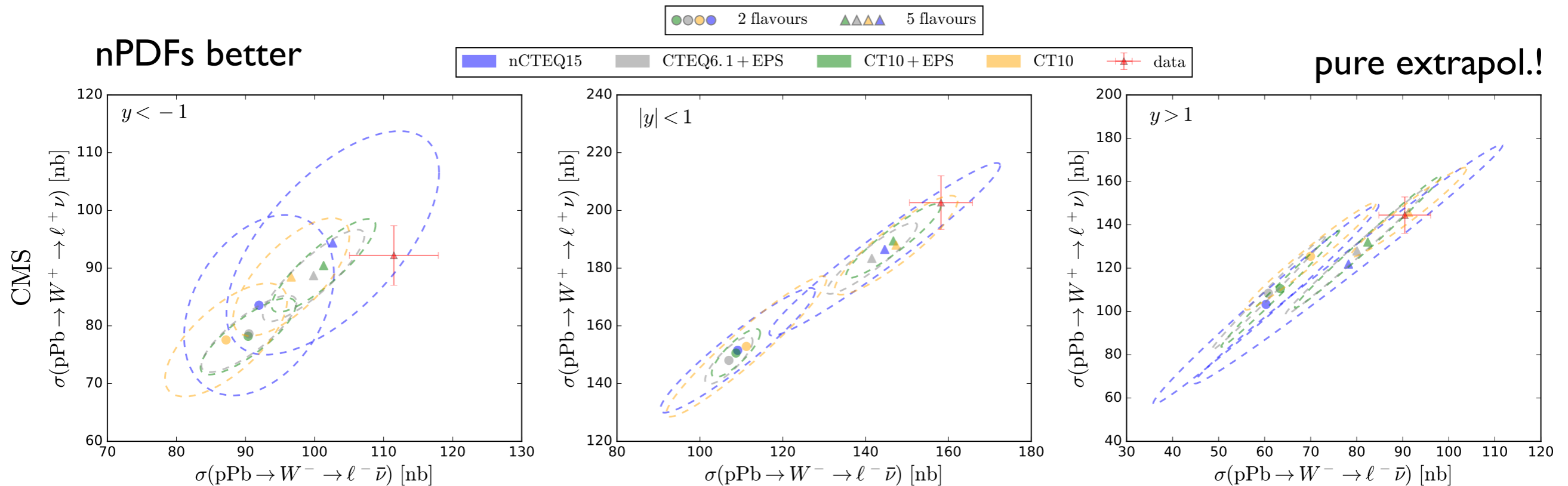


- $y < -1: x > 5 \times 10^{-2} \dots 0.3$  (region where nPDFs are constrained by data in global analysis)
- $|y| < 1: x \sim 10^{-2}$  (transition region from anti-shadowing to shadowing)
- $y > 1: x < 5 \times 10^{-3}$  (pure extrapolation!)

# W-boson rapidity distributions

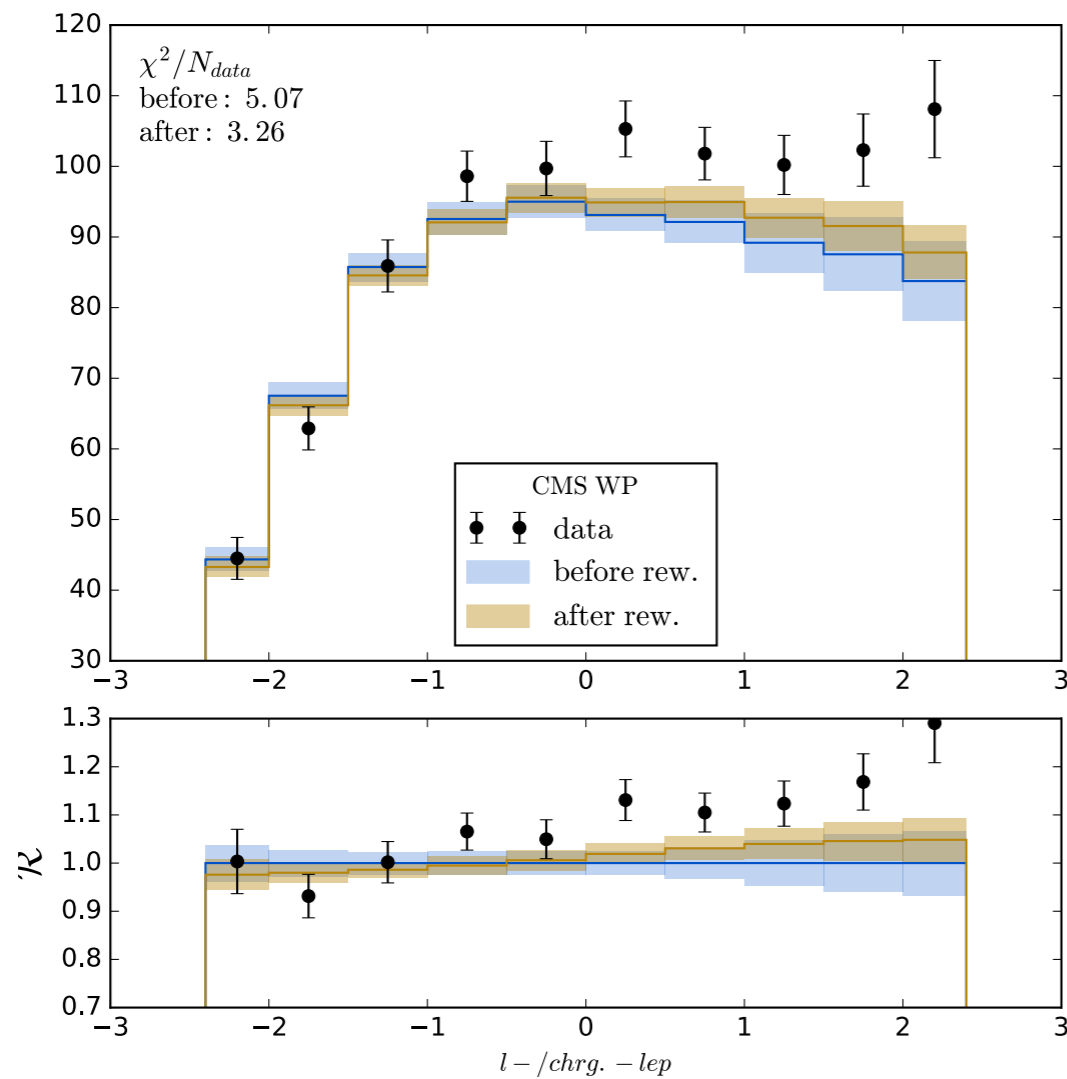


# Importance of strange PDF

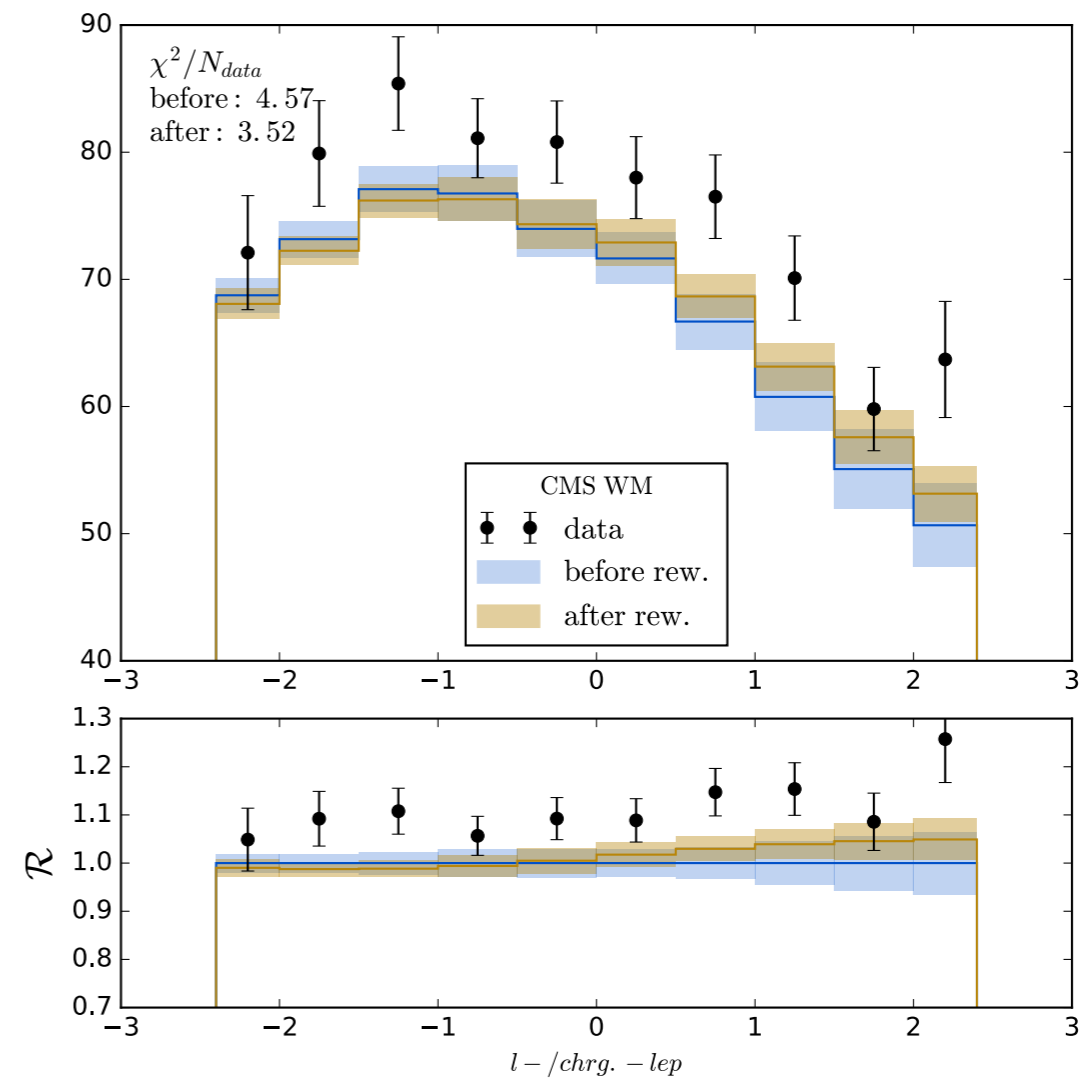


- $y < -1$  (large  $x$ ):  $s > \bar{s}$  could help!
- $|y| < 1$ : delayed transition from anti-shadowing to shadowing could help **as seen in NuTeV neutrino data**
- $y > 1$ : Extrapolation, **rather no shadowing at very small  $x$ ?**

# Reweighting



(a)  $W^+$



(b)  $W^-$

- Improvements after reweighting
- However, strange PDF not fitted independently in nCTEQ15
- Need to include data in global analysis and open up strange PDF

# Wishlist and Conclusions



# Available pPb LHC data

- $W/Z$  production
  - ATLAS [[arXiv:1507.06232](#), [ATLAS-CONF-2015-056](#)]
  - CMS [[arXiv:1512.06461](#), [arXiv:1503.05825](#)]
  - LHCb [[arXiv:1406.2885](#)]
  - ALICE [[arXiv:1511.06398](#)]
- Jets
  - ATLAS [[arXiv:1412.4092](#)]
  - CMS [[arXiv:1401.4433](#), [CMS-PAS-HIN-14-001](#)]
- Charged particle production (FFs dependence)
  - CMS [[CMS-PAS-HIN-12-017](#)]
  - ALICE [[arXiv:1405.2737](#), [arXiv:1505.04717](#)]
- Isolated photons (PbPb)
  - ATLAS [[arXiv:1506.08552](#)]
  - CMS [[arXiv:1201.3093](#)]
  - ALICE [[arXiv:1509.07324](#)]

# Wishlist

- More precise data for W/Z production
  - Advantage: uncolored final state!
  - sensitive to strange PDF at  $y < -1$  assuming light sea known; comparison with **dimuon data** from NuTeV
  - **small-x**: constraints on light sea (and strange sea but flavour separation difficult)
- Inclusive D-meson production
  - Very sensitive to gluon production at small-x!  
see PROSA study (for the gluon in the proton): [EPJC75\(2015\)396](#), arXiv: [1503.04581](#)
  - at large  $p_T$  and forward rapidities: probe of IC
- Inclusive photon+charm production
  - probe of intrinsic charm

# Wishlist: Fixed target mode

- several different nuclei, constrain **large-x** nuclear PDFs
- Modern measurement of DY lepton pair production
- Inclusive D-meson production
  - probe nuclear gluon at large-x
  - constrain heavy quark (charm) distribution, test models of intrinsic charm
- Inclusive photon+charm production
  - ideal testing ground for intrinsic charm [recent review, arXiv:1504.06287]

# Conclusions

- Much recent progress (EPPS'16, NCTEQ'15, W/Z analysis)
- nPDF uncertainties still substantial
- Need more precise LHC pA data (LHC5, LHC8) from as many hard processes as possible! **Lead-only analysis possible!**
- Coloured and un-coloured final states to test shadowing vs energy loss effects
- Bright future: future fixed target experiments, EIC, LHeC,  $\pi$ -A data from COMPASS
- A lot of room for theoretical progress

# Backup

# EPS'09 framework

- ▶ LO & NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ( $Q_0=1.3\text{GeV}$ )

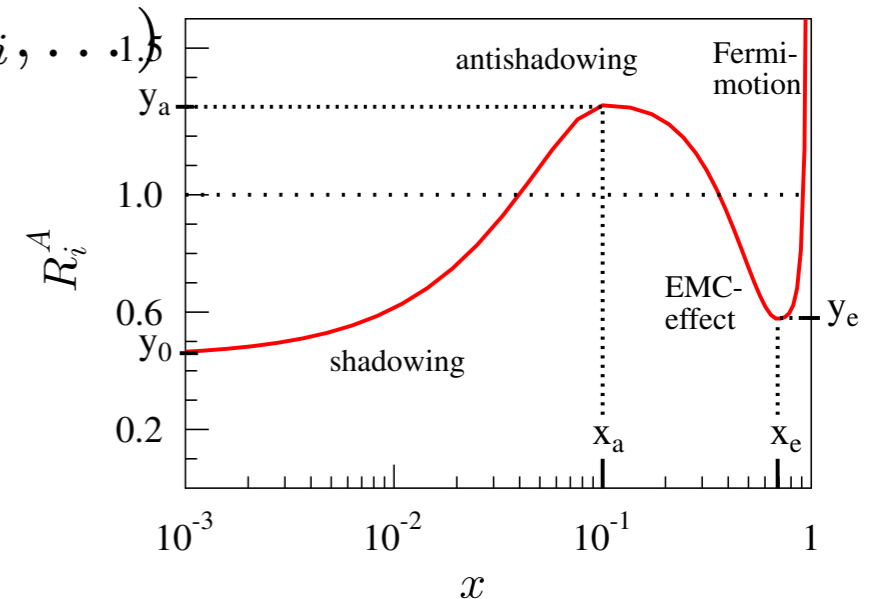
$$f_i^{p/A}(x_N, \mu_0) = R_i(x_N, \mu_0, A, Z) f_i(x_N, \mu_0), \quad i = \text{valence, sea, } g$$

$$R_i(x, A, Z) = \begin{cases} a_0 + (a_1 + a_2 x)(e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x)(1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$

A-dependence of fitting parameters ( $d_i = a_i, b_i, \dots$ )

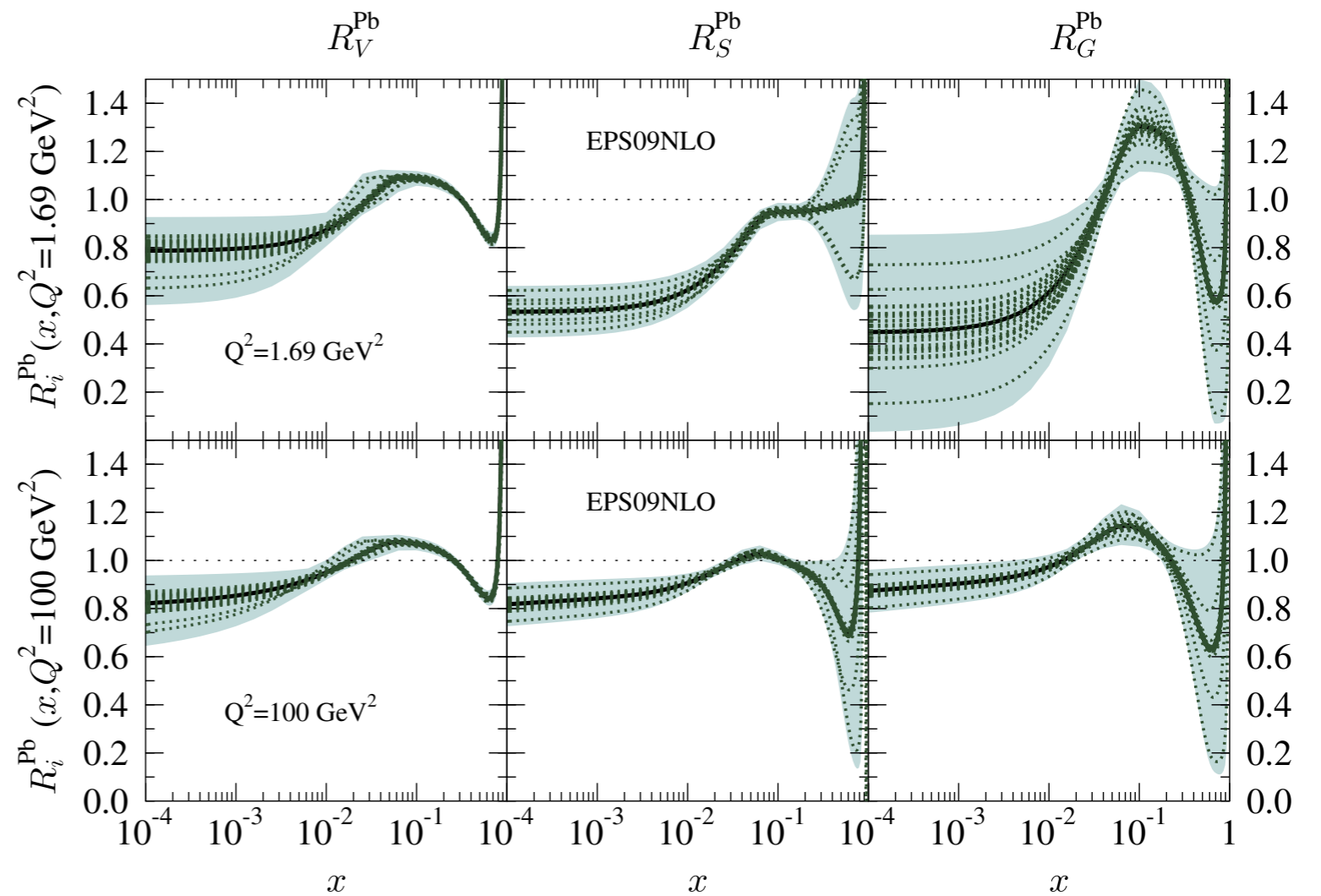
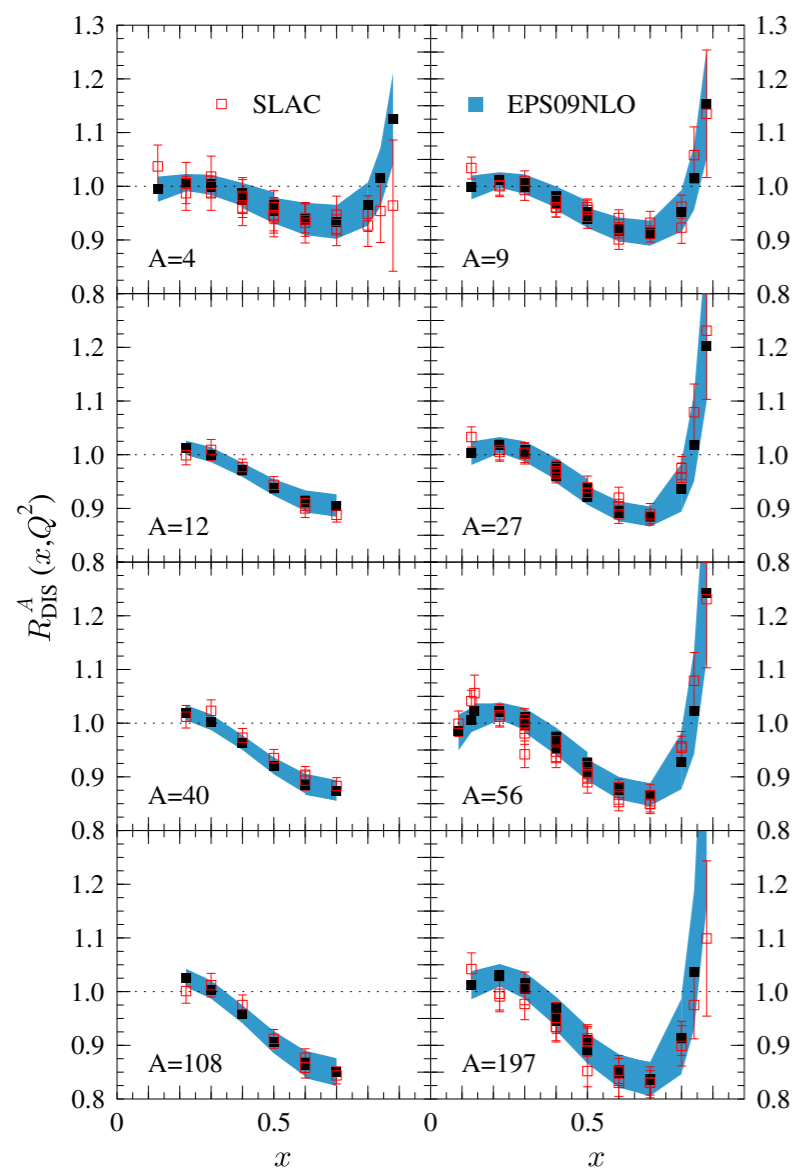
$$d_i^A = d_i^{A_{ref}} \left( \frac{A}{A_{ref}} \right)^{p_{d_i}}$$

- ▶ CTEQ6.1M free proton baseline
- ▶ Neglects  $x_N > 1$
- ▶ Data: DIS, DY,  $\pi^0$  @ RHIC



# EPS'09 framework

► NLO fit:  $\chi^2/dof = 0.79$



# HKN'07 framework

- ▶ LO & NLO PDFs with errors
- ▶ Error PDFs produced with *Hessian method*
- ▶ Parametrization ( $Q_0=1\text{GeV}$ )

$$f_i^{p/A}(x_N, Q_0) = R_i^A(x_N, Q_0) f_i^p(x_N, Q_0), \quad i = \text{valence, sea, } g$$

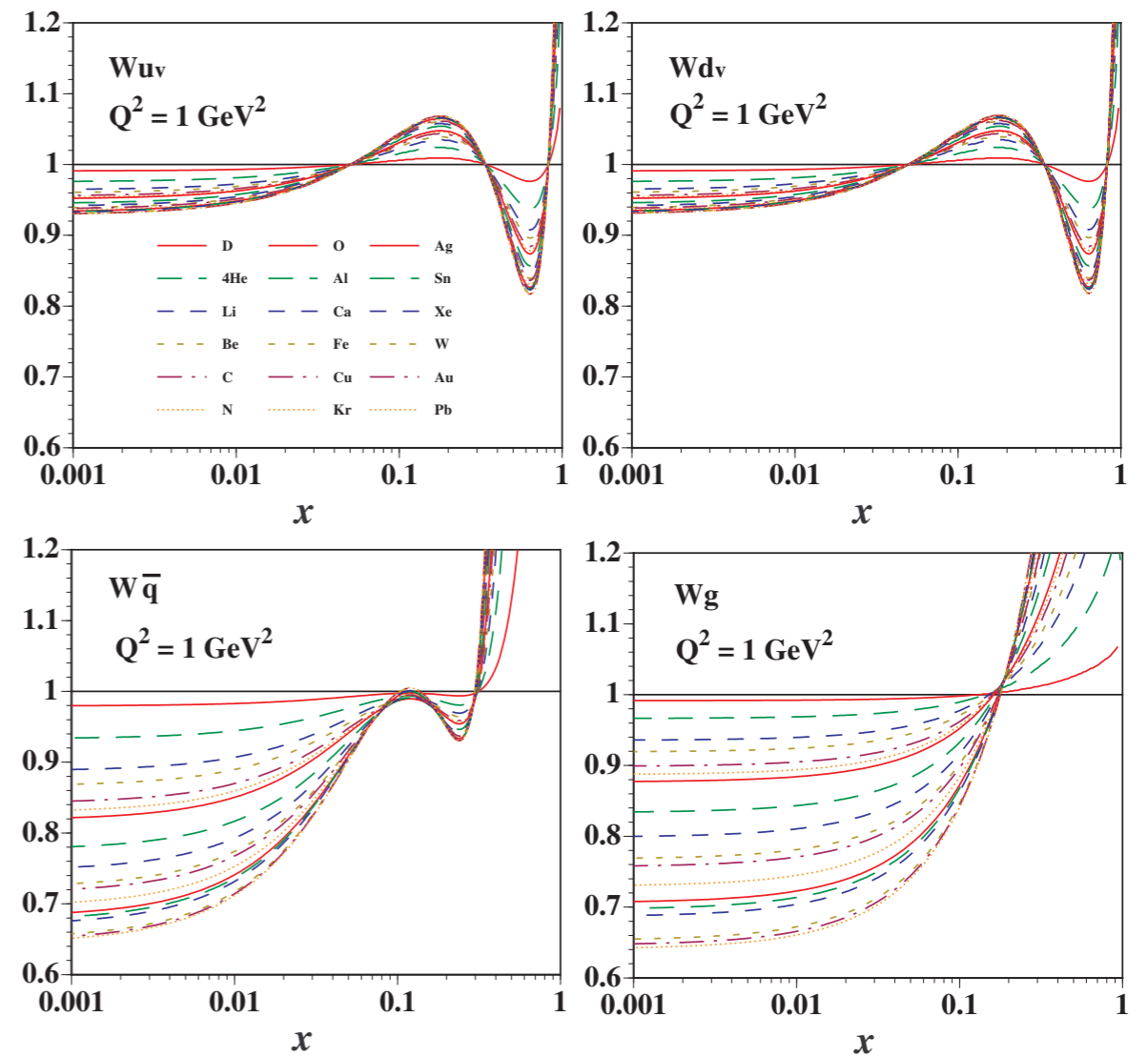
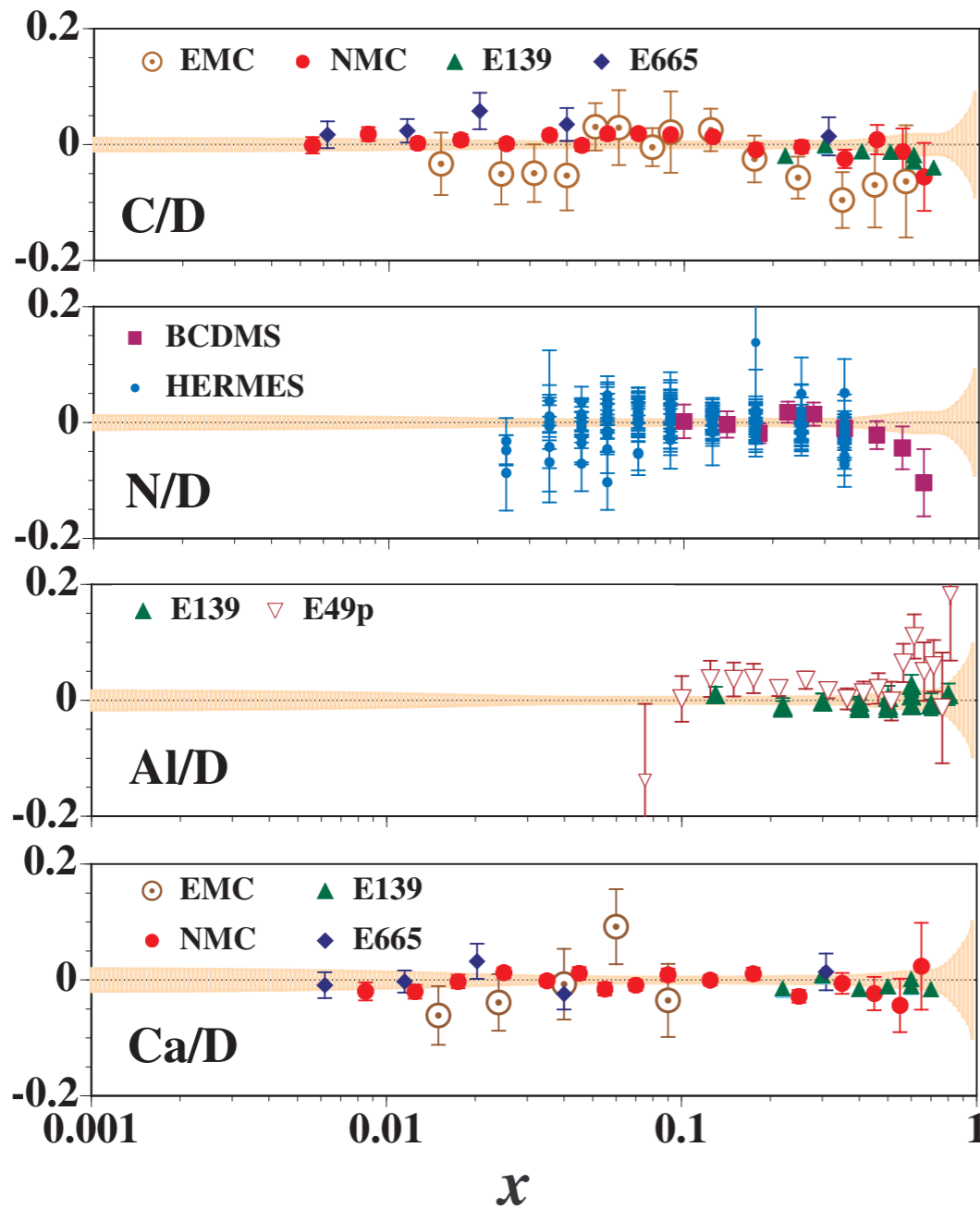
$$R_i(x, Q_0, A) = 1 + \left(1 - \frac{1}{A^\alpha}\right) \frac{a_i + b_i x + c_i x^2 + d_i x^3}{(1-x)^{\beta_i}}$$

- ▶ MRST 1998 free proton baseline
- ▶ Neglects  $x_N > 1$
- ▶ Data: DIS & DY

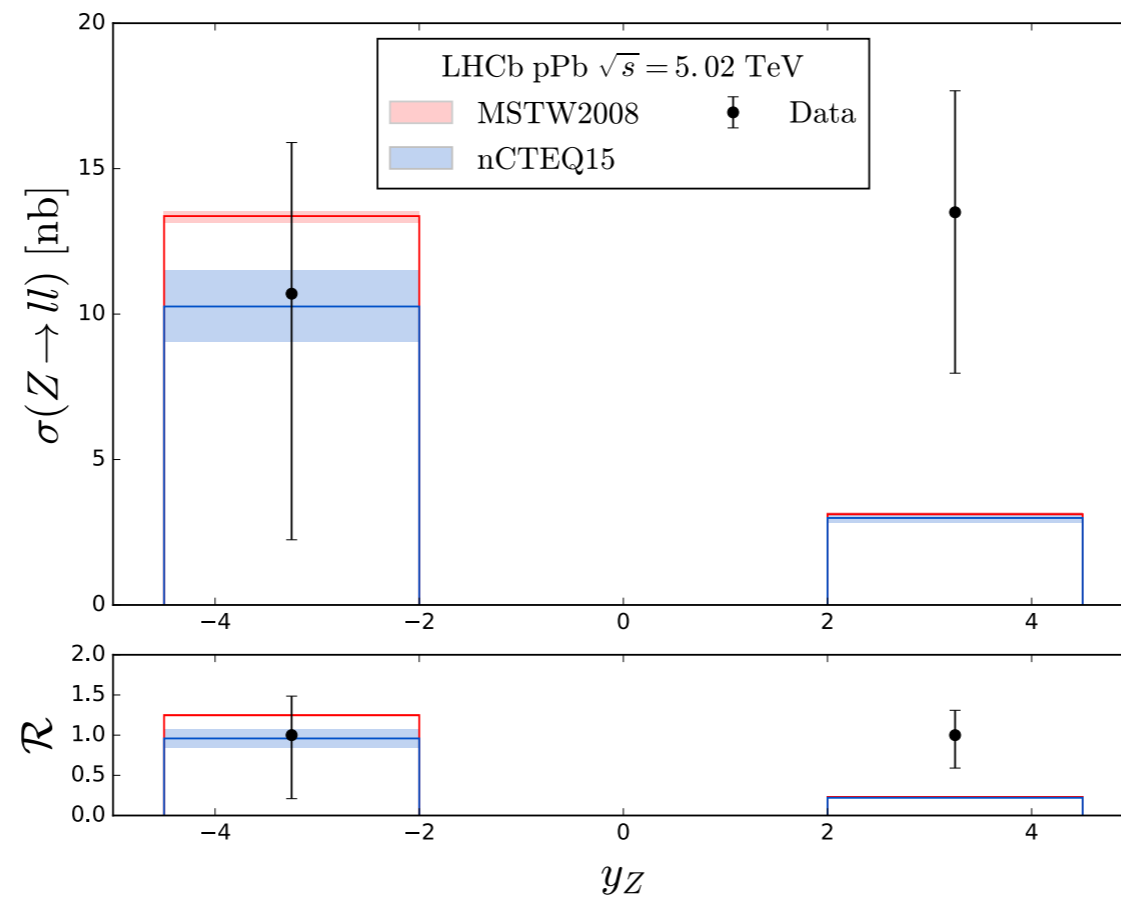
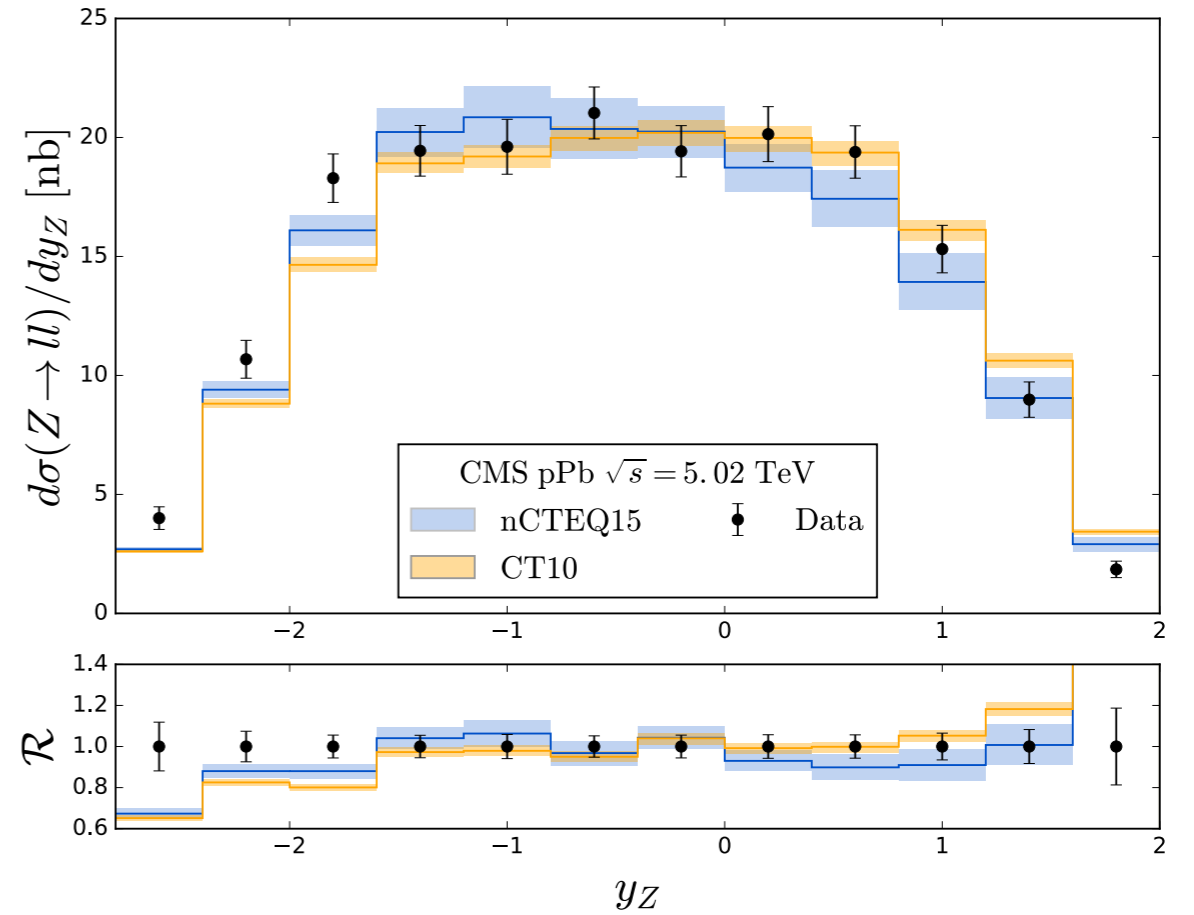
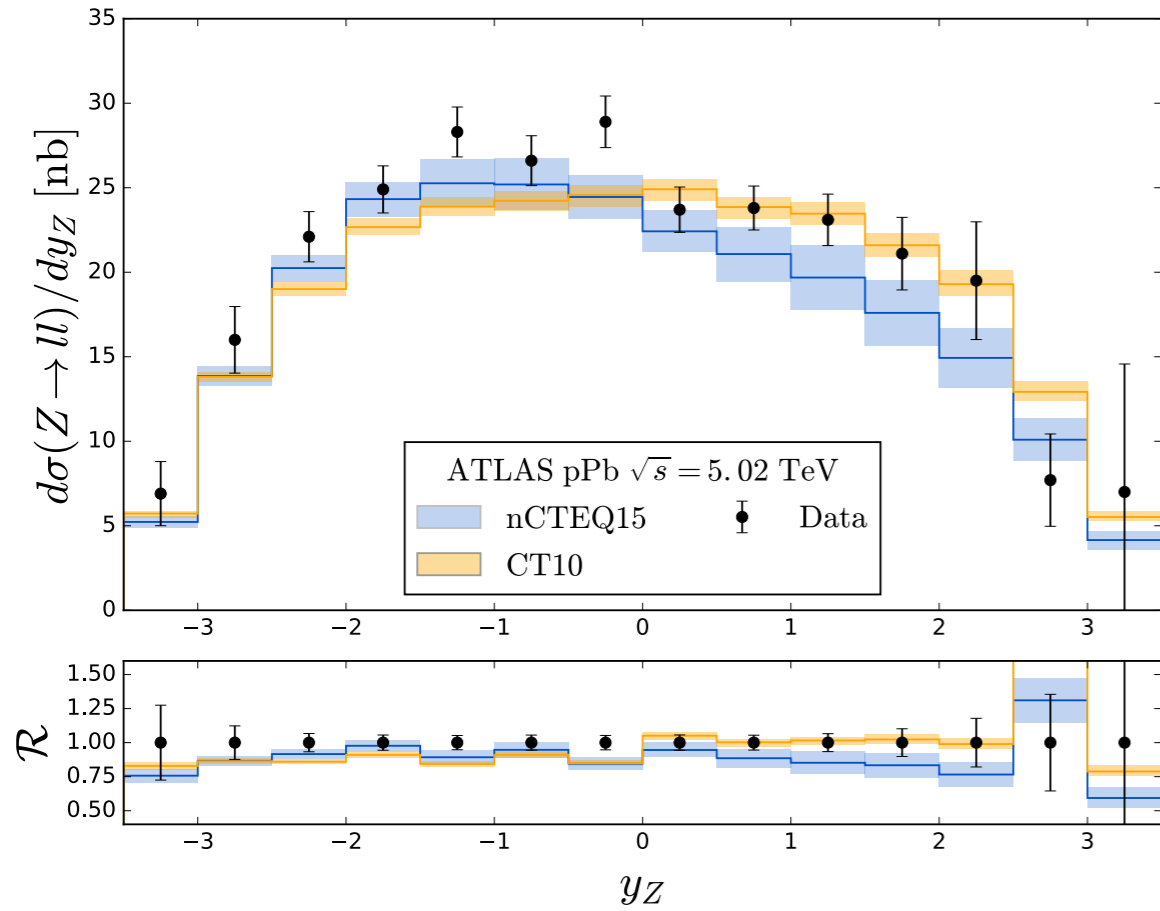


# HKN'07 framework

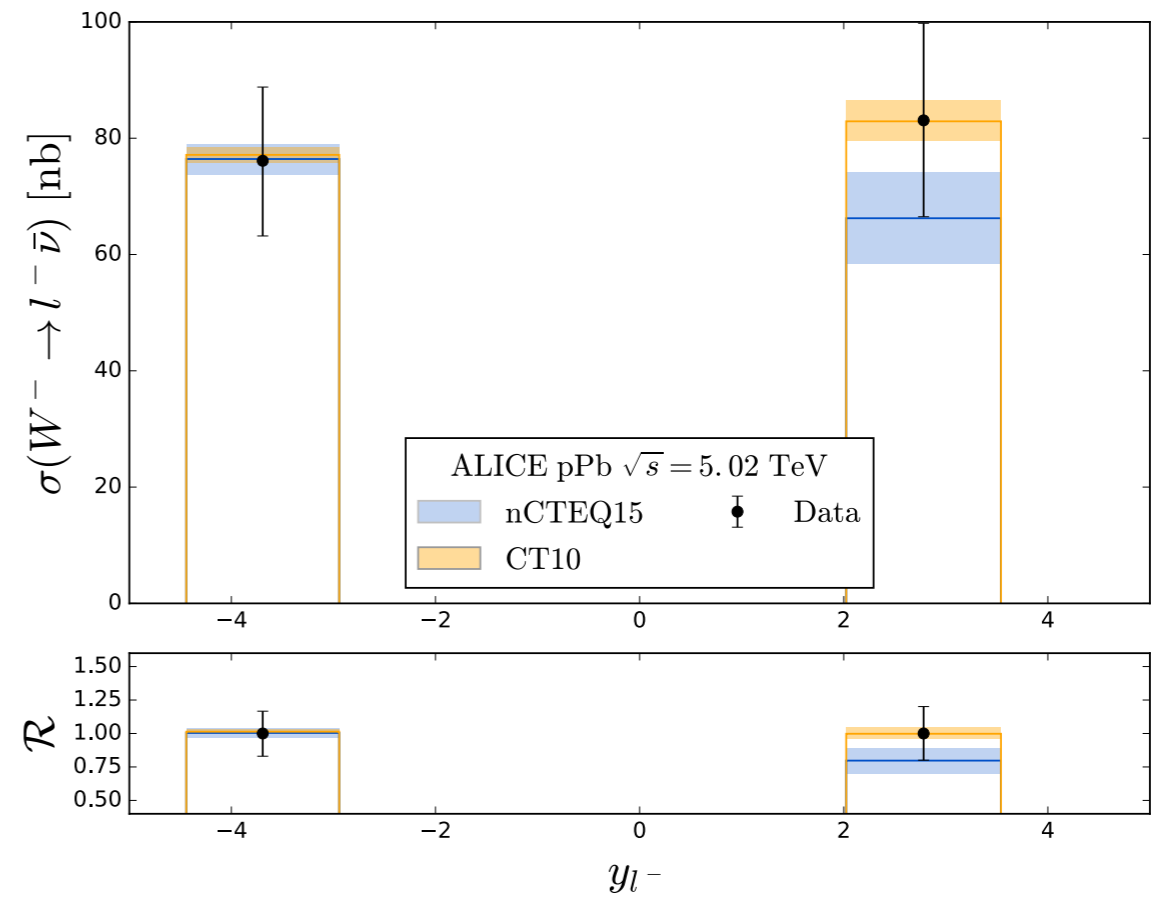
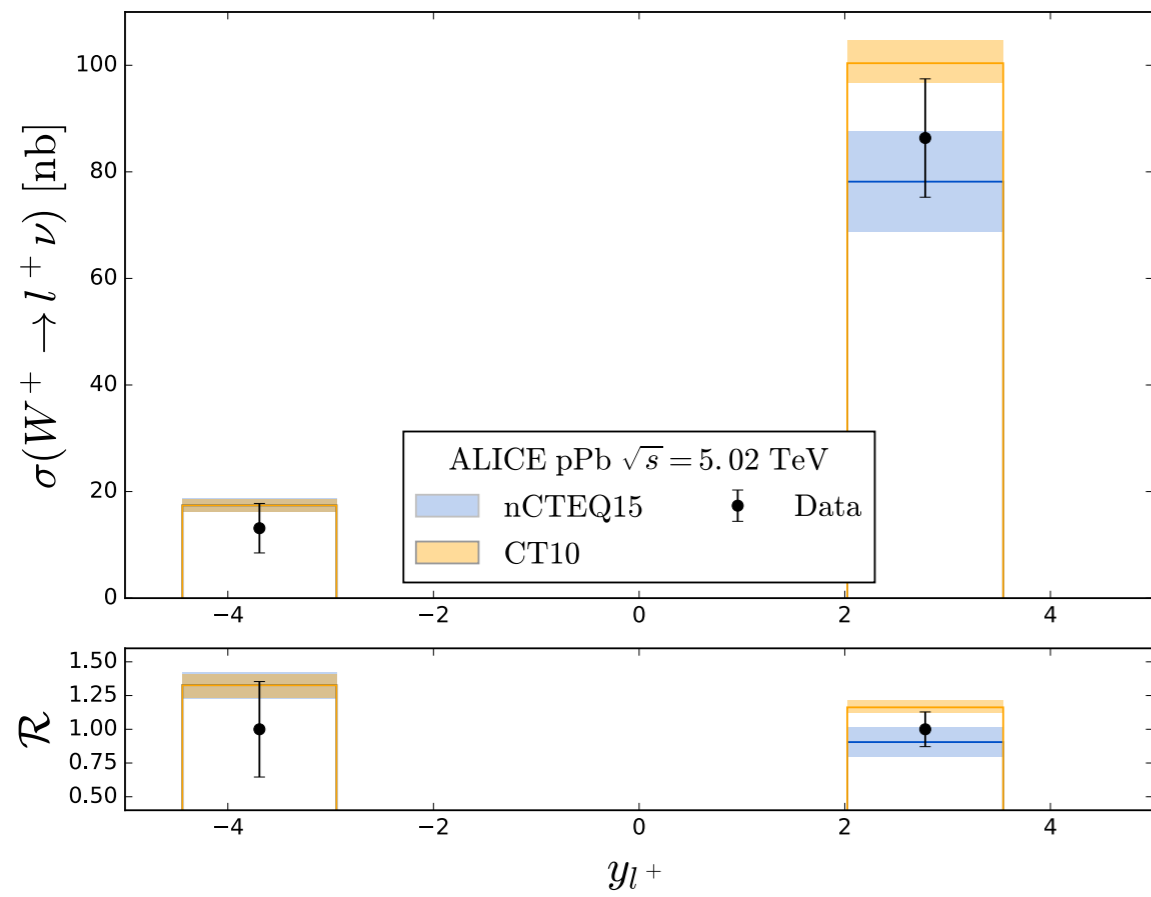
► NLO fit:  $\chi^2/dof = 1.21$



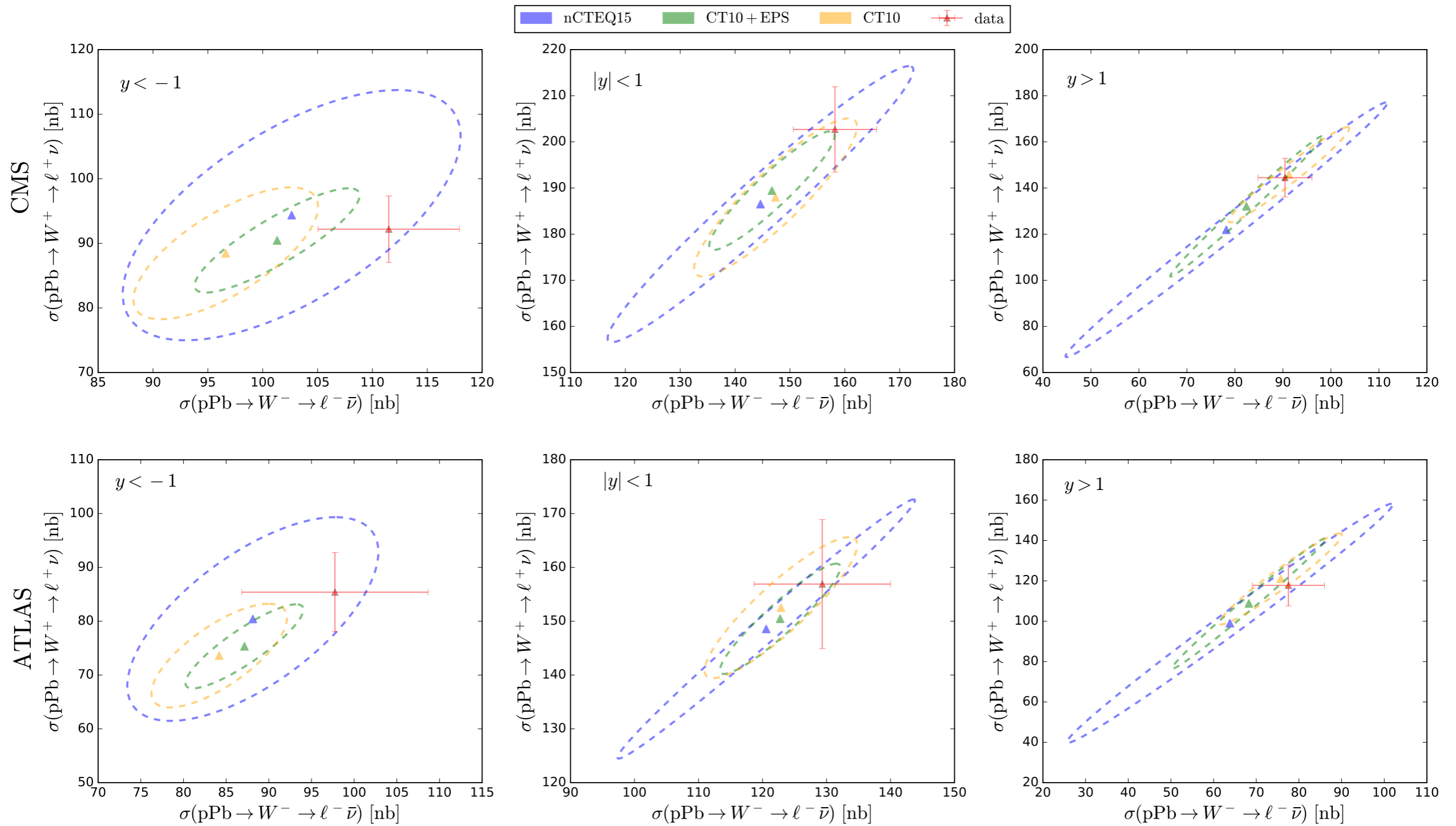
# Z-boson rapidity distributions



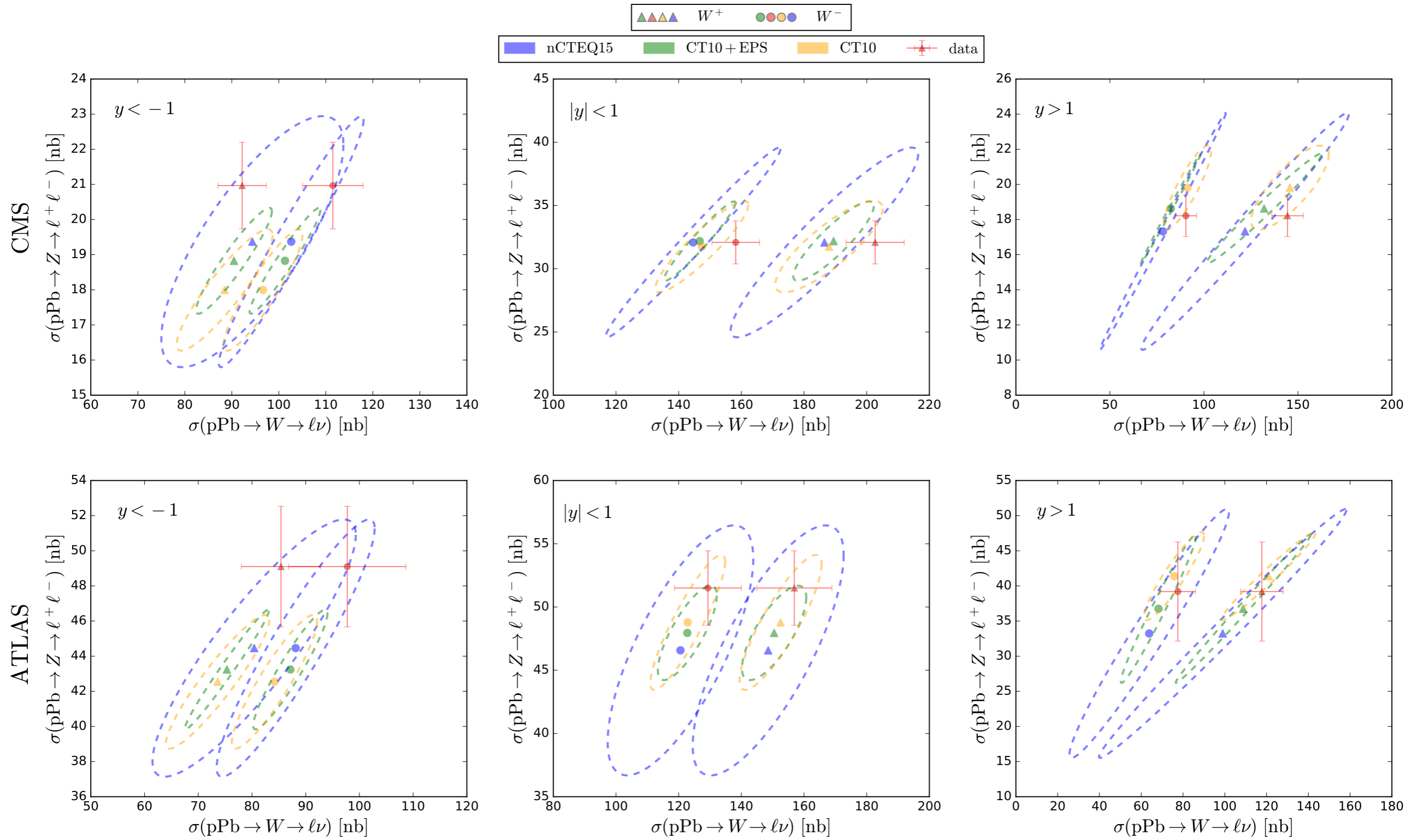
# W-boson rapidity distributions



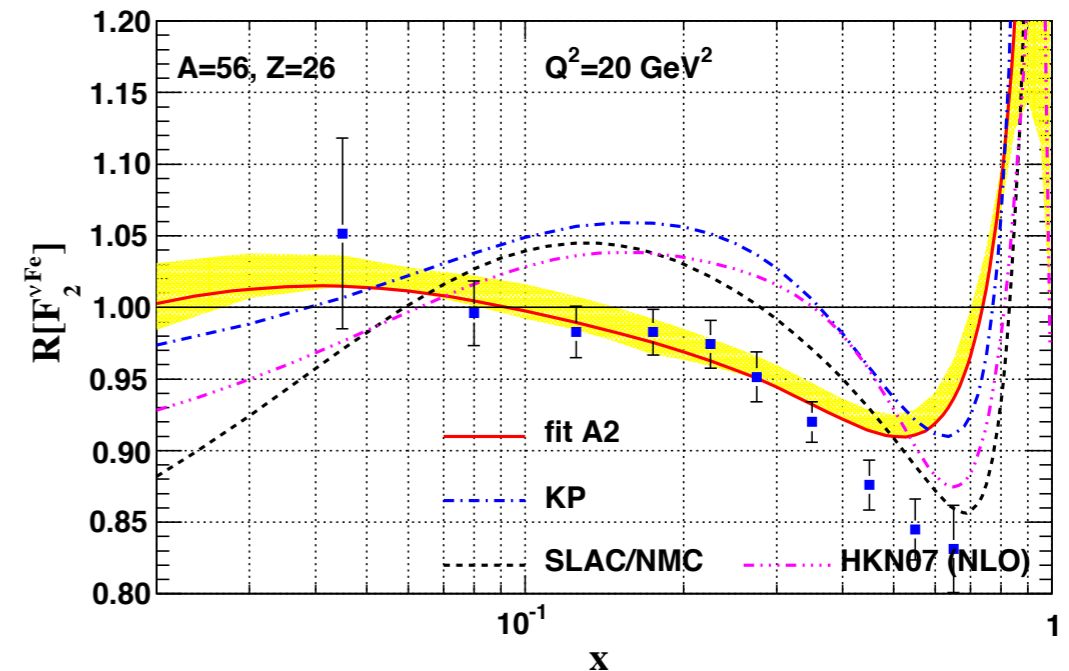
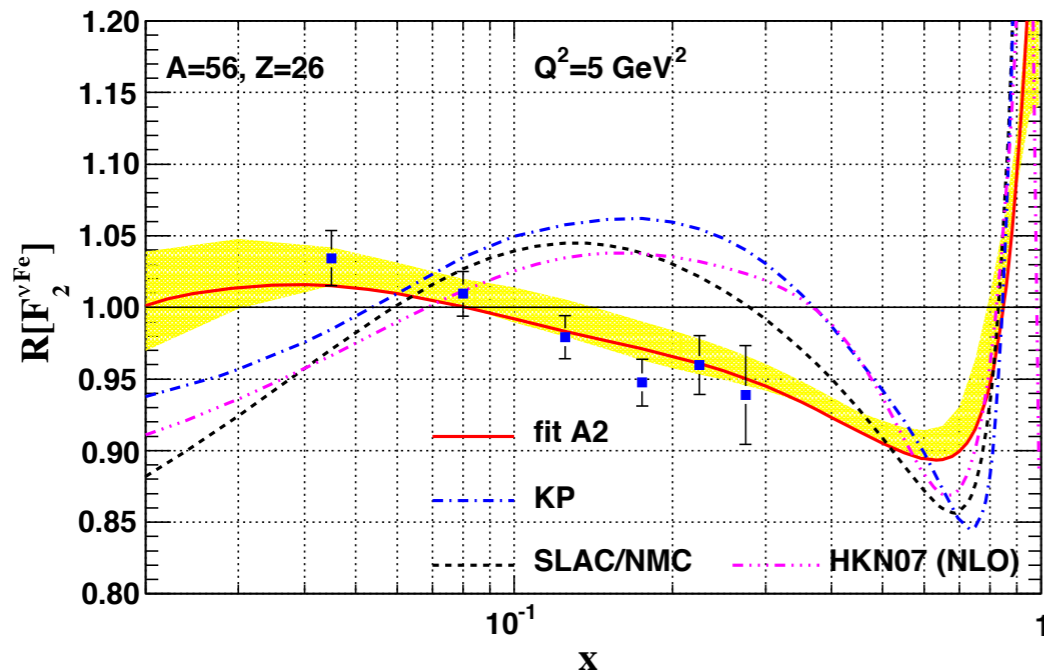
# $(W^+, W^-)$ Correlation



# (Z,W) Correlation



# NUCLEAR CORRECTION FACTOR $R[F_2^{\nu Fe}]$



- Are nuclear corrections in charged-lepton and neutrino DIS different?
- Obviously the PDFs from fits to  $\ell A + DY$  data do not describe the neutrino DIS data.
- However, a better flavor decomposition could be possible resulting from a global analysis of  $\ell A$ ,  $DY$  and  $\nu A$  data.

Note:  $x_{\min} = 0.02$  in these figures.

# TOLERANCE CRITERION

Probability distribution for the  $\chi^2$  function

$$P_N(\chi^2) = \frac{(\chi^2)^{N/2-1} e^{-\chi^2/2}}{2^{N/2} \Gamma(N/2)}$$

Determine  $\xi_{50}^2$  and  $\xi_{90}^2$  (i.e.  $p = 50$ ,  $p = 90$ ):

$$\int_0^{\xi_p^2} d\chi^2 P_N(\chi^2) = p/100$$

Condition for compatibility of two fits:

The 2nd fit ( $\chi_n^2$ ) should be within the 90% C.L. region of the first fit ( $\chi_{n,0}^2$ )

$$\chi_n^2 / \chi_{n,0}^2 < \xi_{90}^2 / \xi_{50}^2 \quad \Leftrightarrow \quad C_{90} \equiv \frac{\Delta\chi^2}{\frac{\chi_{n,0}^2}{\xi_{50}^2} (\xi_{90}^2 - \xi_{50}^2)} < 1$$

see CTEQ'01, PRD65(2001)014012; MSTW'09, EPJC(2009)63,189-285